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## *Control and Modeling of Power Electronics*



<https://www.ieee-pels.org/technical-activities/tc-1>



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# Model Predictive Control for Power Electronics Applications

Prof. Marco Rivera

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## Outline

- Power Electronics, Machines and Control Group
- Introduction to Predictive Control in Power Converters and Electrical Drives
- Examples of Predictive Control in Power Converters and Electrical Drives
- Technical Issues for the Implementation of Predictive Control
- Trends and Challenges of Predictive Control
- Conclusions
- Q&A/Discussion



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# Power Electronics, Machines and Control Research Group



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## Power Electronics and Machine Centre PEMC Research Group



Prof. Marco Rivera



- Transport electrification and energy conversion
- One of the largest integrated PEMD group worldwide
- National/European leader
- >£45M active research grants with >60% of research income linked to industry



# Power Electronics, Machines and Control Research Group

## Research Themes

- Electrical machines
- Power electronic systems
- Electric motor drives and systems
- Power electronic integration and reliability

## Underlying Scientific Research

- Power device packaging and cooling
- Microgrid control
- Cooling methodologies and thermal integration
- New modelling methods
- Electromagnetic modelling
- Modulation theory
- Physics of failure – power converters and electrical machines
- Advanced control strategies for power converters and drives



## More than 200 Researchers/Academics

- ≈ 26 Academic staff [Faculty]
- ≈ 70 Contract research fellows
- ≈ 110 PhD students
- ≈ 12 Visiting scholars/researchers

## Application Areas - Electrification

- Future electricity networks
- Renewable energy
- Microgrids and grid connected converters
- Industrial applications
- Automotive and marine
- All/more electric aircraft

## New PEMC Group Facilities - opened March 2021

- 5500m<sup>2</sup> laboratories with 5MVA power supply
- Voltage supplies to 11kV
- Power systems – DC and AC
- Electrical machine testing up to 20MW
- Environmental chambers

**Current Research Grants ≈ US\$45M**

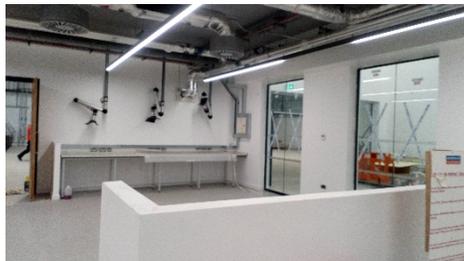


# Power Electronics, Machines and Control Research Group: Building Layout

## Power Electronics Laboratory

Power electronics, devices and converters. Facility for construction, characterisation, analysis and lifetime testing.

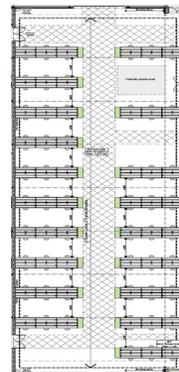
- 115m<sup>2</sup> environmental testing facility
- Clean room facilities
- X-ray and microcopy space
- Magnetic testing facility
- 38m<sup>2</sup> EMC shielded room



## Power Electronic Converters and Motor Drives Laboratory

General Machine and Converter testing: work on standard sized electrical machines, motor drives and power converters

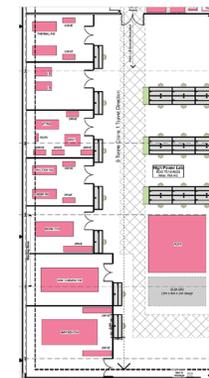
- 80 standard research benches with integrated guarding
- 3-phase 400V @ 64A per bench plus single phase sockets
- 50kW liquid cooling loop



## Wolfson High Power Laboratory

For high power, high voltage and large power electronic converter and motor drive system testing

- 5MW total site mains supply
  - 1.1/3.3kW @ 3000A HVAC
  - 400V @ 4000A LVAC
  - 6kV HVDC
- Thermal test cell – 40m<sup>2</sup>
- High speed testing – 18m<sup>2</sup> sunken test rig space

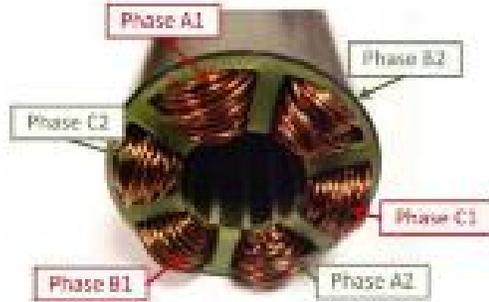




# Electrical Machine Demonstrators



150 kW, 32krpm PM generator – 16kW/kg



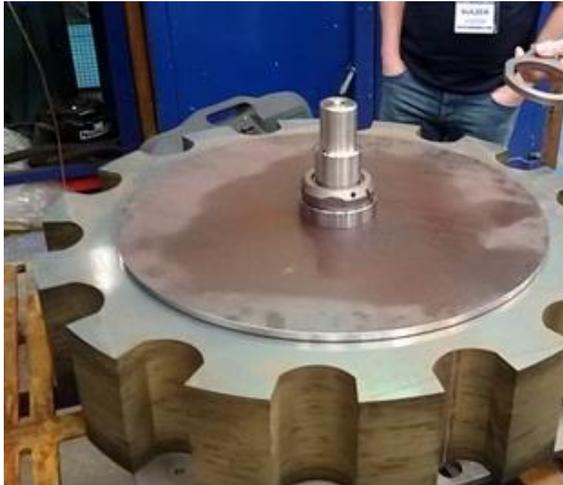
Fault-tolerant multi-phase machine



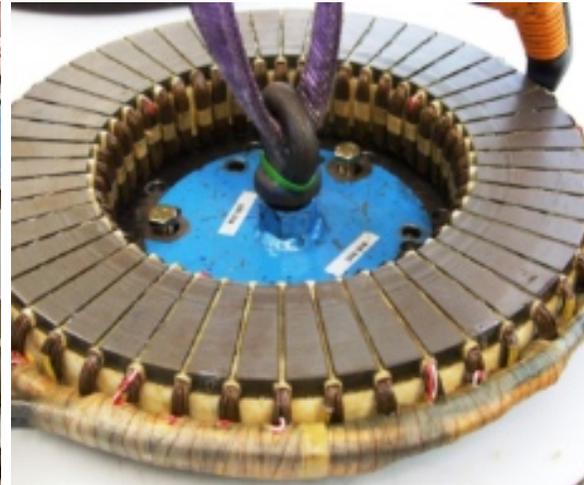
7kNm machine for aircraft taxiing –  
43 Nm/kg and 184 kNm/m<sup>3</sup>



PM assist – SynRel machine  
for EV applications



SRM for energy storage



Integrated dual-airgap axial machine



24V, 5kW, 120 krpm PM machine turbo  
compounding

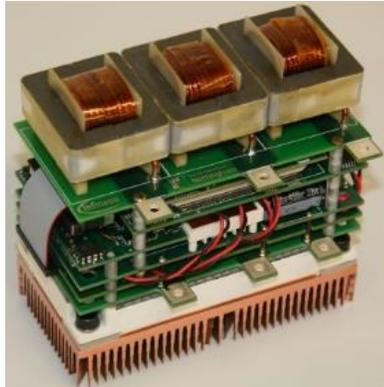


# Power Electronics Converters

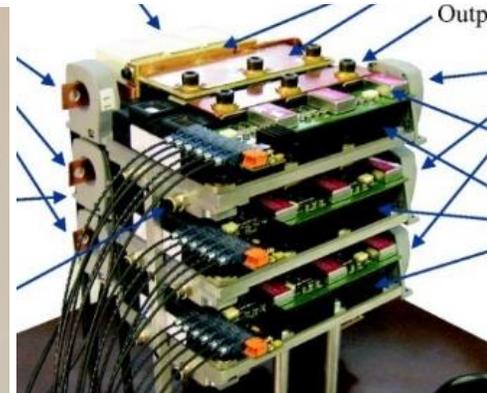


30kW matrix integrated into machine endplate

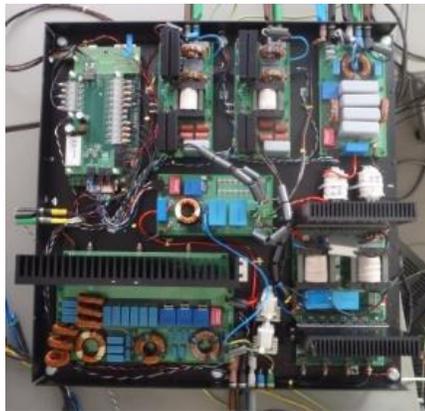
20kW/litre SiC JFET matrix converter



150kW Si/SiC matrix converter



3.3kW, 500kW modular AC-AC converter



Aerospace SiC Mosfet DC-DC converter



450kW dual-bridge CSR converter



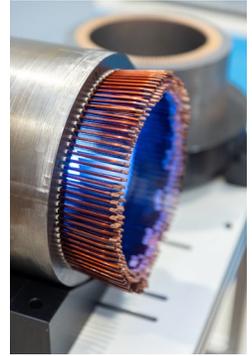
Fault-tolerant multi-phase 4MVA e-drive



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# Power Electronics, Machines and Control Research Group





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# Introduction

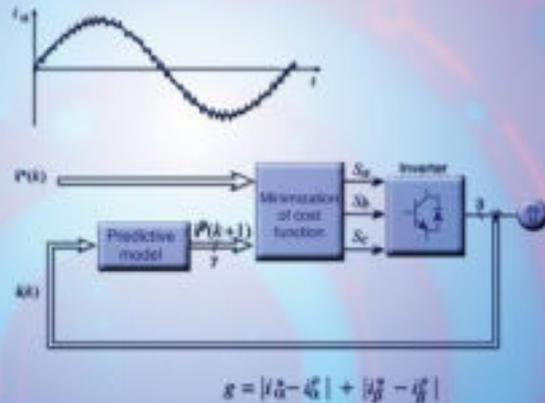


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# Predictive Control of Power Converters and Electrical Drives

Jose Rodriguez  
Patricio Cortes



WILEY

IEEE



IEEE TRANSACTIONS ON INDUSTRIAL ELECTRONICS, VOL. 64, NO. 2, FEBRUARY 2017

935

## Model Predictive Control for Power Converters and Drives: Advances and Trends

Sergio Vazquez, *Senior Member, IEEE*, Jose Rodriguez, *Fellow, IEEE*, Marco Rivera, *Member, IEEE*, Leopoldo G. Franquelo, *Fellow, IEEE*, and Margarita Norambuena, *Member, IEEE*

**Abstract**—Model predictive control (MPC) is a very attractive solution for controlling power electronic converters. The aim of this paper is to present and discuss the latest developments in MPC for power converters and drives, describing the current state of this control strategy and analyzing the new trends and challenges it presents when applied to power electronic systems. The paper revisits the operating principle of MPC and identifies three key elements in the MPC strategies, namely the prediction model, the cost function, and the optimization algorithm. This paper summarizes the most recent research concerning these elements, providing details about the different solutions proposed by the academic and industrial communities.

apply in multivariable systems, and presents a fast dynamic response. Further, it allows for nonlinearities and constraints to be incorporated into the control law in a straightforward manner, and it can incorporate nested control loops in only one loop [4], [5].

In particular, power electronic applications require control responses in the order of tens to hundreds of microseconds to work properly. However, it is well known that MPC has a larger computational burden than other control strategies. For this reason, most of the works focused on this issue at the initial research stages of MPC for power electronic systems [6].

[Model Predictive Control for Power Converters and Drives: Advances and Trends | IEEE Journals & Magazine | IEEE Xplore](#)

## A Review on Weighting Factor Design of Finite Control Set Model Predictive Control Strategies for AC Electric Drives

Emrah Zerdali, *Senior Member, IEEE*, Marco Rivera, *Senior Member, IEEE*, and Patrick Wheeler, *Fellow, IEEE*

[A Review on Weighting Factor Design of Finite Control Set Model Predictive Control Strategies for AC Electric Drives](#)

## - Basic Principles of Model Predictive Control

A PREDICTIVE CONTROLLER FOR THE STATOR CURRENT VECTOR  
OF AC MACHINES FED FROM A SWITCHED VOLTAGE SOURCE

Joachim Holtz and Siegfried Stadtfeld

Laboratory for Electrical Machines and Drives, University of Wuppertal  
Postfach 10 01 27, 5600 Wuppertal 1, West-Germany

### Abstract

The paper describes a novel approach to the PWM problem based on an on-line optimization of the switching sequence. In this concept, the standard pulsewidth modulator is completely eliminated. Input quantities to a switching controller are the stator current vector components as supplied by a field oriented control system. These are used to control the current vector trajectory in the complex plane such that a minimum spatial error with respect to the reference vector is maintained. In this way, the computation of the stator voltage reference signals usually required in PWM systems is avoided. A predictive algorithm is implemented in the switching controller to obtain minimum current harmonics at minimum switching frequency. The optimization is effective under all operating conditions including transients and zero stator frequency operation.

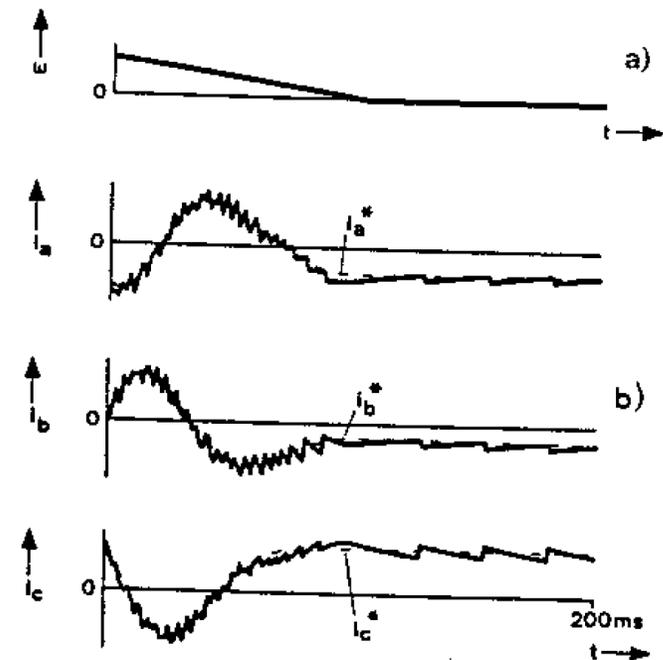


Fig. 13. Braking and operation at zero stator frequency  
a) speed  
b) stator currents



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## - Basic Principles of Model Predictive Control





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## - Basic Principles of Model Predictive Control

### **New Modulation Strategy for a Matrix Converter with a Very Small Mains Filter**

Stefan Müller Ulrich Ammann Stephan Rees

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phone: +49 (0) 711 / 6 85 - 73 87, fax: +49 (0) 711 / 685 - 73 78  
e-mail: [ammann@ilr.uni-stuttgart.de](mailto:ammann@ilr.uni-stuttgart.de), www: <http://www.uni-stuttgart.de/ilr>

[New modulation strategy for a matrix converter with a very small mains filter](#) | IEEE Conference Publication | IEEE Xplore

### **Predictive control of three-phase inverter**

J. Rodríguez, J. Pontt, C. Silva, M. Salgado, S. Rees,  
U. Ammann, P. Lezana, R. Huerta and P. Cortés

A new method for current control based on a predictive strategy is presented. This uses a discrete-time model of the load to predict the future value of the current for each of the possible voltage vectors generated by the inverter. The vector which minimises the current error at the next sampling time is selected. Experimental results that confirm the feasibility of the method are given.

[Predictive control of three-phase inverter](#) – Electronics Letters 2004



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## - Basic Principles of Model Predictive Control

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e-mail: [ammann@ilr.uni-stuttgart.de](mailto:ammann@ilr.uni-stuttgart.de), www: <http://www.uni-stuttgart.de/ilr>

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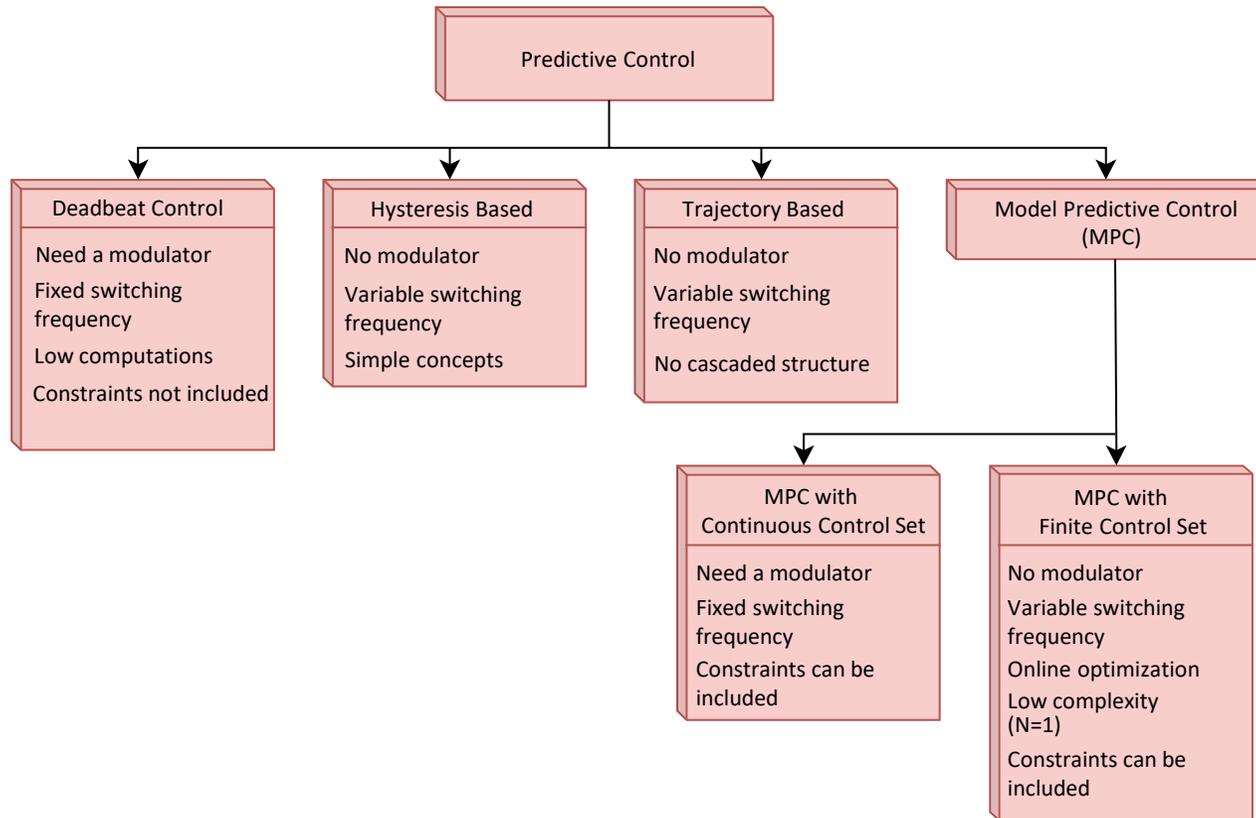
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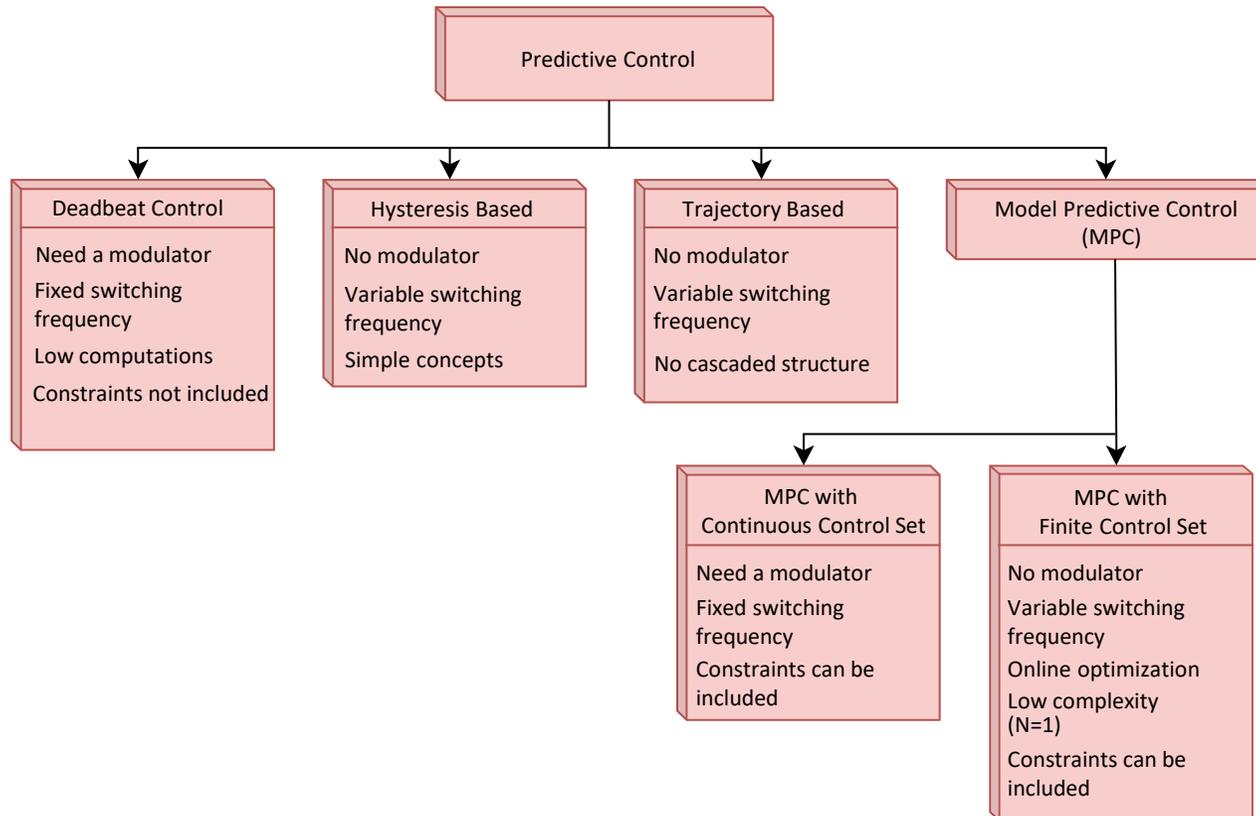
MPC uses a **model of the system** to predict the behavior of the controlled variables and then select the actuation sequence **that minimizes a certain cost function**. The cost function represents **the desired behavior of the system**.



## - Basic Principles of Model Predictive Control: Control Strategies

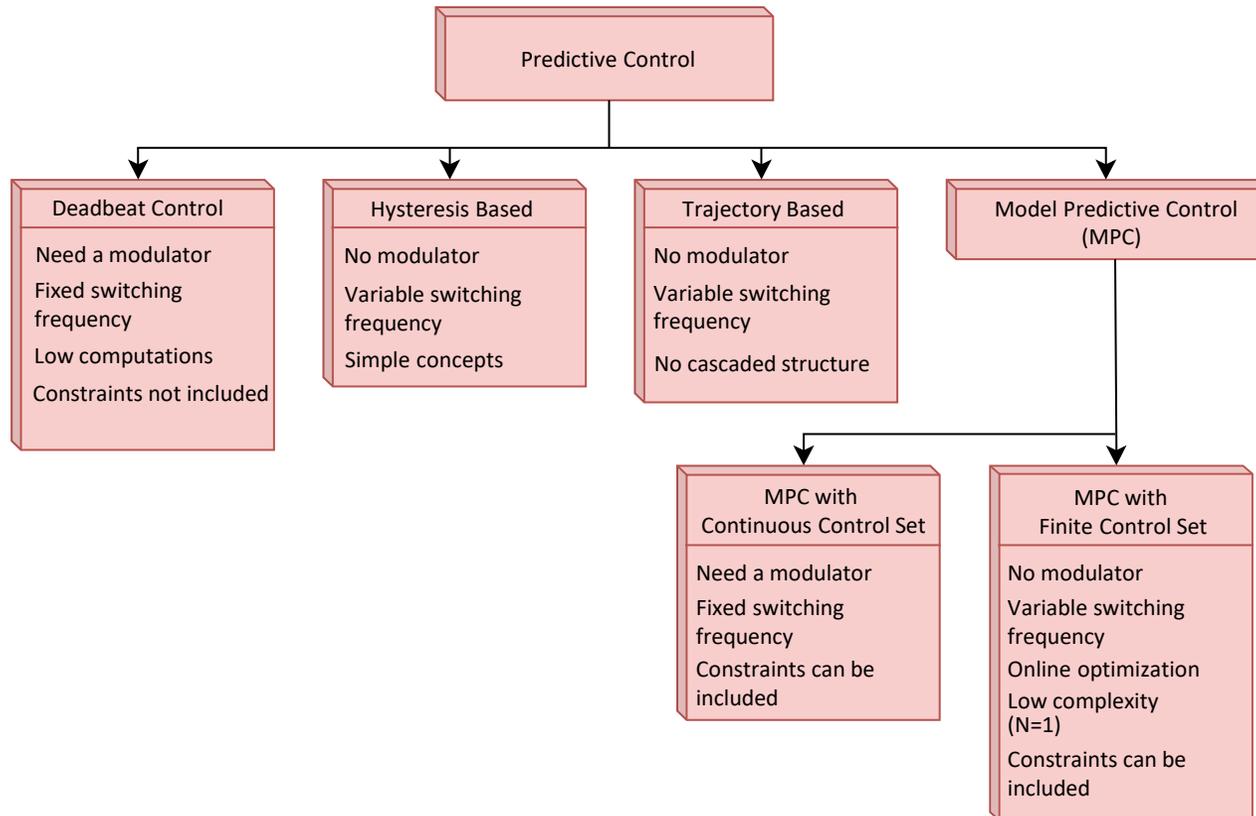


## - Basic Principles of Model Predictive Control: Control Strategies



The main characteristic of predictive control is **the use of the model of the system** for prediction of the future behavior of the controlled variables.

## - Basic Principles of Model Predictive Control: Control Strategies



The main characteristic of predictive control is **the use of the model of the system** for prediction of the future behavior of the controlled variables.

This information is used by the controller in order to obtain the **optimal actuation**, according to a predefined optimization criterion.



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## - Basic Principles of Model Predictive Control: Advantages

- Concepts are very intuitive and easy to understand.
- It can be applied to a great variety of systems.
- The multivariable case can be easily considered.
- Delay times can be compensated.
- Easy inclusion of nonlinearities in the model.
- Simple treatment of constraints.
- The resulting controller is easy to implement.
- This methodology is open to include modifications and extensions depending on specific applications.



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## - Basic Principles of Model Predictive Control: Disadvantages

- Large amount of calculations.
- The quality of the model has a direct influence on the quality of the resulting controller.
- In the classical MPC strategy is observed a variable switching frequency.
- When there are several objectives weighting factors are needed.

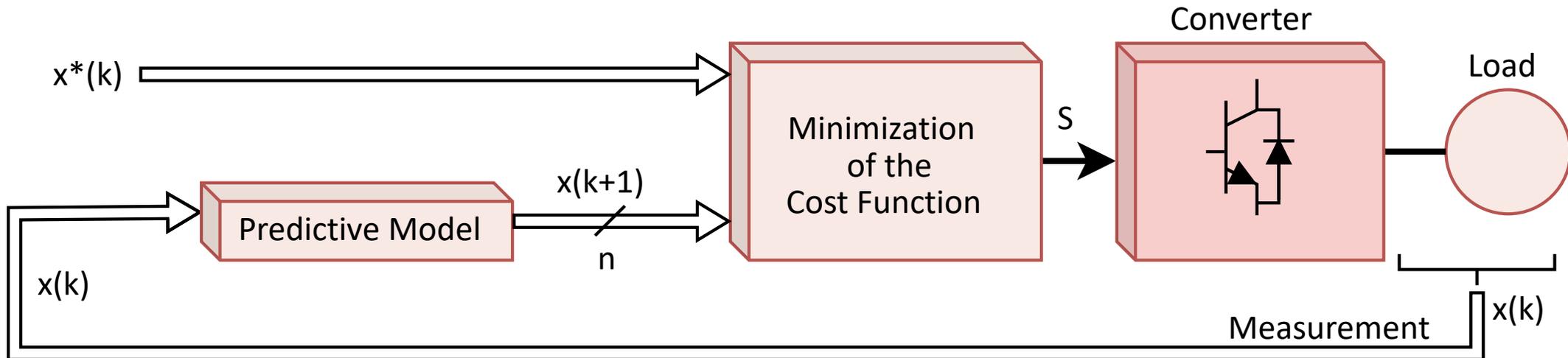


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# Predictive Control for Power Converters and Electrical Drives

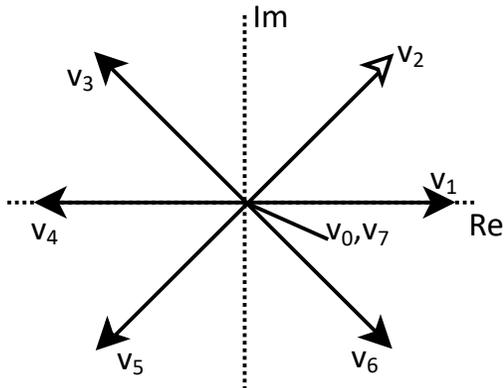
## - Controller Design: General MPC Scheme for Power Converters





## - Controller Design: How Does it Work?

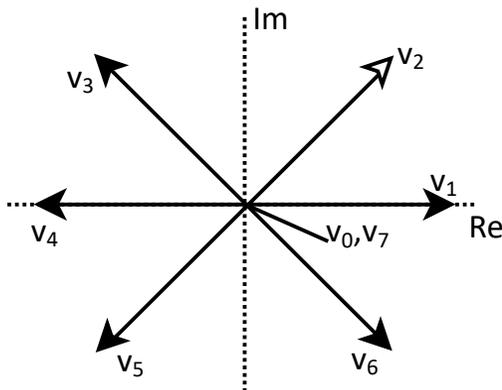
- The converter is modelled as a system with finite states





## - Controller Design: How Does it Work?

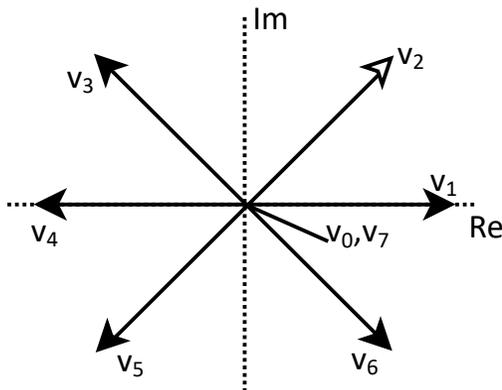
- The converter is modelled as a system with finite states
- A model of the load is used to predict the behaviour for each possible switching state



$$\hat{\mathbf{i}}(k+1) = \left(1 - \frac{RT_s}{L}\right) \mathbf{i}(k) + \frac{T_s}{L} (\mathbf{v}(k) - \hat{\mathbf{e}}(k))$$

## - Controller Design: How Does it Work?

- The converter is modelled as a system with finite states
- A model of the load is used to predict the behaviour for each possible switching state
- A cost function is defined and represents the desired behaviour of the system

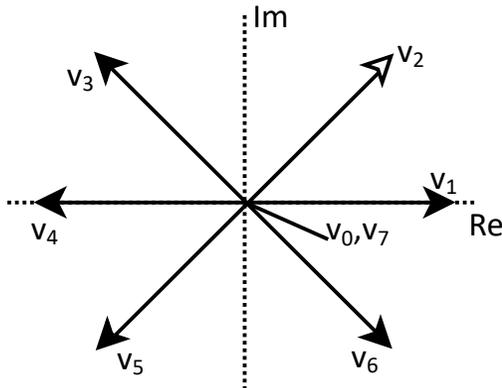


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$$g = |i_{\alpha}^* - i_{\alpha}^p| + |i_{\beta}^* - i_{\beta}^p|$$

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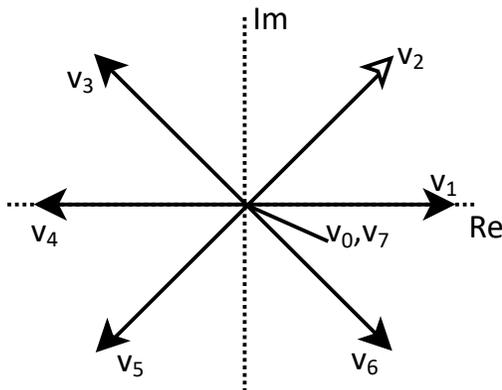


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$$g = |i_{\alpha}^* - i_{\alpha}^p| + |i_{\beta}^* - i_{\beta}^p| \quad g_{\min} = \min \{ g \}$$

... and that is all!!



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## Predictive Control for Power Converters and Electrical Drives

# Examples



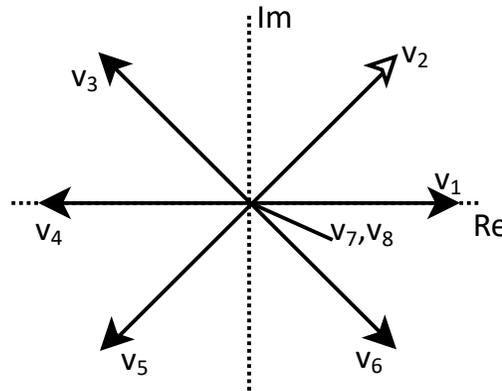
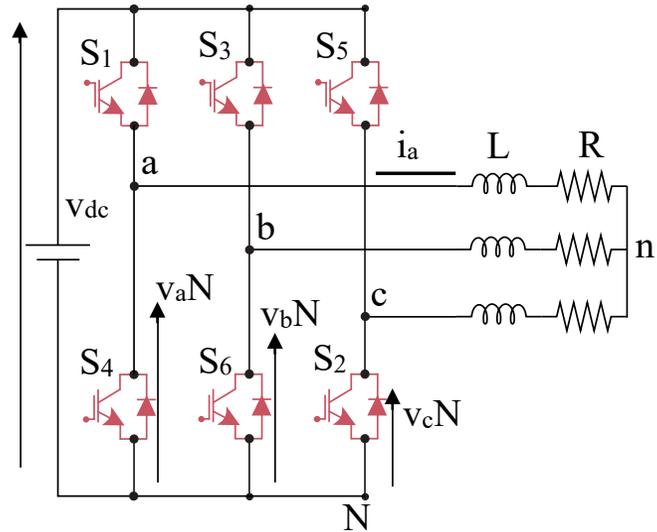
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**Predictive Control for Power Converters and Electrical Drives**

# Model Predictive Control for Three Phase Inverter

## - Two Level Voltage Source Inverter: Topology and Switching States

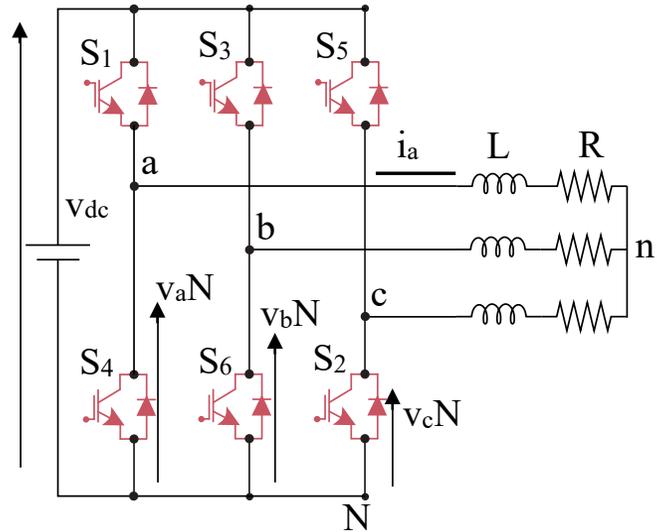


Valid Switching States of the VSI

| # | $S_{r1}$ | $S_{r2}$ | $S_{r3}$ | $S_{r4}$ | $S_{r5}$ | $S_{r6}$ |
|---|----------|----------|----------|----------|----------|----------|
| 1 | 1        | 1        | 0        | 0        | 0        | 1        |
| 2 | 1        | 1        | 1        | 0        | 0        | 0        |
| 3 | 0        | 1        | 1        | 1        | 0        | 0        |
| 4 | 0        | 0        | 1        | 1        | 1        | 0        |
| 5 | 0        | 0        | 0        | 1        | 1        | 1        |
| 6 | 1        | 0        | 0        | 0        | 1        | 1        |
| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

- 6 commutation devices
- 8 valid switching states

## - Two Level Voltage Source Inverter: Converter Model



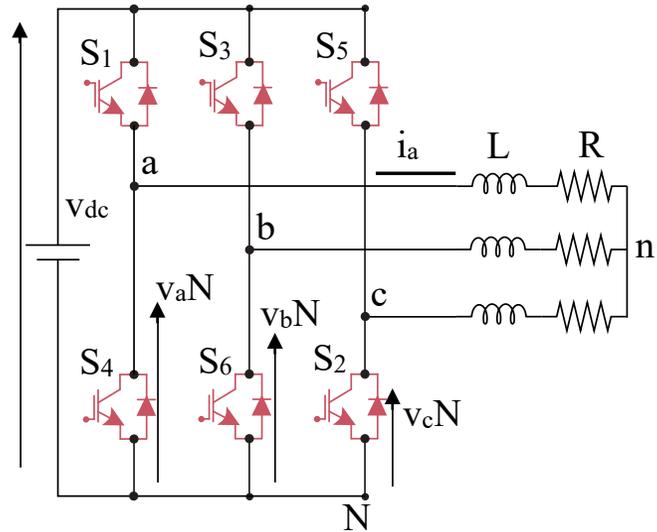
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| 4 | 0        | 0        | 1        | 1        | 1        | 0        |
| 5 | 0        | 0        | 0        | 1        | 1        | 1        |
| 6 | 1        | 0        | 0        | 0        | 1        | 1        |
| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

$$i_{dc} = [ S_1 \quad S_3 \quad S_5 ] \mathbf{i}$$

$$\mathbf{v} = \begin{bmatrix} S_1 \\ S_3 \\ S_5 \end{bmatrix} v_{dc}$$

## - Two Level Voltage Source Inverter: Load Model

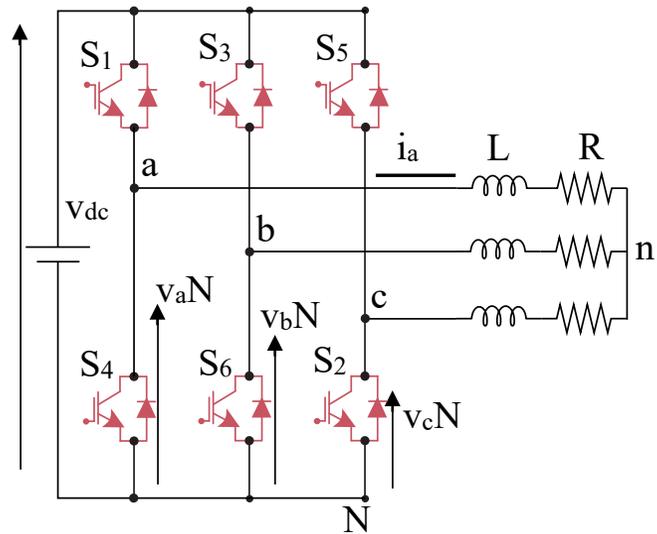


Valid Switching States of the VSI

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| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

$$\mathbf{v} = L \frac{d\mathbf{i}}{dt} + R\mathbf{i}$$

## - PCC of a Two Level Voltage Source Inverter: Discrete Model



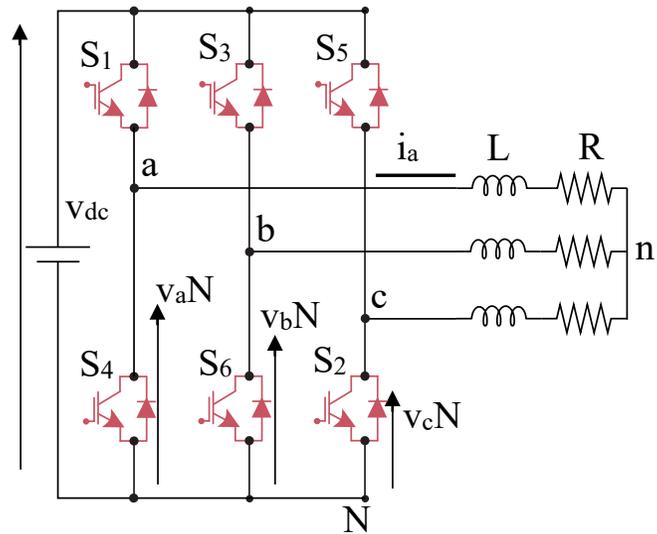
Valid Switching States of the VSI

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| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

- Considering Euler approximation

$$\mathbf{i}^{k+1} = \left(1 - \frac{RT_s}{L}\right) \mathbf{i}^k + \frac{T_s}{L} \mathbf{v}^k$$

## - PCC of a Two Level Voltage Source Inverter: Discrete Model



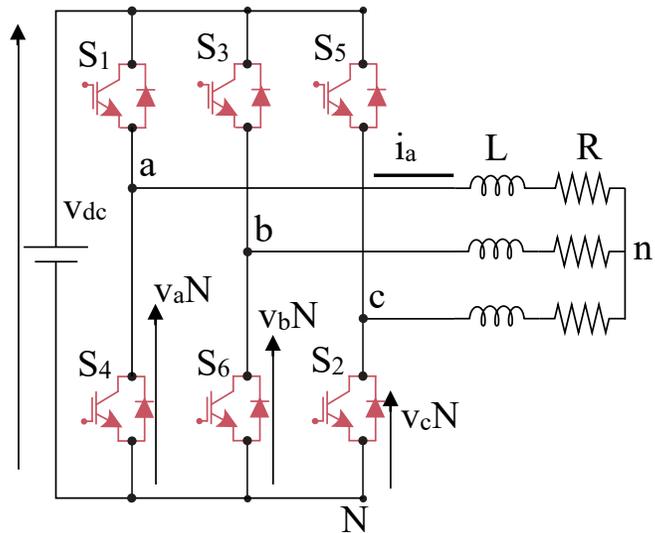
Valid Switching States of the VSI

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| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

- Considering Euler approximation

$$\mathbf{i}^{k+1} = \left(1 - \frac{RT_s}{L}\right) \mathbf{i}^k + \frac{T_s}{L} \mathbf{v}^k \quad \mathbf{v} = \begin{bmatrix} S_1 \\ S_3 \\ S_5 \end{bmatrix} v_{dc}$$

## - PCC of a Two Level Voltage Source Inverter: Cost Function



Valid Switching States of the VSI

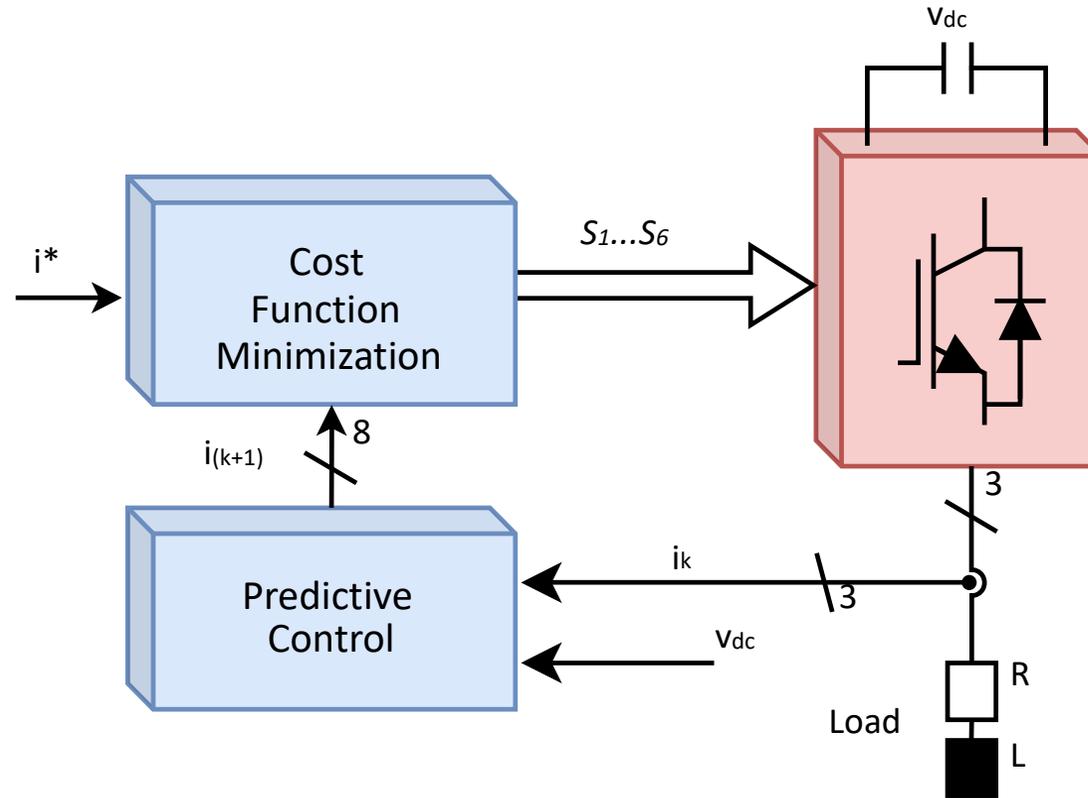
| # | $S_{r1}$ | $S_{r2}$ | $S_{r3}$ | $S_{r4}$ | $S_{r5}$ | $S_{r6}$ |
|---|----------|----------|----------|----------|----------|----------|
| 1 | 1        | 1        | 0        | 0        | 0        | 1        |
| 2 | 1        | 1        | 1        | 0        | 0        | 0        |
| 3 | 0        | 1        | 1        | 1        | 0        | 0        |
| 4 | 0        | 0        | 1        | 1        | 1        | 0        |
| 5 | 0        | 0        | 0        | 1        | 1        | 1        |
| 6 | 1        | 0        | 0        | 0        | 1        | 1        |
| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |

$$g(k + 1) = (\mathbf{i}^* - \mathbf{i}^{k+1})^2$$

- The current error must be zero
- From the valid switching states, the one that minimizes the cost function is selected to be applied in the next sampling time

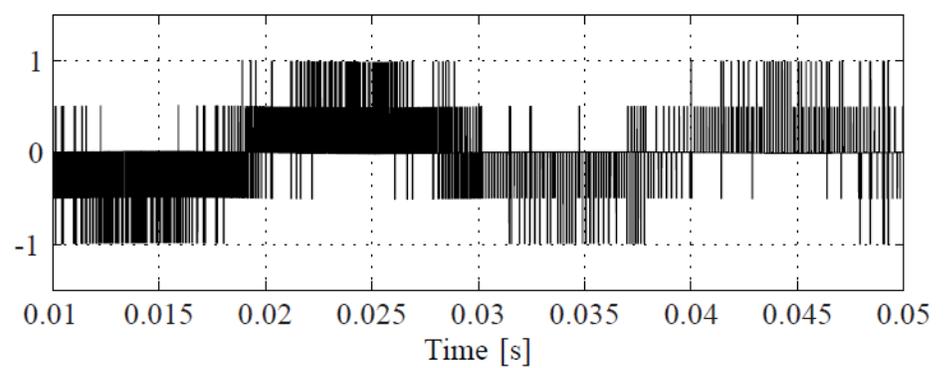
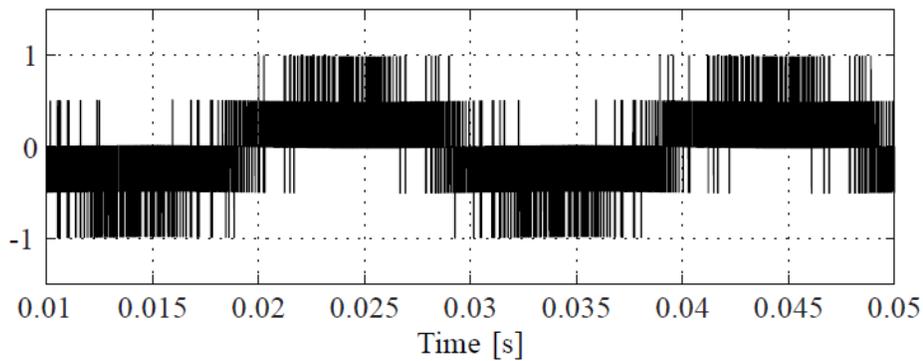
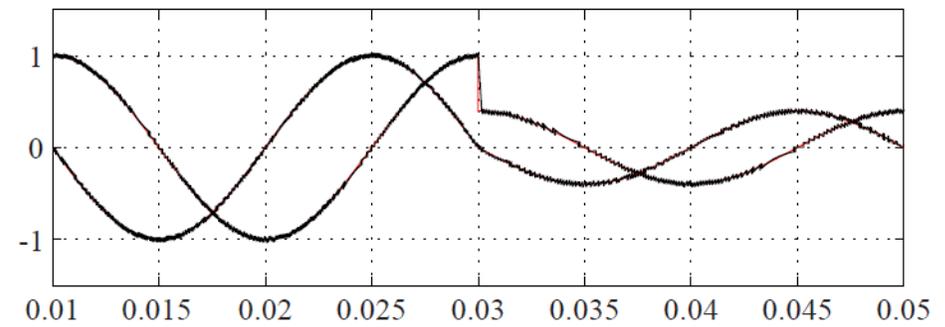
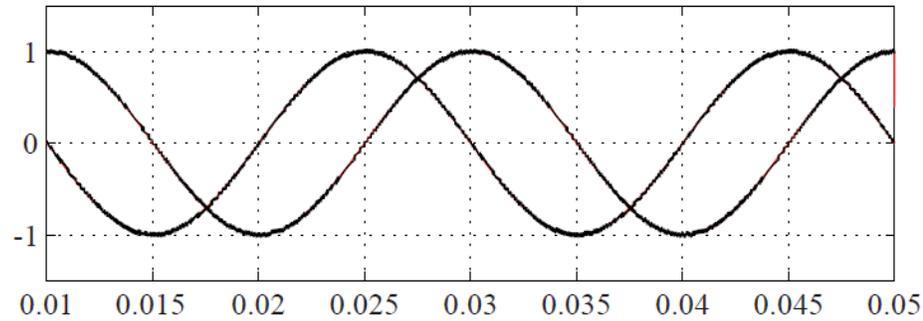


## - PCC of a Two Level Voltage Source Inverter: Control Scheme





## - PCC of a Two Level Voltage Source Inverter: Simulated Results





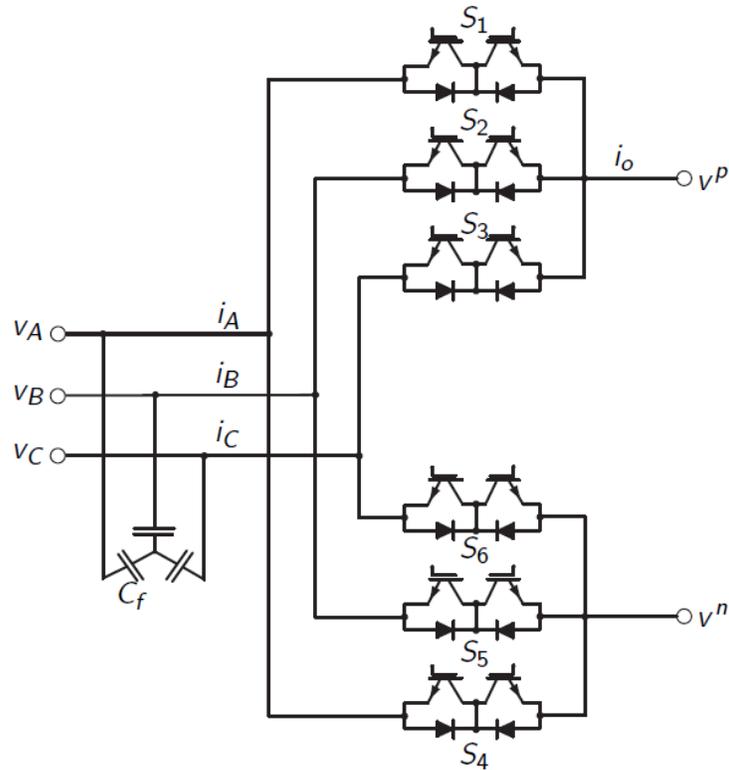
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## Predictive Control for Power Converters and Electrical Drives

# Model Predictive Control for a Single-Phase Matrix Converter

# - MPC of a Single-Phase Matrix Converter: Mathematical Model



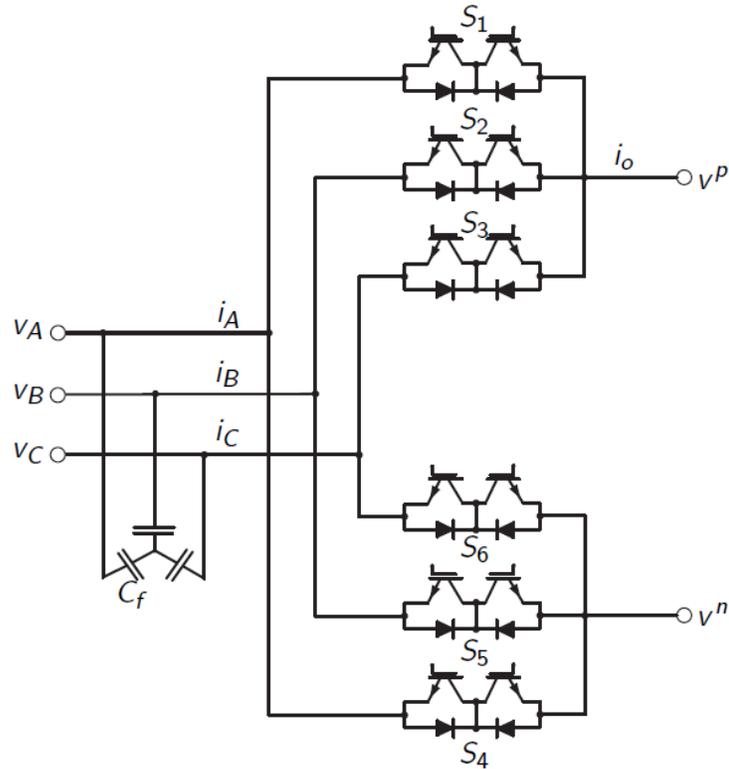
$$v^P = [ S_1 \quad S_2 \quad S_3 ] \mathbf{v}_i,$$

$$v^N = [ S_4 \quad S_5 \quad S_6 ] \mathbf{v}_i.$$

$$\mathbf{i}_i = \begin{bmatrix} S_1 - S_4 \\ S_2 - S_5 \\ S_3 - S_6 \end{bmatrix} i_o. \quad (1)$$



## - MPC of a Single-Phase Matrix Converter: Nine Valid Switching States



$$v^P = [ S_1 \quad S_2 \quad S_3 ] \mathbf{v}_i,$$

$$v^N = [ S_4 \quad S_5 \quad S_6 ] \mathbf{v}_i.$$

$$\mathbf{i}_i = \begin{bmatrix} S_1 - S_4 \\ S_2 - S_5 \\ S_3 - S_6 \end{bmatrix} i_o. \quad (1)$$

| # | $S_1$ | $S_2$ | $S_3$ | $S_4$ | $S_5$ | $S_6$ | $v^P$ | $v^N$ | $i_A$  | $i_B$  | $i_C$  |
|---|-------|-------|-------|-------|-------|-------|-------|-------|--------|--------|--------|
| 1 | 0     | 0     | 1     | 0     | 0     | 1     | $V_C$ | $V_C$ | 0      | 0      | 0      |
| 2 | 0     | 1     | 0     | 0     | 1     | 0     | $V_B$ | $V_B$ | 0      | 0      | 0      |
| 3 | 1     | 0     | 0     | 1     | 0     | 0     | $V_A$ | $V_A$ | 0      | 0      | 0      |
| 4 | 0     | 0     | 1     | 0     | 1     | 0     | $V_C$ | $V_B$ | 0      | $-i_o$ | $i_o$  |
| 5 | 0     | 0     | 1     | 1     | 0     | 0     | $V_C$ | $V_A$ | $-i_o$ | 0      | $i_o$  |
| 6 | 0     | 1     | 0     | 0     | 0     | 1     | $V_B$ | $V_C$ | 0      | $i_o$  | $-i_o$ |
| 7 | 0     | 1     | 0     | 1     | 0     | 0     | $V_B$ | $V_A$ | $-i_o$ | $i_o$  | 0      |
| 8 | 1     | 0     | 0     | 0     | 0     | 1     | $V_A$ | $V_C$ | $i_o$  | 0      | $-i_o$ |
| 9 | 1     | 0     | 0     | 0     | 1     | 0     | $V_A$ | $V_B$ | $i_o$  | $-i_o$ | 0      |

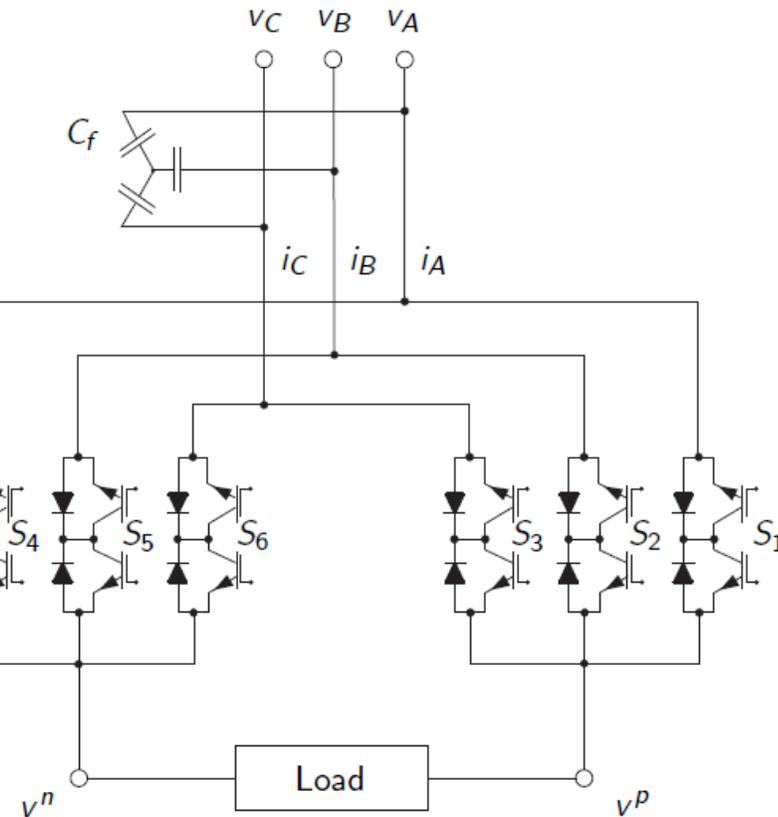
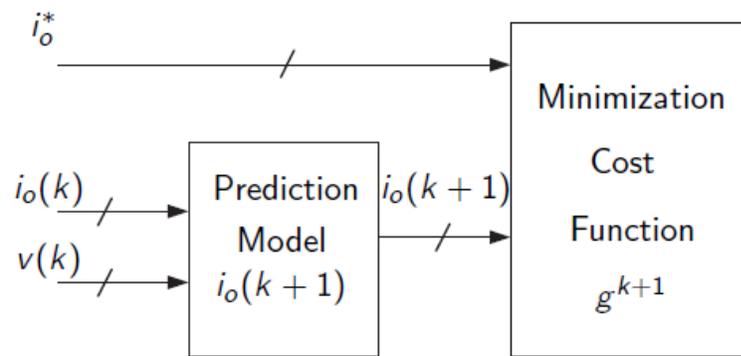
## - MPC of a Single-Phase Matrix Converter: Control Scheme

Predictive model:

$$i_o(k+1) = (T_s/L)v(k) + (1 - RT_s/L)i_o(k).$$

Cost function optimization:

$$g(k+1) = (i_o^*(k+1) - i_o(k+1))^2.$$



# - MPC of a Single-Phase Matrix Converter: Results

## Simulation

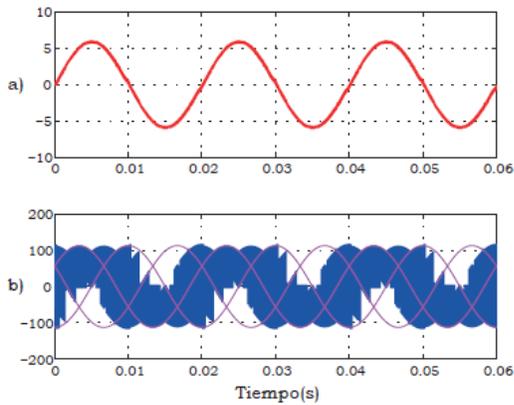


Fig. 1:  $i_o = 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;

## Experimental

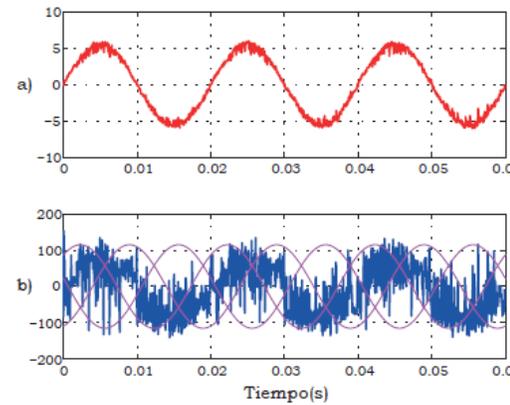


Fig. 2:  $i_o = 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;

## Simulation

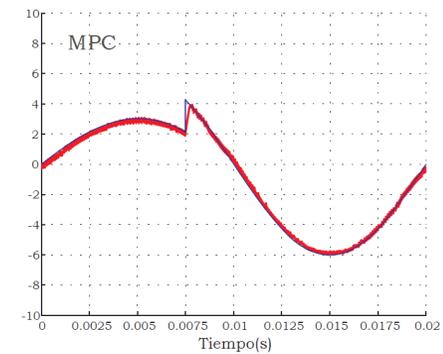


Fig. 3:  $i_o = 3 - 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;

## Experimental

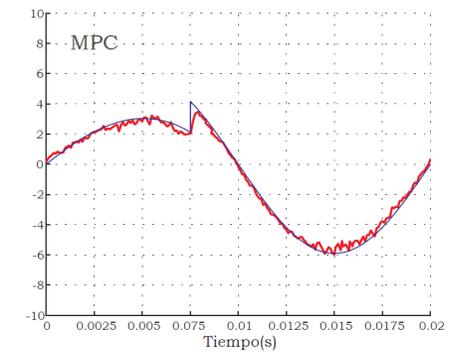


Fig. 4:  $i_o = 3 - 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;

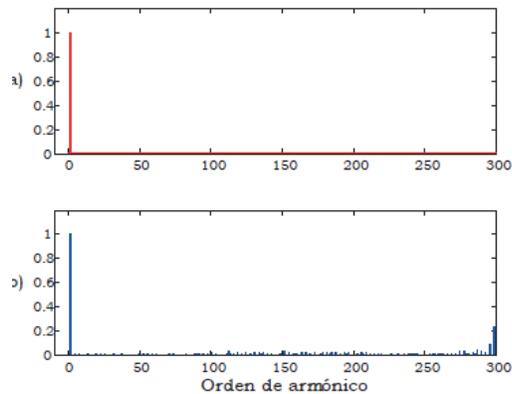


Fig. 3:  $i_o = 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;

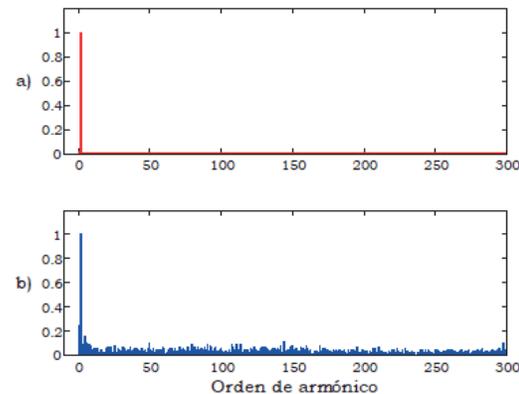
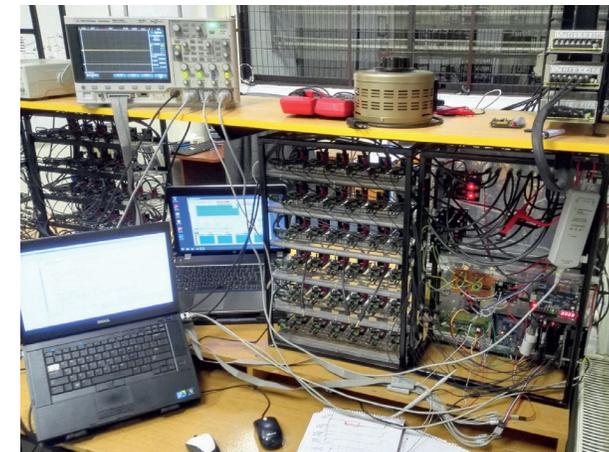


Fig. 4:  $i_o = 6 \text{ Apk}$ ;  $f_o = 50 \text{ Hz}$ ;  $f_s = 40 \text{ kHz}$ ;  $v_i = 112 \text{ V pk}$ ;





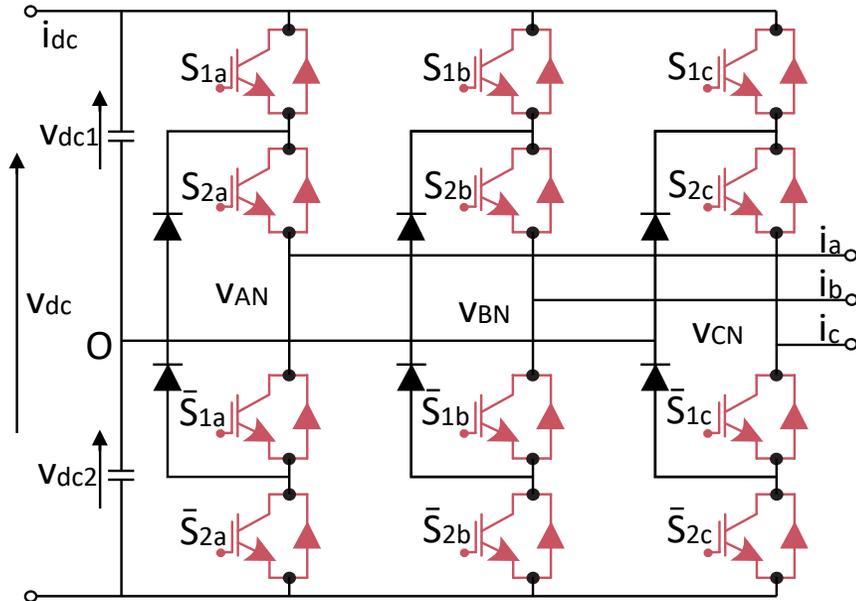
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**Predictive Control for Power Converters and Electrical Drives**

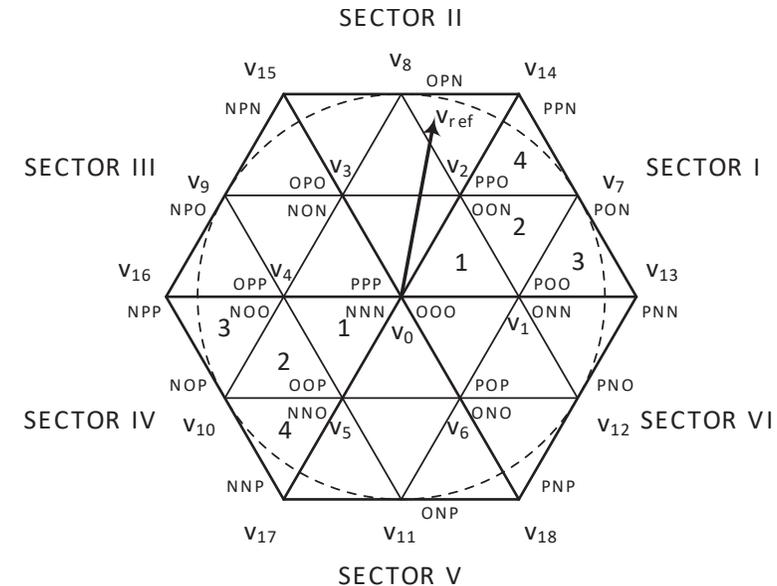
# Model Predictive Control for an NPC Inverter

## - NPC Inverter: Topology and Switching States

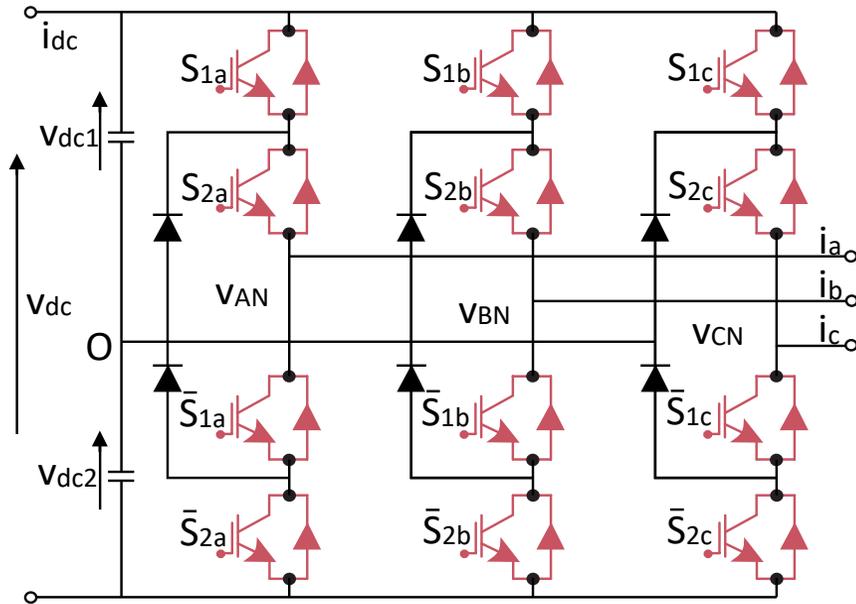


- Widely used in industry for high power medium voltage power conversion and drives
- 12 commutation devices
- 27 valid switching states

| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $V_{dc1} + V_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $V_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |



## - NPC Inverter: Converter Model

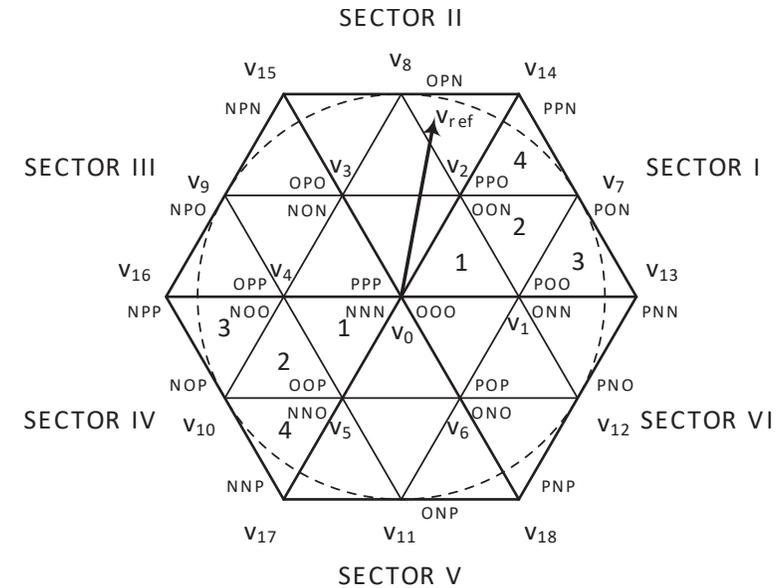


$$v_{xN} = v_{dc1}S_{1x} + v_{dc2}S_{2x}, \quad x = a, b, c$$

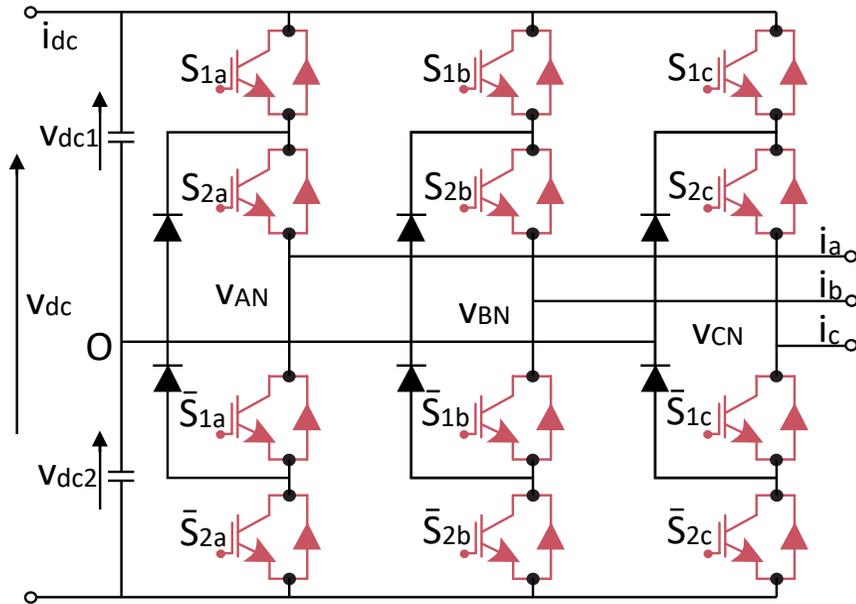
$$\frac{d v_{dc1}}{dt} = \frac{i_{dc1}}{C_1}$$

$$\frac{d v_{dc2}}{dt} = \frac{i_{dc2}}{C_2}$$

| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xN}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $v_{dc1} + v_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $v_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |

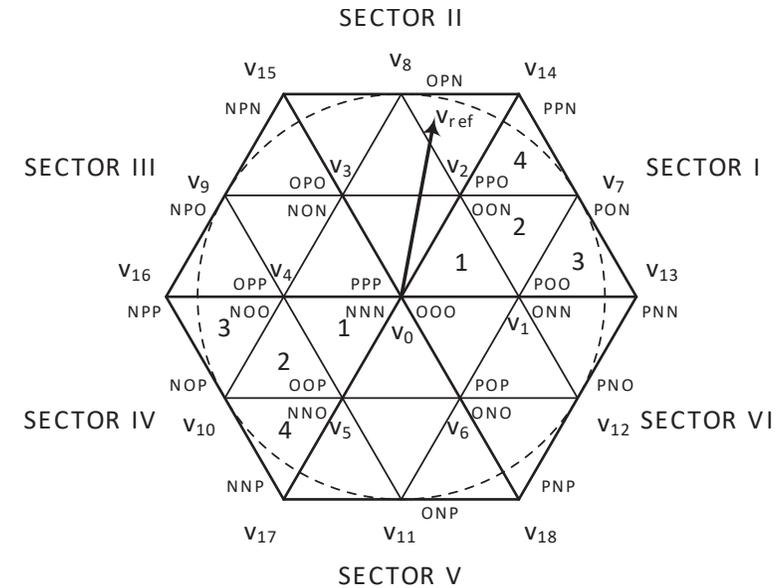


## - NPC Inverter: Load Model

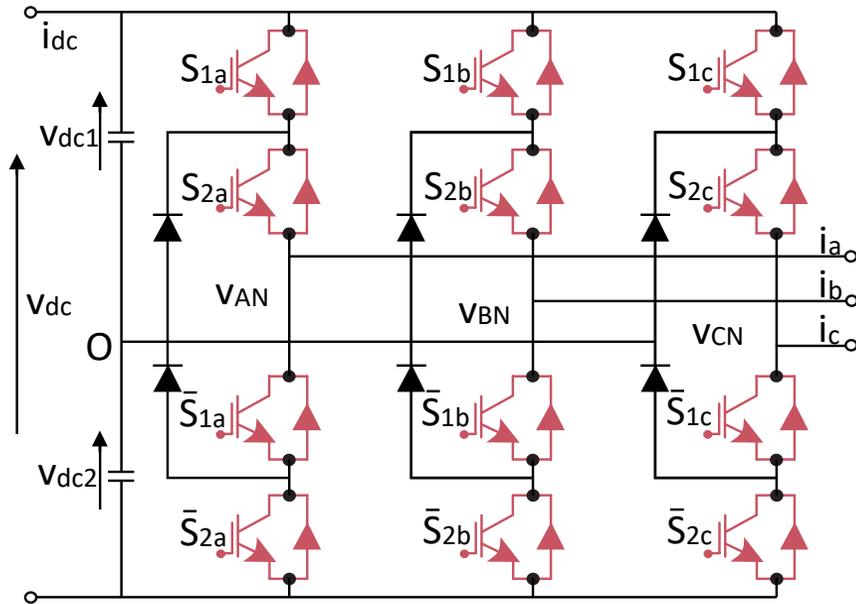


$$\mathbf{v} = L \frac{d\mathbf{i}}{dt} + R\mathbf{i}$$

| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $v_{dc1} + v_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $v_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |



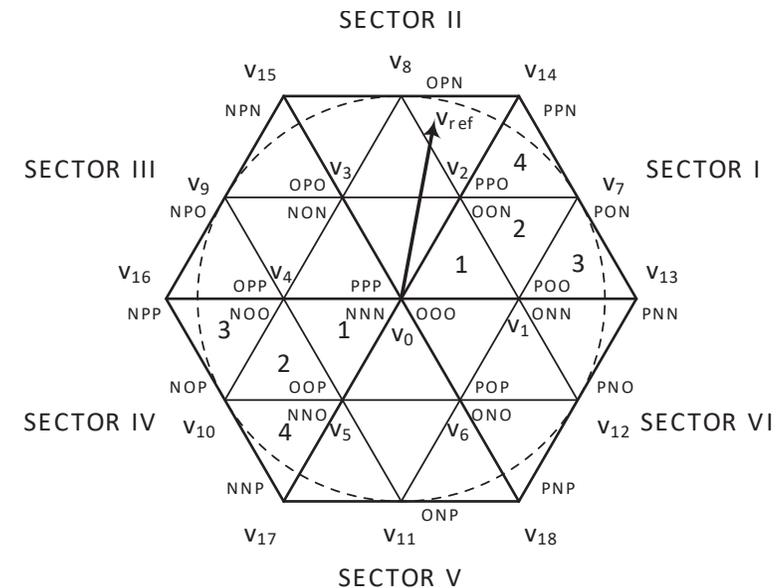
## - PCC of an NPC Inverter: Discrete Model



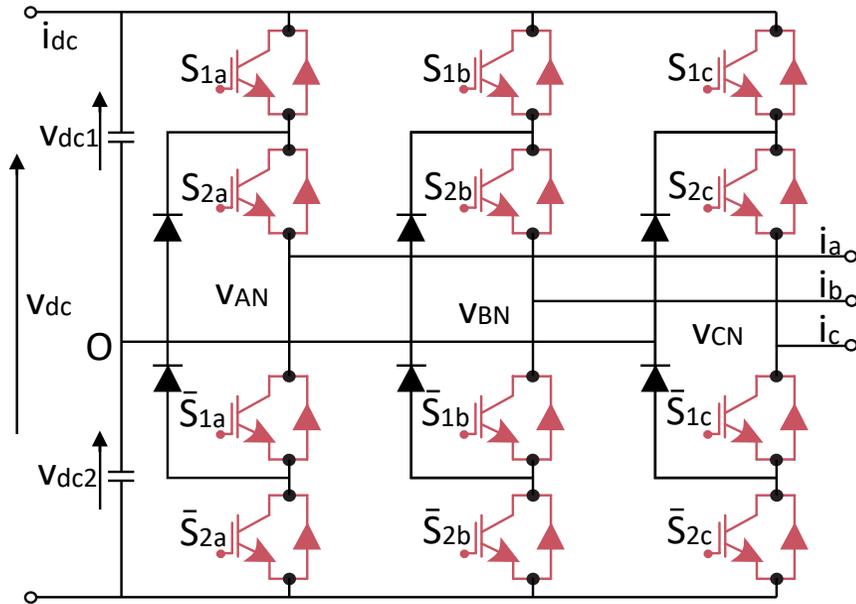
$$\mathbf{i}^{k+1} = \left(1 - \frac{RT_s}{L}\right) \mathbf{i}^k + \frac{T_s}{L} \mathbf{v}^k$$

$$v_{dcx}^{k+1} = v_{dcx}^k + \frac{T_s}{C_x} i_{cx}^{k+1}, \quad x = 1, 2$$

| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $v_{dc1} + v_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $v_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |

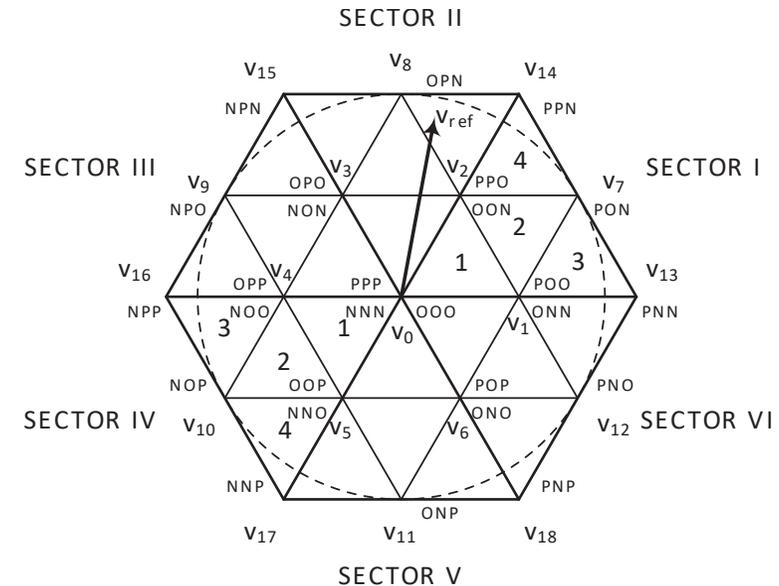


## - PCC of an NPC Inverter: Cost Function

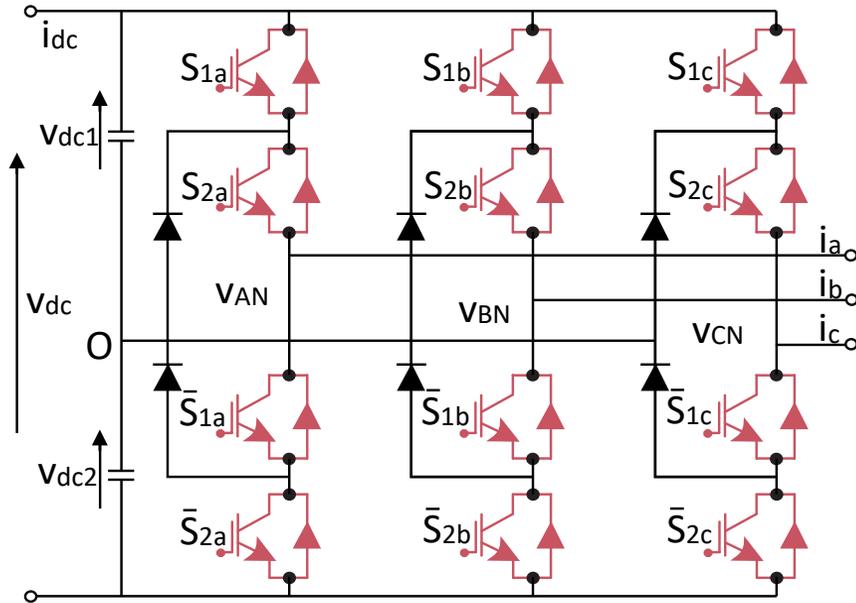


$$g^{k+1} = g_{track}^{k+1} + g_{bal}^{k+1}$$

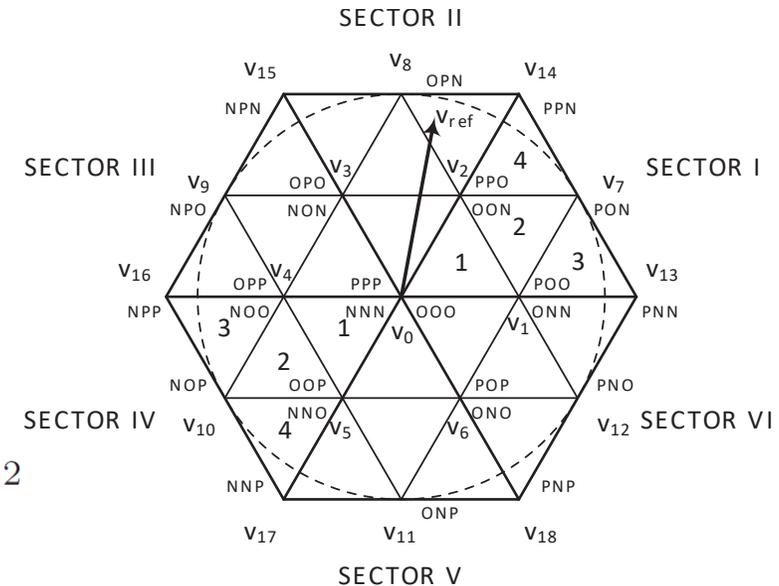
| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $v_{dc1} + v_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $v_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |



## - PCC of an NPC Inverter: Cost Function



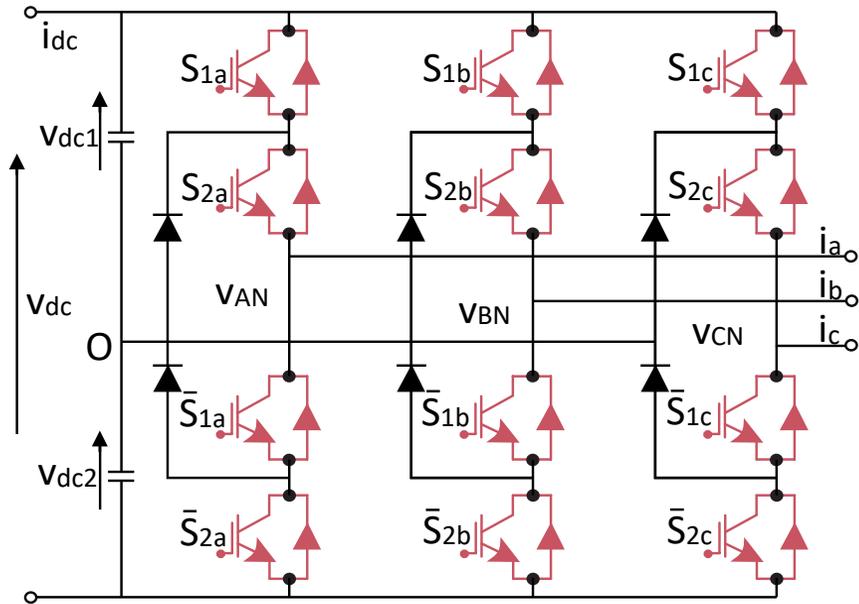
| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $V_{dc1} + V_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $V_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |



$$g^{k+1} = g_{track}^{k+1} + g_{bal}^{k+1}$$

$$g_{track}^{k+1} = [i_a^* - i_a^{k+1}]^2 + [i_b^* - i_b^{k+1}]^2 + [i_c^* - i_c^{k+1}]^2$$

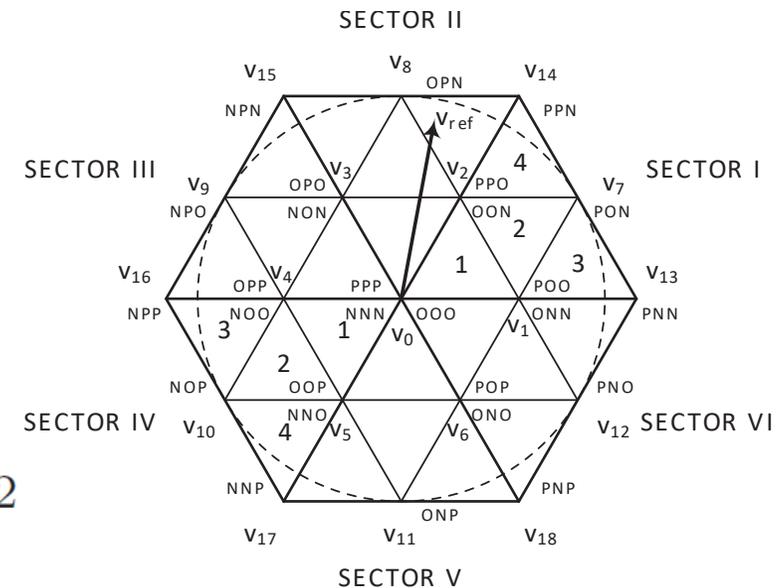
## - PCC of an NPC Inverter: Cost Function



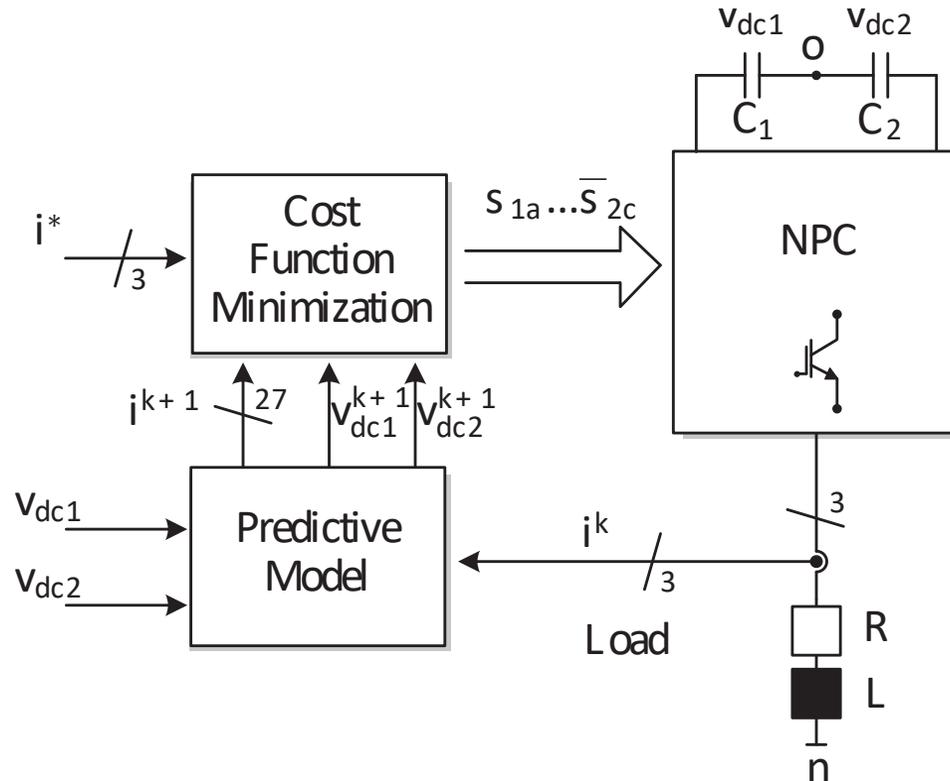
$$g^{k+1} = g_{track}^{k+1} + g_{bal}^{k+1}$$

$$g_{bal}^{k+1} = \lambda_{dc} * [v_{dc1}^{k+1} - v_{dc2}^{k+1}]^2$$

| $S_x$ | $S_{1x}$ | $S_{2x}$ | $\bar{S}_{1x}$ | $\bar{S}_{2x}$ | $v_{xn}$            |
|-------|----------|----------|----------------|----------------|---------------------|
| 1     | 1        | 1        | 0              | 0              | $v_{dc1} + v_{dc2}$ |
| 0     | 0        | 1        | 1              | 0              | $v_{dc2}$           |
| -1    | 0        | 0        | 1              | 1              | 0                   |



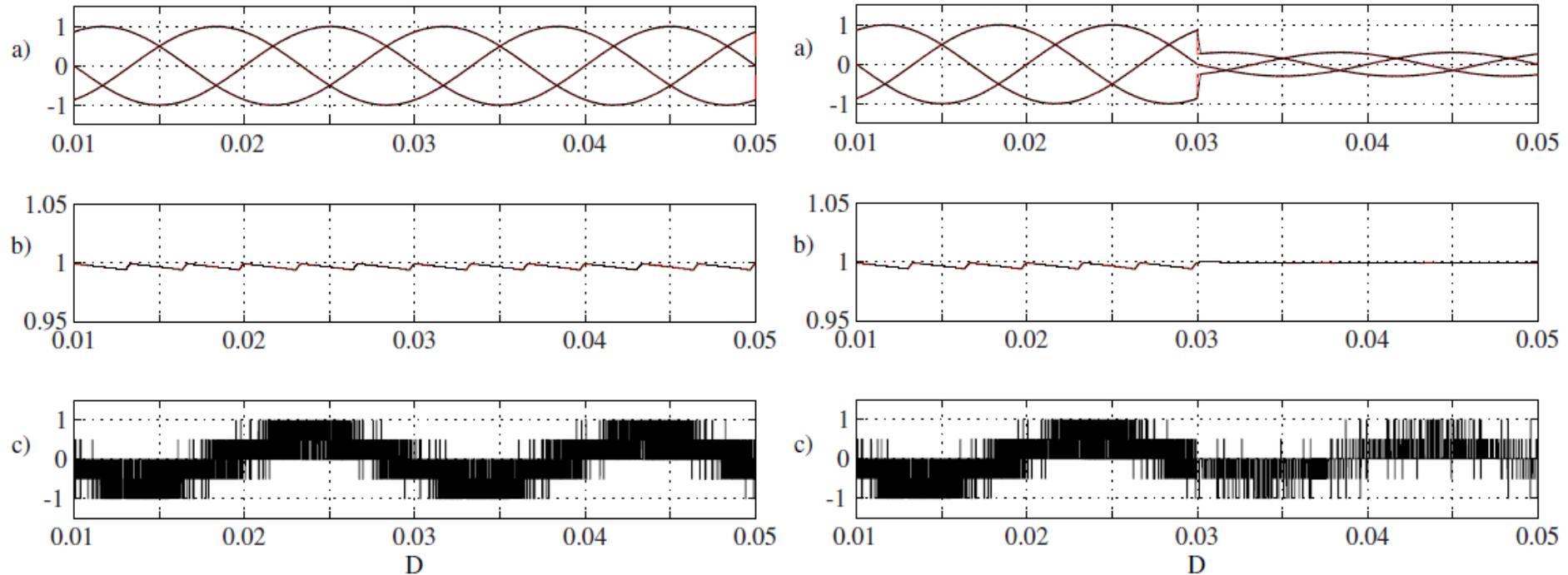
## - PCC of an NPC Inverter: Control Scheme



- The NPC inverter presents a **high number of switching states**, compared to the two levels inverter.
- The behavior of the system is predicted for each possible switching state of the NPC inverter.
- The switching state that minimizes a given cost function is **selected to be applied during the next sampling interval**.



## - PCC of an NPC Inverter: Simulated Results





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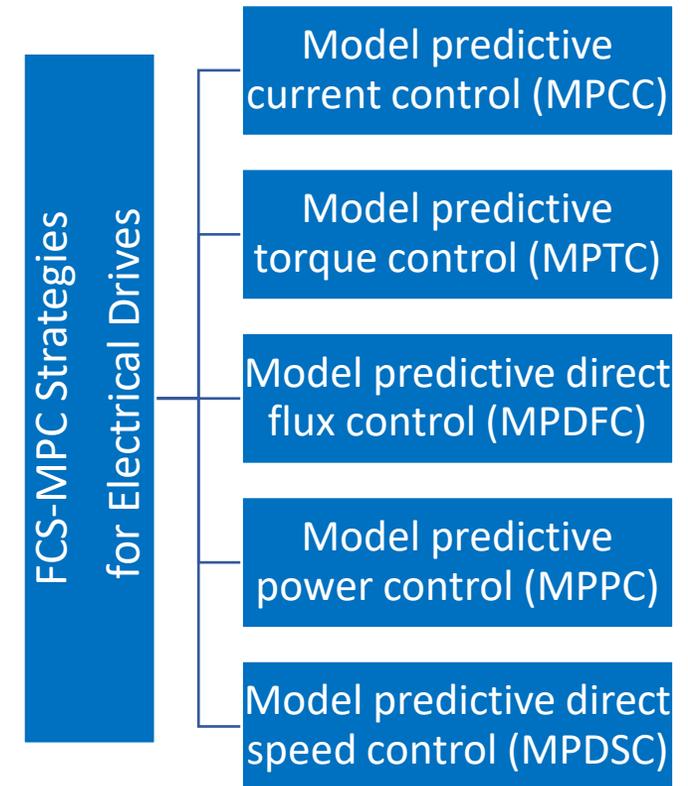
**Predictive Control for Power Converters and Electrical Drives**

# MPC applied to Electrical Drives



## - MPC Strategies for Electrical Drives

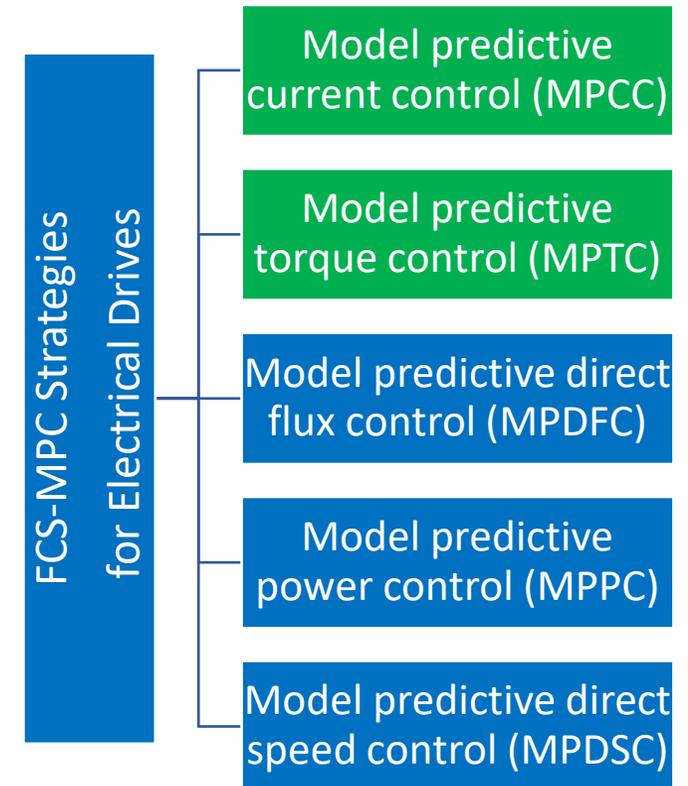
- Various FCS-MPC strategies have been proposed for high-performance control of electric machines.





## - MPC Strategies for Electrical Drives

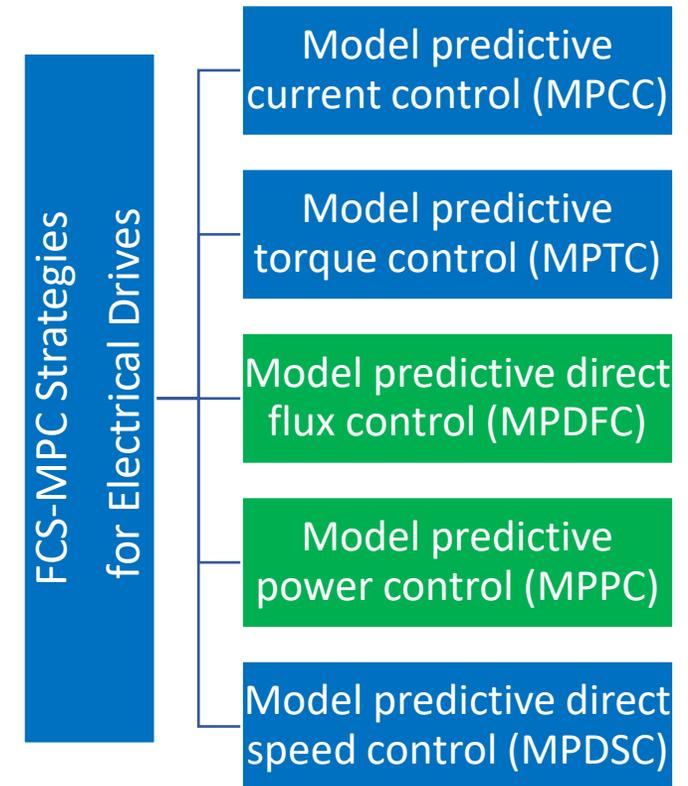
- Various FCS-MPC strategies have been proposed for high-performance control of electric machines.
- Of these, model predictive current control (MPCC) and model predictive torque control (MPTC) are quite popular.





## - MPC Strategies for Electrical Drives

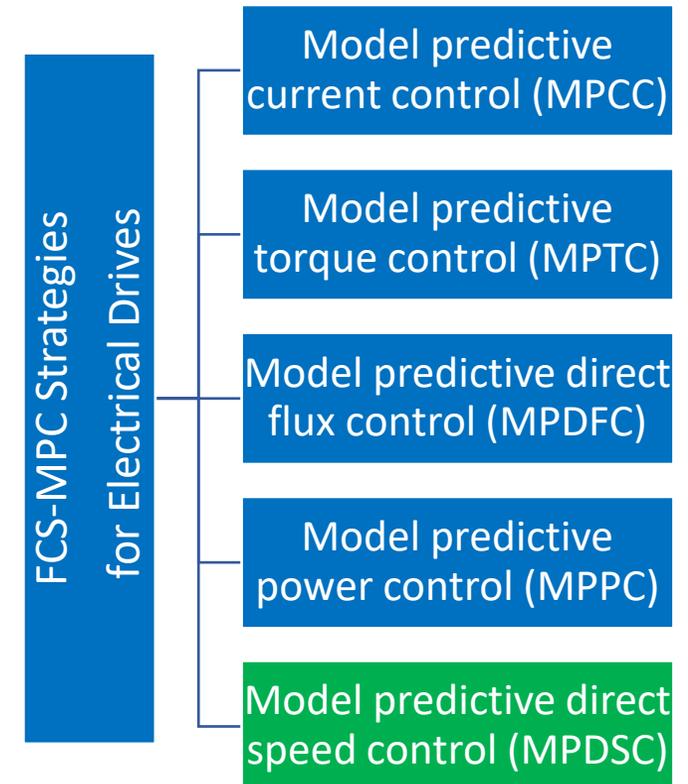
- Various FCS-MPC strategies have been proposed for high-performance control of electric machines.
- Of these, model predictive current control (MPCC) and model predictive torque control (MPTC) are quite popular.
- Model predictive direct flux control (MPDFC) and model predictive power control (MPPC) are strong candidates to MPTC as they eliminates the weighting factor in MPTC.





## - MPC Strategies for Electrical Drives

- Various FCS-MPC strategies have been proposed for high-performance control of electric machines.
- Of these, model predictive current control (MPCC) and model predictive torque control (MPTC) are quite popular.
- Model predictive direct flux control (MPDFC) and model predictive power control (MPPC) are strong candidates to MPTC as they eliminates the weighting factor in MPTC.
- Model predictive direct speed control (MPDSC) eliminates the cascaded control structure of previous FCS-MPC strategies to improve the control performance. However, it requires load information, which is costly to measure.



## - Application of FCS-MPC Strategies for PMSM Control

### PMSM model:

$$\dot{\mathbf{x}}_t = \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) + \mathbf{w}_t$$

$$\mathbf{z}_t = \mathbf{h}(\mathbf{x}_t) + \mathbf{v}_t$$

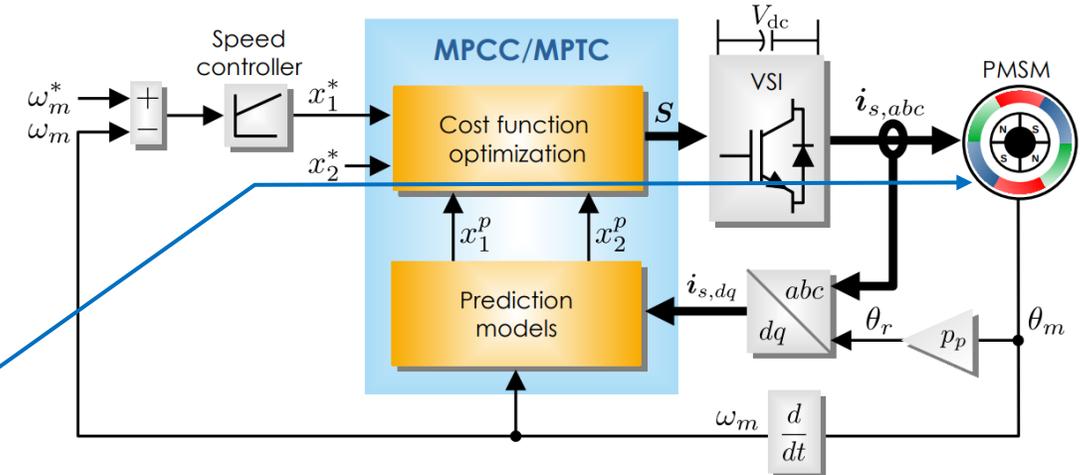
where

$$\mathbf{x}_t = \begin{bmatrix} i_d \\ i_q \\ \omega_m \end{bmatrix}, \mathbf{u}_t = \begin{bmatrix} v_d \\ v_q \end{bmatrix}, \mathbf{h}(\mathbf{x}_t) = \begin{bmatrix} i_d \\ i_q \\ \omega_m \end{bmatrix},$$

$$\mathbf{f}(\mathbf{x}_t, \mathbf{u}_t) = \begin{bmatrix} \frac{1}{L_s} v_d - \frac{R_s}{L_s} i_d + p_p \omega_m i_q \\ \frac{1}{L_s} v_q - \frac{R_s}{L_s} i_q - p_p \omega_m i_d - \frac{p_p}{L_s} \omega_m \psi_{pm} \\ \frac{3}{2} \frac{p_p}{J_t} \psi_{pm} i_q - \frac{B_t}{J_t} \omega_m - \frac{\tau_l}{J_t} \end{bmatrix}$$

After applying forward Euler discretization, the discrete PMSM model can be obtained as follows:

$$\mathbf{x}_{k+1} = \mathbf{x}_k + T_s \cdot \mathbf{f}(\mathbf{x}_t, \mathbf{u}_t)$$



Block diagram of MPCC and MPTC strategies for PMSM control ( $x_1 = i_q, x_2 = i_d$  for MPCC;  $x_1 = \tau_e, x_2 = \|\psi_s\|$  for MPTC).

## - Application of MPCC Strategy for PMSM Control

### MPCC strategy

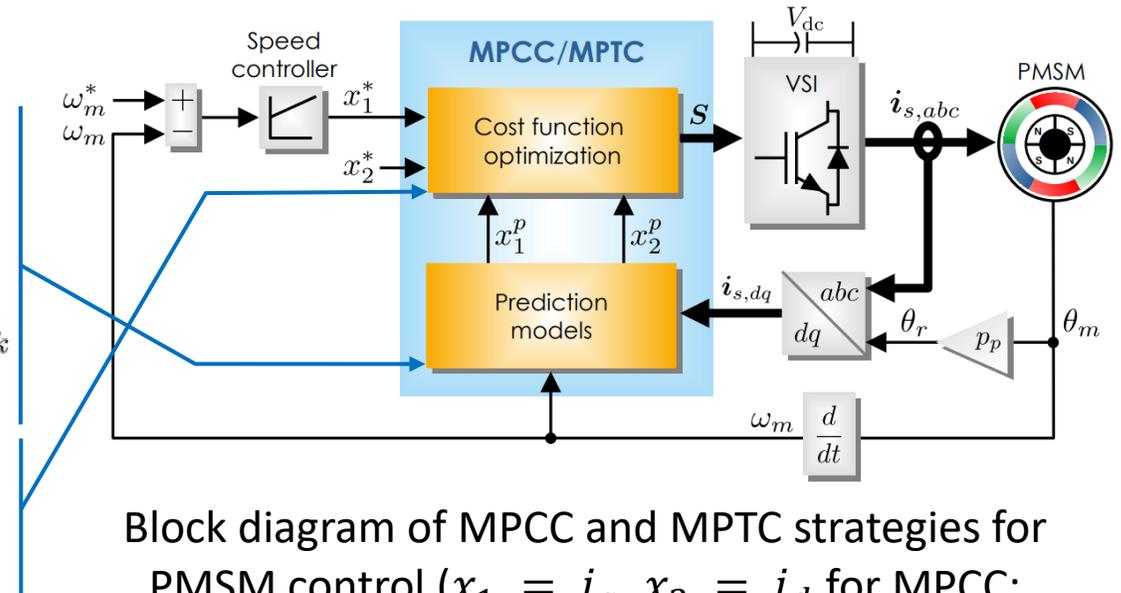
- Stator current predictions:

$$i_{d,k+1}^p = \left(1 - \frac{R_s T_s}{L_s}\right) i_{d,k} + p_p T_s \omega_{m,k} i_{q,k} + \frac{T_s}{L_s} v_{q,k}$$

$$i_{q,k+1}^p = \left(1 - \frac{R_s T_s}{L_s}\right) i_{q,k} - p_p T_s \omega_{m,k} i_{d,k} - \frac{T_s p_p}{L_s} \omega_{m,k} \psi_{pm} + \frac{T_s}{L_s} v_{q,k}$$

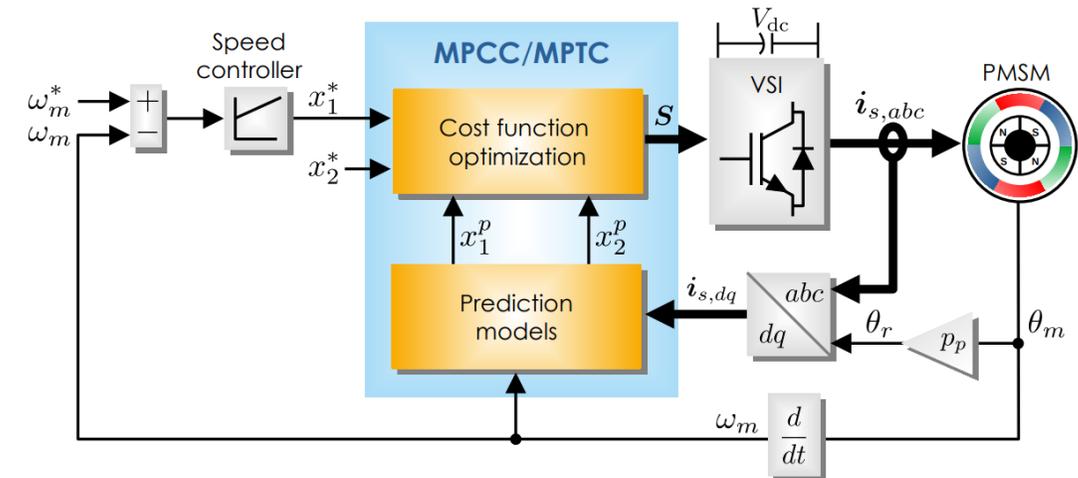
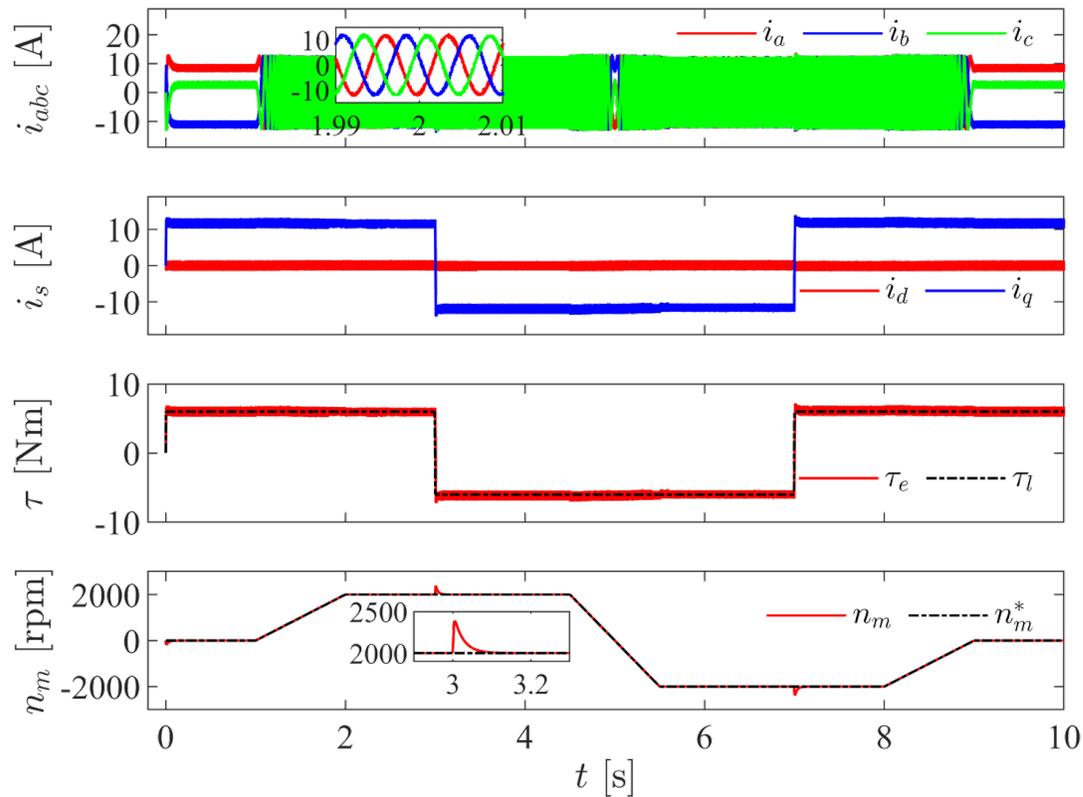
- Cost function:

$$g = |i_d^* - i_{d,k+1}^p| + |i_q^* - i_{q,k+1}^p|$$



Block diagram of MPCC and MPTC strategies for PMSM control ( $x_1 = i_q, x_2 = i_d$  for MPCC;  $x_1 = \tau_e, x_2 = \|\psi_s\|$  for MPTC).

## - Application of MPCC Strategy for PMSM Control - Results



Block diagram of MPCC and MPTC strategies for PMSM control ( $x_1 = i_q, x_2 = i_d$  for MPCC;  $x_1 = \tau_e, x_2 = \|\psi_s\|$  for MPTC).

Results: control performance under four-quadrant operation

## - Application of MPTC Strategy for PMSM Control

### MPTC strategy

#### Stator current predictions:

$$i_{d,k+1}^p = \left(1 - \frac{R_s T_s}{L_s}\right) i_{d,k} + p_p T_s \omega_{m,k} i_{q,k} + \frac{T_s}{L_s} v_{q,k}$$

$$i_{q,k+1}^p = \left(1 - \frac{R_s T_s}{L_s}\right) i_{q,k} - p_p T_s \omega_{m,k} i_{d,k} - \frac{T_s p_p}{L_s} \omega_{m,k} \psi_{pm} + \frac{T_s}{L_s} v_{q,k}$$

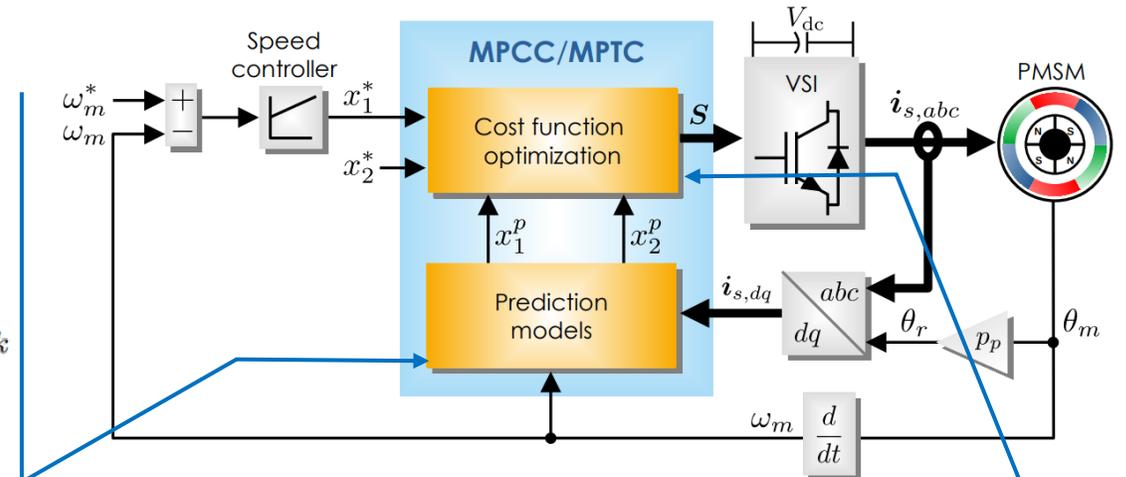
#### Flux prediction:

$$\psi_{d,k+1}^p = L_d i_{d,k+1}^p + \psi_{pm}$$

$$\psi_{q,k+1}^p = L_q i_{q,k+1}^p$$

#### Torque prediction:

$$\tau_{e,k+1}^p = 1.5 p_p (\psi_{d,k+1}^p i_{q,k+1}^p - \psi_{q,k+1}^p i_{d,k+1}^p)$$

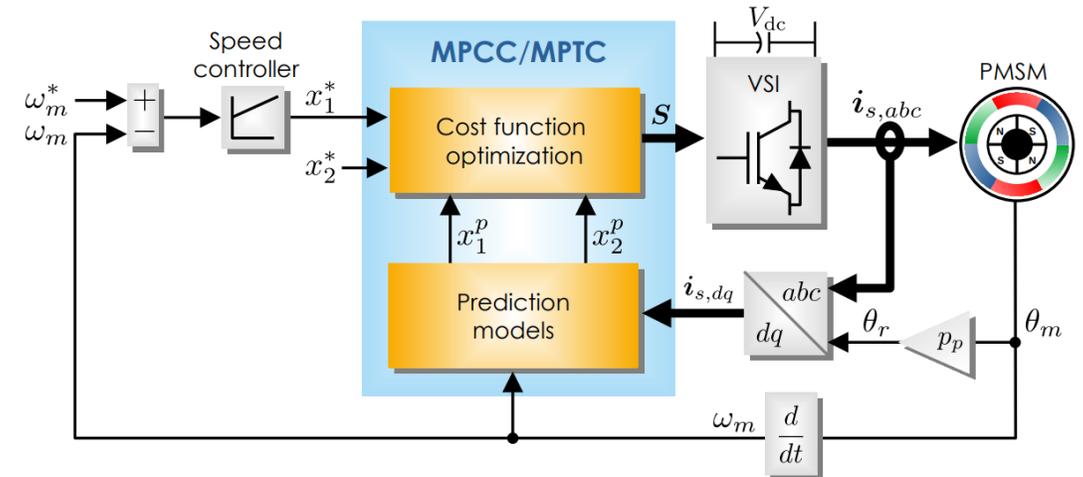
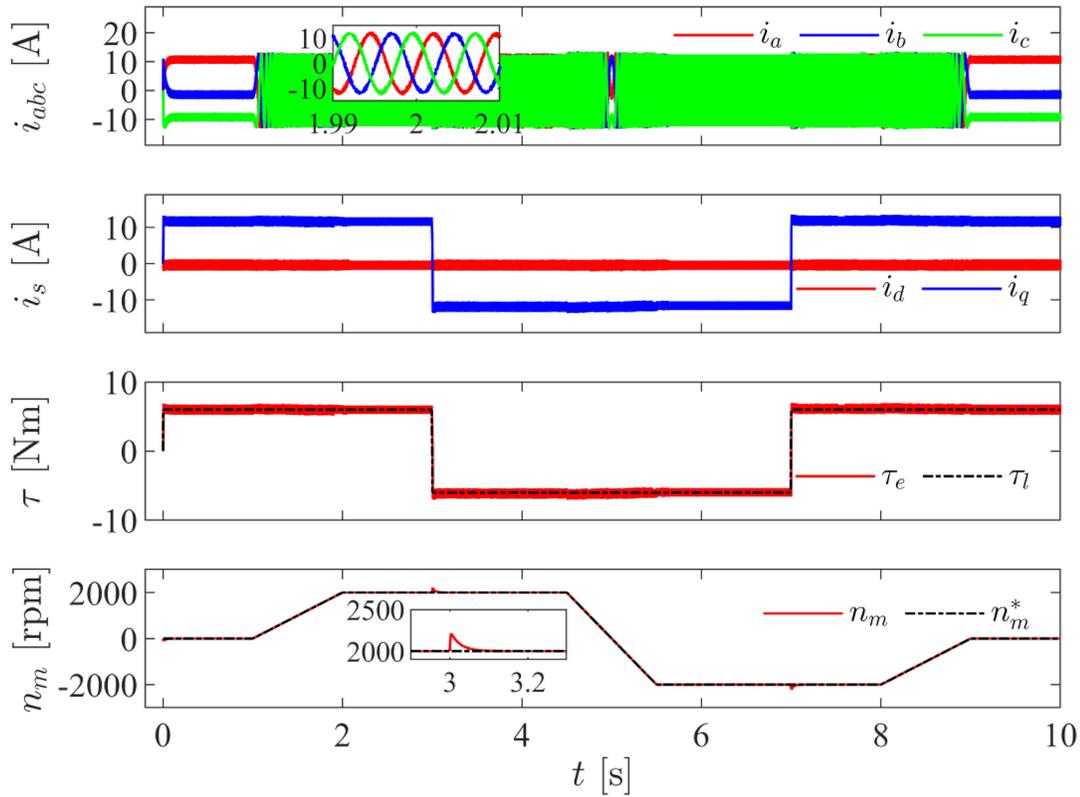


Block diagram of MPCC and MPTC strategies for PMSM control ( $x_1 = i_q$ ,  $x_2 = i_d$  for MPCC;  $x_1 = \tau_e$ ,  $x_2 = \|\psi_s\|$  for MPTC).

#### Cost function:

$$g = |\tau_e^* - \tau_{e,k+1}^p| + \lambda_\psi \left| |\psi_s^*| - |\psi_{s,k+1}^p| \right|$$

## - Application of MPTC Strategy for PMSM Control - Results

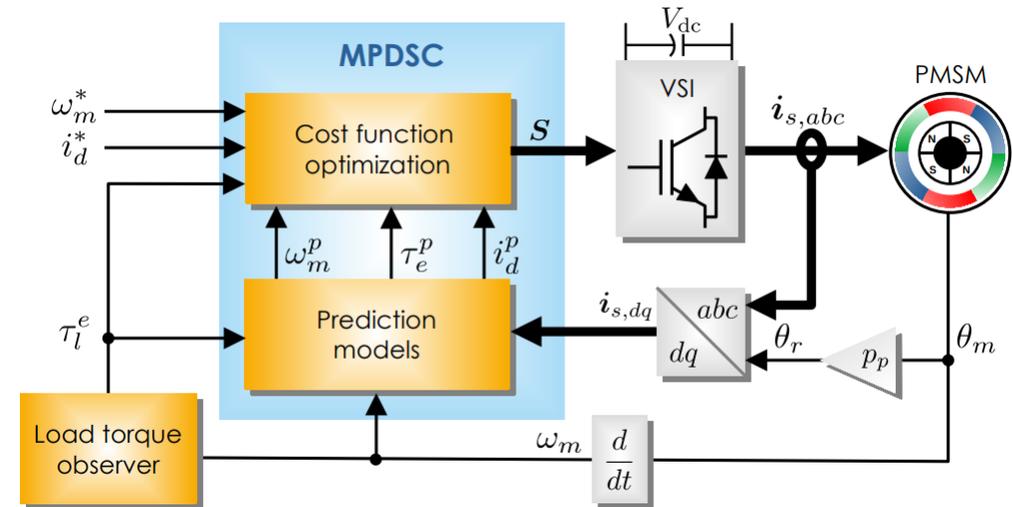


Block diagram of MPCC and MPTC strategies for PMSM control ( $x_1 = i_q, x_2 = i_d$  for MPCC;  $x_1 = \tau_e, x_2 = \|\psi_s\|$  for MPTC).

Results: control performance under four-quadrant operation



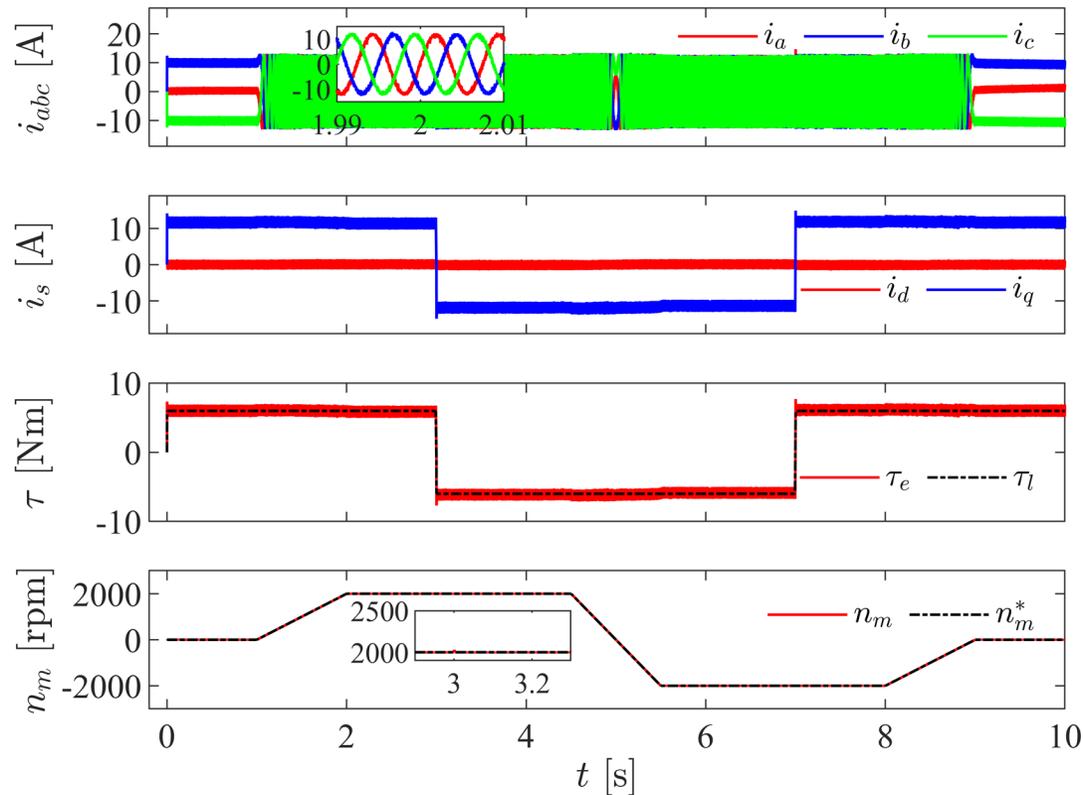
## - Application of MPDSC Strategy for PMSM Control



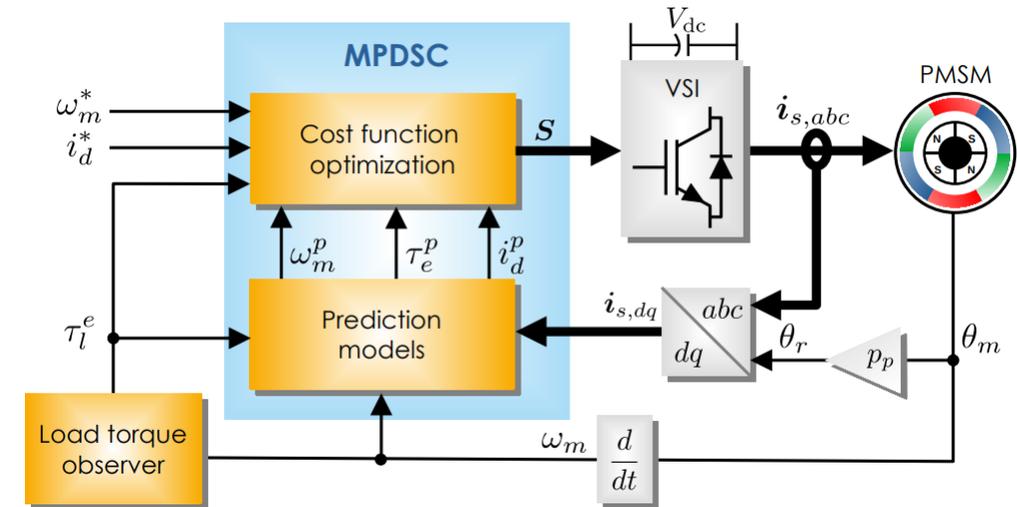
Block diagram of MPDSC strategy.



## - Application of MPDSC Strategy for PMSM Control - Results



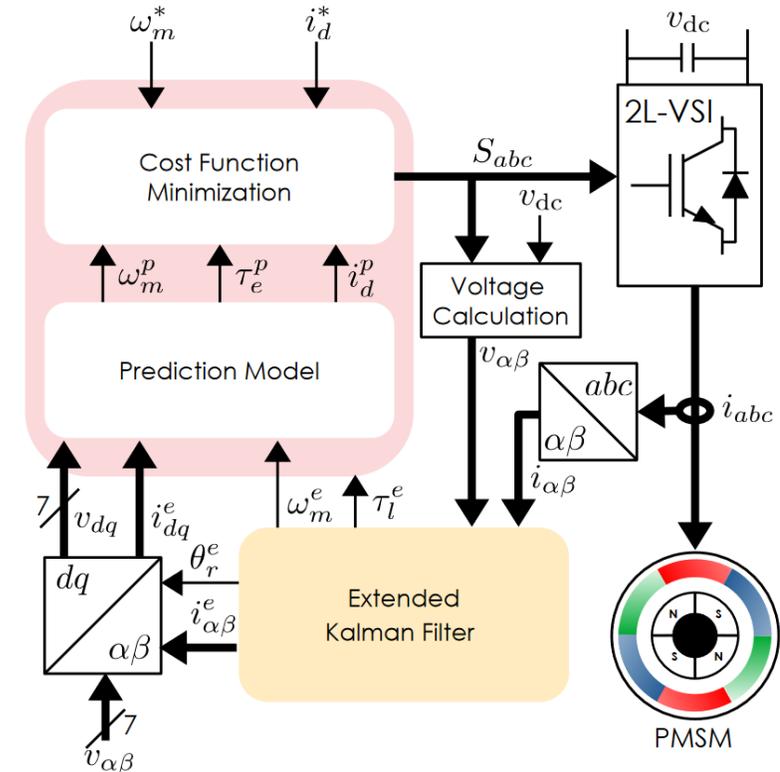
Results: control performance under four-quadrant operation



Block diagram of MPDSC strategy.

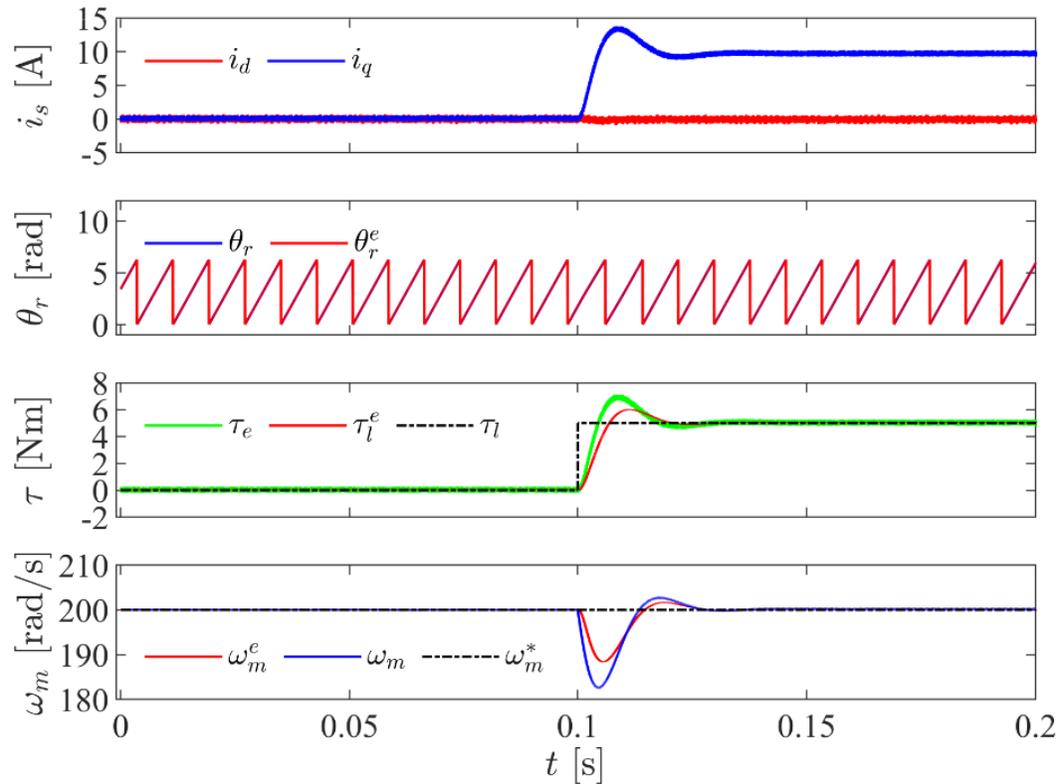
## - Sensorless MPDSC Strategy for PMSM Control

- Measuring load torque is a costly solution; therefore, it is a well-accepted approach to estimate it using an estimator/observer.
- Speed is often measured by an encoder mounted to the shaft but depending on the application, it may not be possible to mount a speed sensor. Also, it is not a cost-effective way.
- In such cases, combining sensorless control and MPC strategies is a viable option.
- For this purpose, an observer, e.g., an EKF can be designed to estimate position, speed, and load torque, as shown in the figure. Because EKF makes it possible to estimate all these states using a single observer.

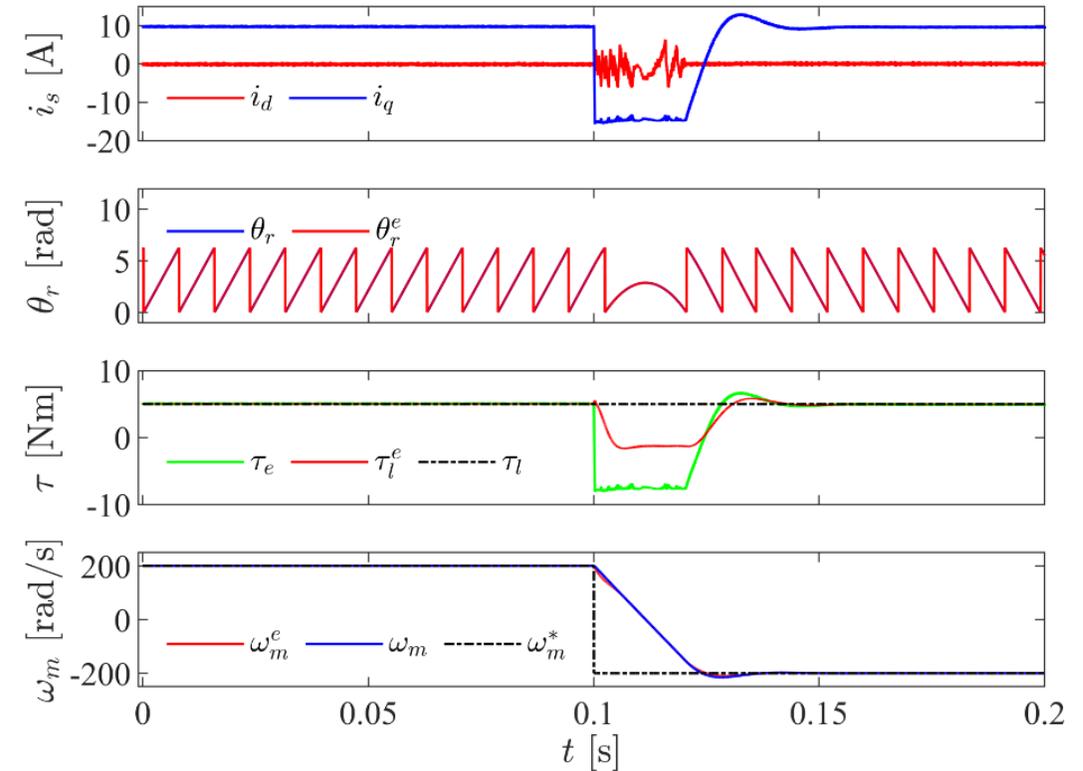


Block diagram of the sensorless PDSC of PMSM.

## - Sensorless MPDSC Strategy for PMSM Control

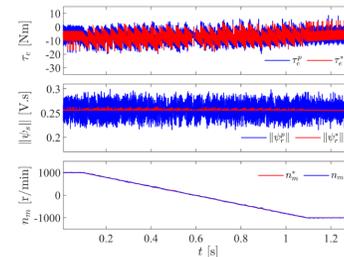
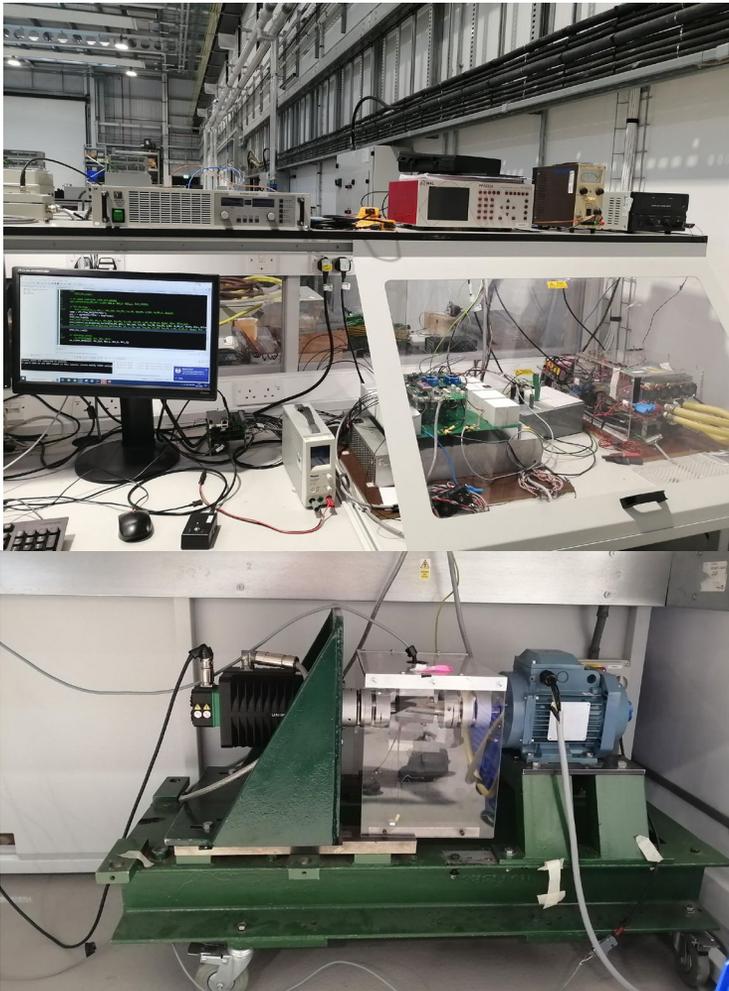


Performance of sensorless MPDSC-based PMSM drive under load changes at 200 rad/s.

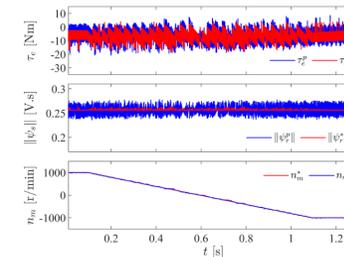


Performance of sensorless MPDSC-based PMSM drive under speed reversals with a load of 5 Nm.

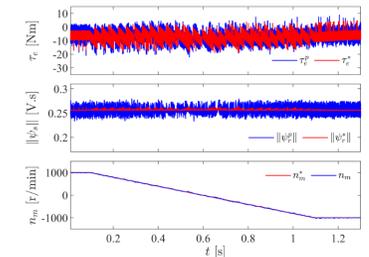
# Experimental Implementation of MPC Strategies for the PMSM



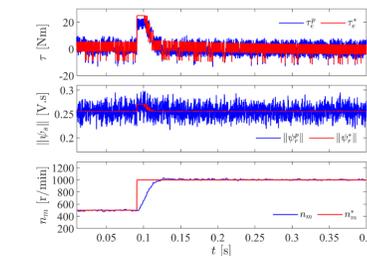
(a)



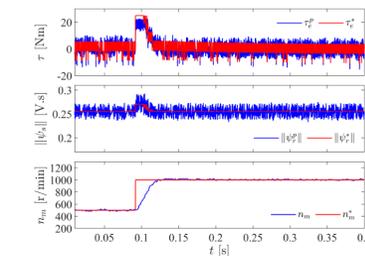
(b)



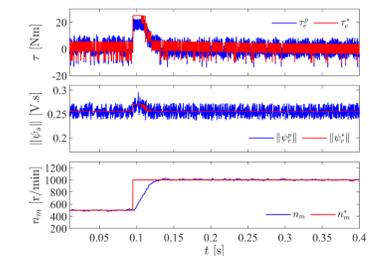
(c)



(a)



(b)



(c)

Experimental results: (a) conventional MPTC; (b) DM-based MPTC using Euclidean norm; (c) Proposed DM-based MPTC



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## Predictive Control for Power Converters and Electrical Drives

# Technical Issues for the Implementation of Predictive Control



## - Examples of Cost Function for Power Electronics Applications

Several ways to represent the same control objective.

$$g = |x^* - x^p|$$

$$g = (x^* - x^p)^2$$

$$g = \left| \int_k^{k+1} (x^*(t) - x^p(t)) dt \right|$$

Reference Tracking

| Application      | Cost function  |
|------------------|--|
| CSC-AFE          | $g =  q  + \lambda  \hat{i}_L - i_L^* $ $g = (q)^2 + \lambda (\hat{i}_L - i_L^*)^2$  |
| VSC-AFE          | $g =  \hat{i}_k - i_k^* $ $g =  \hat{i}_k - i_k^*  + \lambda_n n_c$ $g = (\hat{i}_k - i_k^*)^2$  |
| Motor drive      | $g = (\hat{P} - P^*)^2 + (\hat{Q} - Q^*)^2$  |
| VSC-UPS          | $g = (\hat{T} - T^*)^2 + \lambda (\hat{\psi} - \psi^*)^2$  |
| Statcom          | $g = (\hat{v}_o - v_o^*)^2$  |
| Matrix converter | $g = (\hat{i}_k - i_k^*)^2$ $g =  \hat{i}_L - i_L^*  + \lambda  \hat{Q} - Q^* $ $g = (\hat{i}_L - i_L^*)^2 + \lambda (\hat{Q} - Q^*)^2$                      |
| HVDC             | $g = g_1 + g_2 + g_3$ $g_1 =  \hat{i}_{jk} - i_{jk}^* $ $g_2 = \lambda_{Ck} \sum_i  \hat{V}_{cijk} - \frac{V_{dc}}{n} $ $g_3 = \lambda_{zk}  \hat{i}_{zjk} $ |

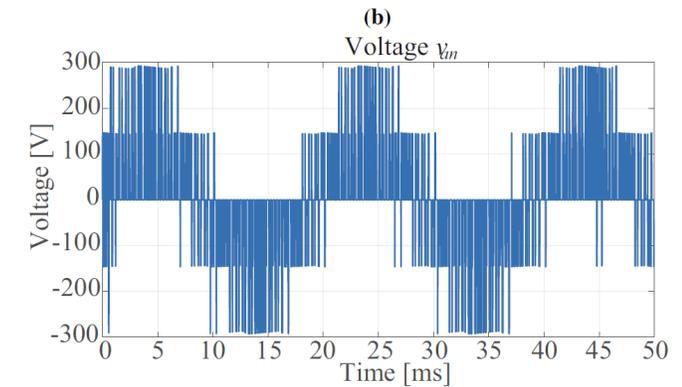
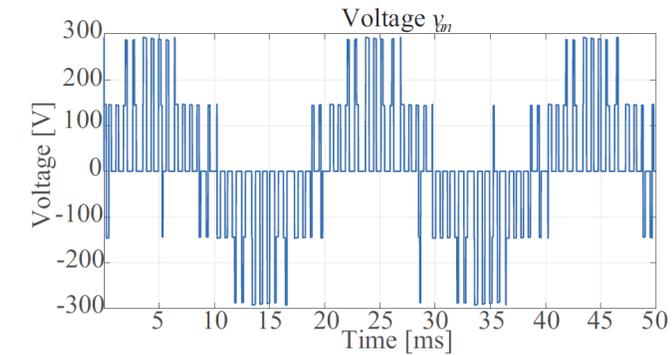
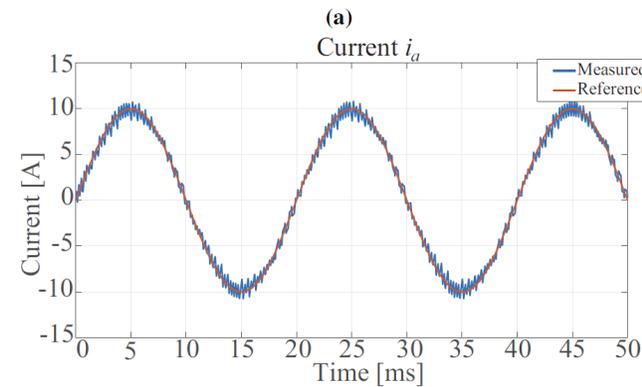
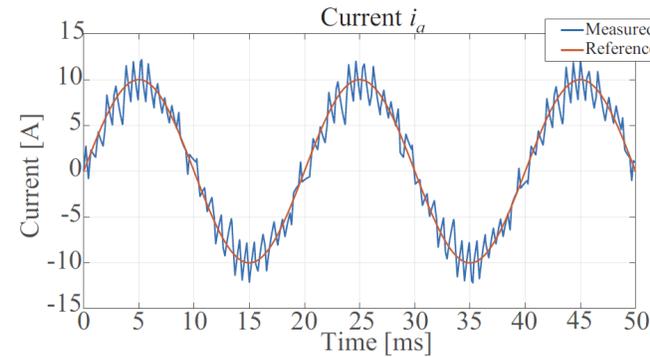
## - Selection of Cost Functions: Switching Frequency Minimization

$$g = (i_{\alpha}^* - i_{\alpha}^p)^2 + (i_{\beta}^* - i_{\beta}^p)^2 + \lambda_n n$$

$$n = |S_a(k) - S_a(k-1)| + |S_b(k) - S_b(k-1)| + |S_c(k) - S_c(k-1)|$$

**Table III:** Total harmonic distortion for each  $\lambda_n$  and the average of switches commutations.

| $\lambda_n$ | THD of $i_a$ | N° commutations (average) |
|-------------|--------------|---------------------------|
| 1.8         | 24.20 %      | 5                         |
| 1.2         | 17.38 %      | 6                         |
| 0.4         | 6.69 %       | 18                        |
| 0.09        | 2.08 %       | 57                        |

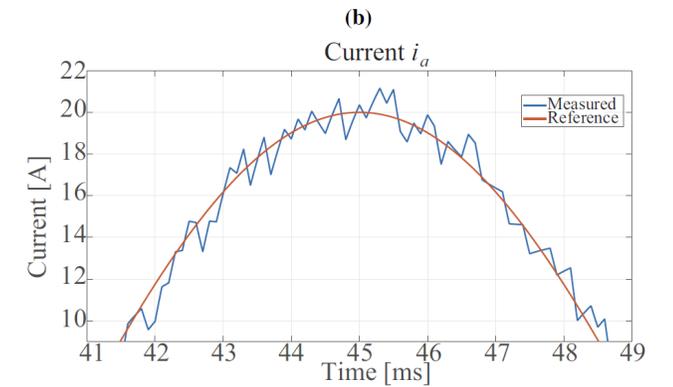
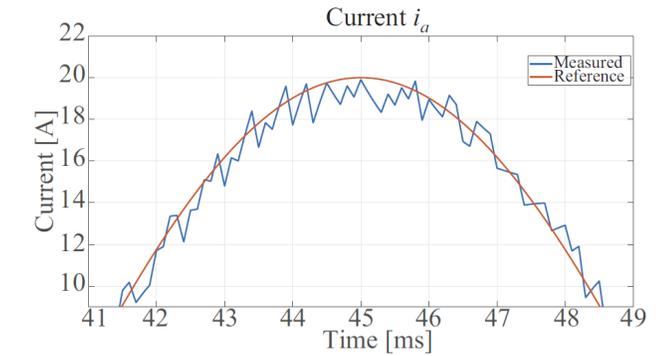
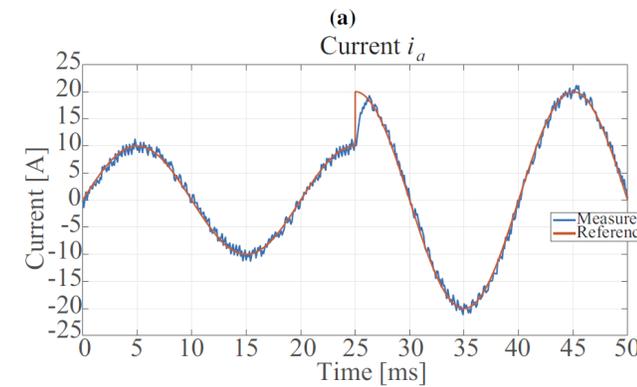
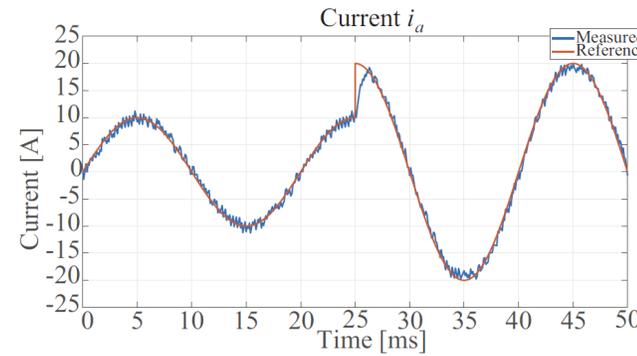


**Figure 3:** Current  $i_a$  and voltage  $v_{an}$  for different values of  $\lambda_n$ .  $\lambda_n = 1.2$  (a) y (b),  $\lambda_n = 0.4$  (c) y (d).

## - Selection of Cost Functions: Strict Restrictions

$$g = (i_{\alpha}^* - i_{\alpha}^p)^2 + (i_{\beta}^* - i_{\beta}^p)^2 + f_{lim}(i^p)$$

$$f_{lim}(i_{\alpha\beta}^p) = \begin{cases} \infty & \text{si } -i_{max} > i_{\alpha}^p \text{ (o } i_{\beta}^p) > i_{max} \\ 0 & \text{in other case} \end{cases} \quad (1)$$



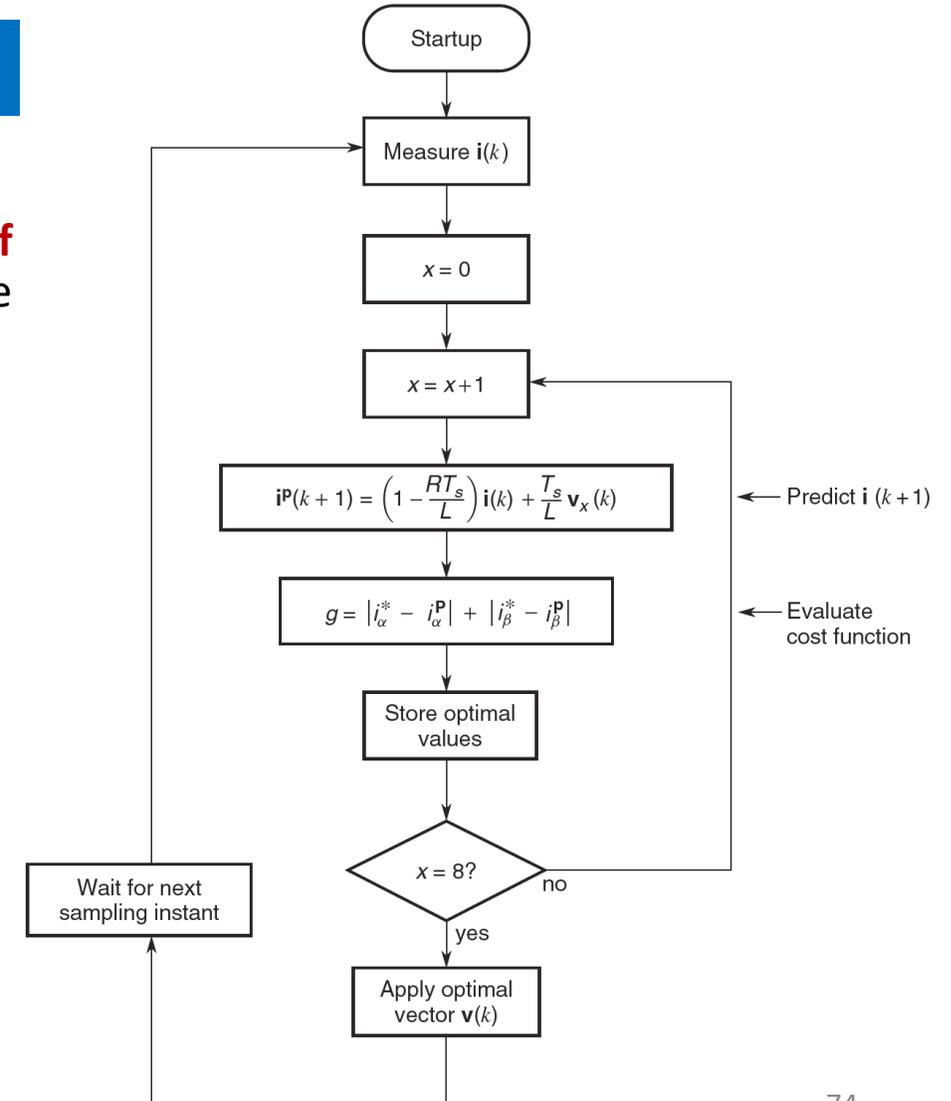
**Figure 4:** (a) Current  $i_a$  with limitation, (b) zoom of the current  $i_a$  with limitation, (c) current  $i_a$  without limitation and (d) zoom of the current  $i_a$  without limitation.

## - Delay Compensation

- Experimental implementation of MPC requires a **large number of calculations**, which generates an important time delay in the actuation.
- The **delay can deteriorate the performance** of the system.
- To avoid this issue, a **delay compensation technique is required**.

$$g = |i_{\alpha}^*(k+1) - i_{\alpha}^p(k+1)| + |i_{\beta}^*(k+1) - i_{\beta}^p(k+1)|$$

$$\mathbf{i}^p(k+1) = \left(1 - \frac{RT_s}{L}\right) \mathbf{i}(k) + \frac{T_s}{L} \mathbf{v}(k)$$



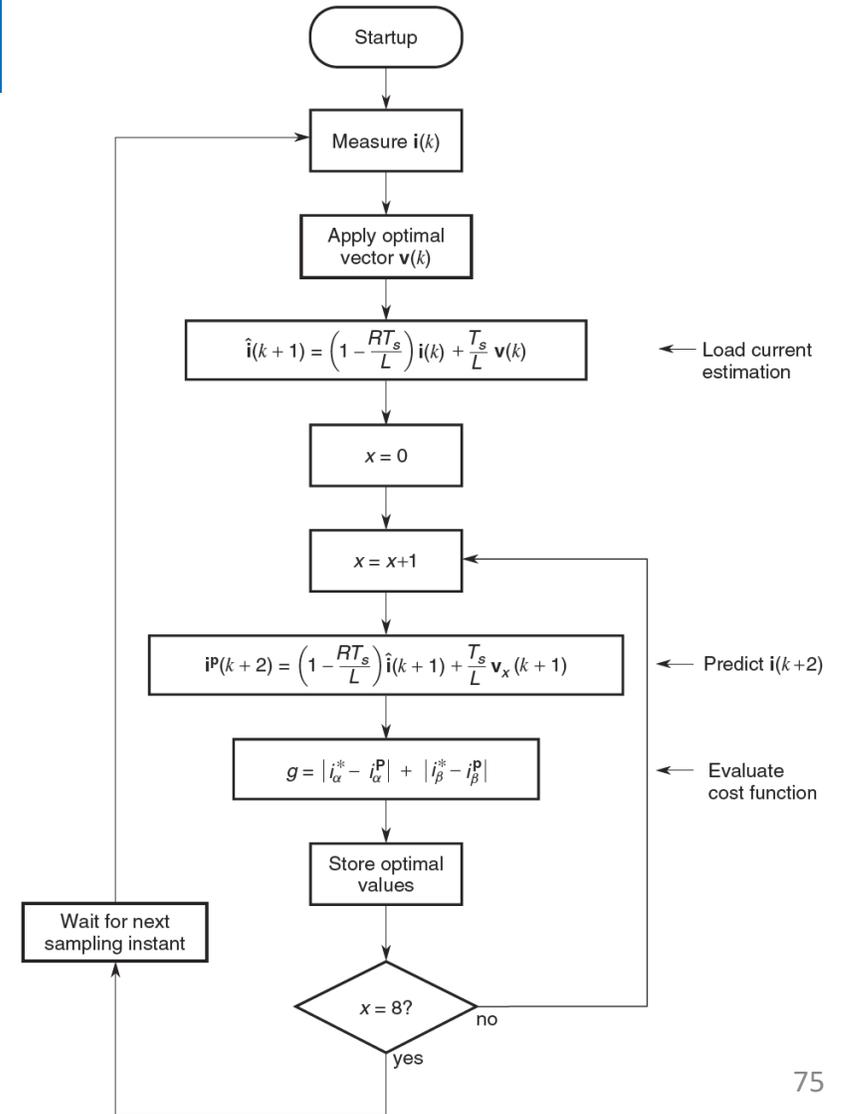


## - Delay Compensation

- Application of the new **optimal voltage vector** is moving to the **beginning**.
- The **estimation of the currents** at time  $t_{k+1}$  is added.
- The estimated currents are **used for the predictions** for all the available switching states.

$$g = |i_{\alpha}^*(k+2) - i_{\alpha}^P(k+2)| + |i_{\beta}^*(k+2) - i_{\beta}^P(k+2)|$$

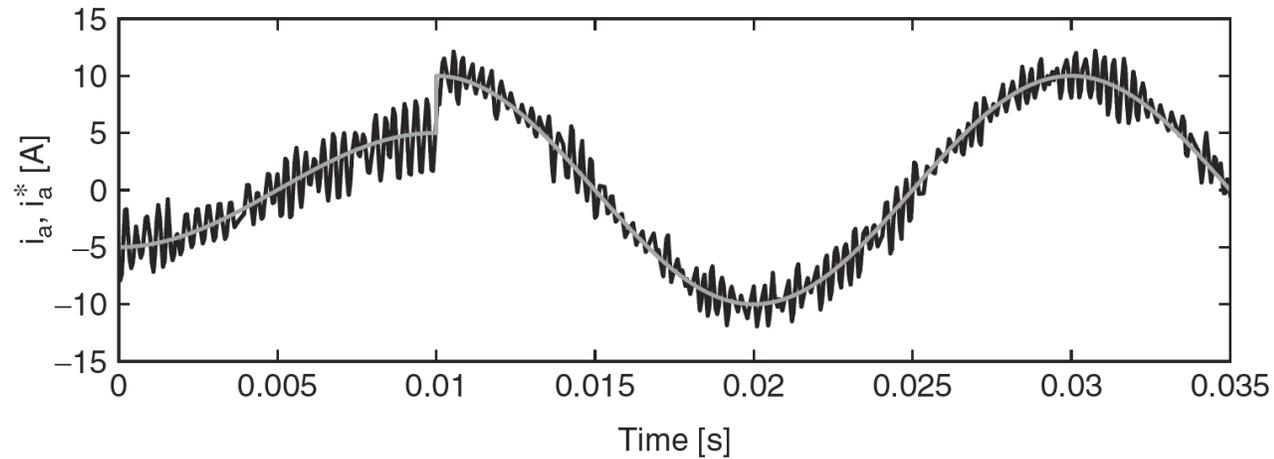
$$i^P(k+2) = \left(1 - \frac{RT_s}{L}\right) \hat{i}(k+1) + \frac{T_s}{L} \mathbf{v}(k+1)$$



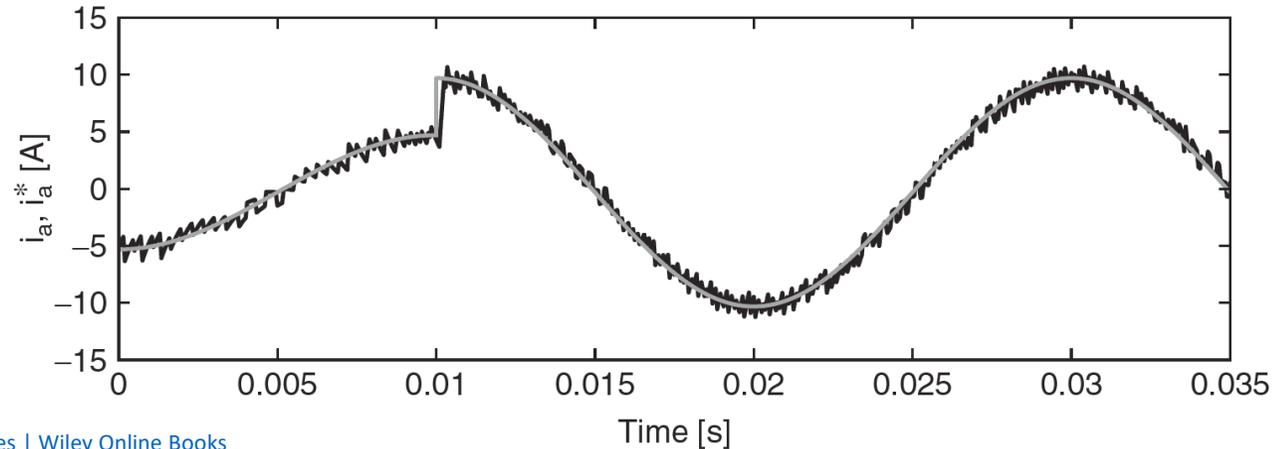


## - Delay Compensation

Without delay compensation



With delay compensation





## - Selection of Weighting Factors

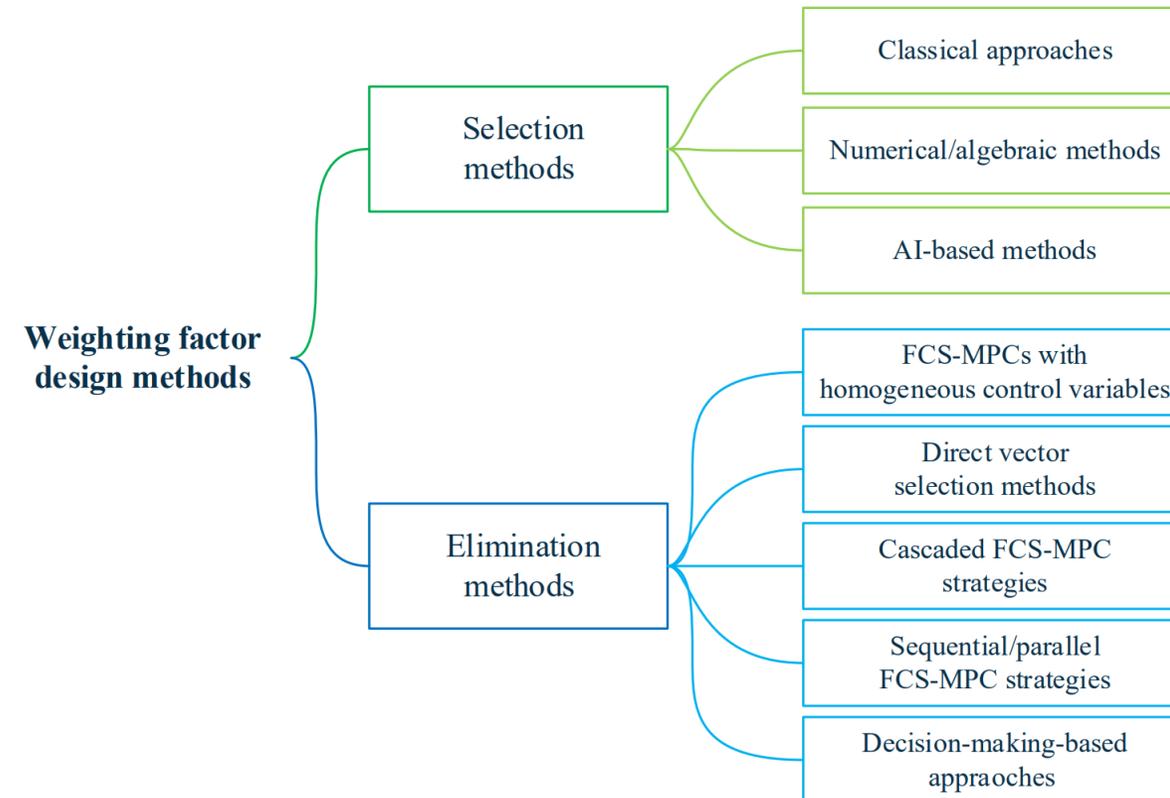
$$g = \lambda_x \|x^* - x^P\| + \lambda_y \|y^* - y^P\| + \dots + \lambda_z \|Z^* - z^P\|$$

- Weighting factors are required when several control objectives are considered.
- To reduce the error, these values must be carefully adjusted.
- There are no theoretical, analytical, or numerical methods to adapt these factors.
- They are determined by empirical procedures.



## - Weighting Factor Design Methods

- Weighting factor design methods can be divided into two main groups: **weighting factor selection methods** and **weighting factor elimination methods**.
- 1<sup>st</sup> group of studies consists of classic approaches, numerical/algebraic methods, meta-heuristic optimization methods, and artificial intelligence (AI)-based methods.
- 2<sup>nd</sup> group of studies includes MPCs with homogeneous control variables, direct vector selection methods, sequential/parallel MPC strategies, and decision-making (DM)-based approaches.



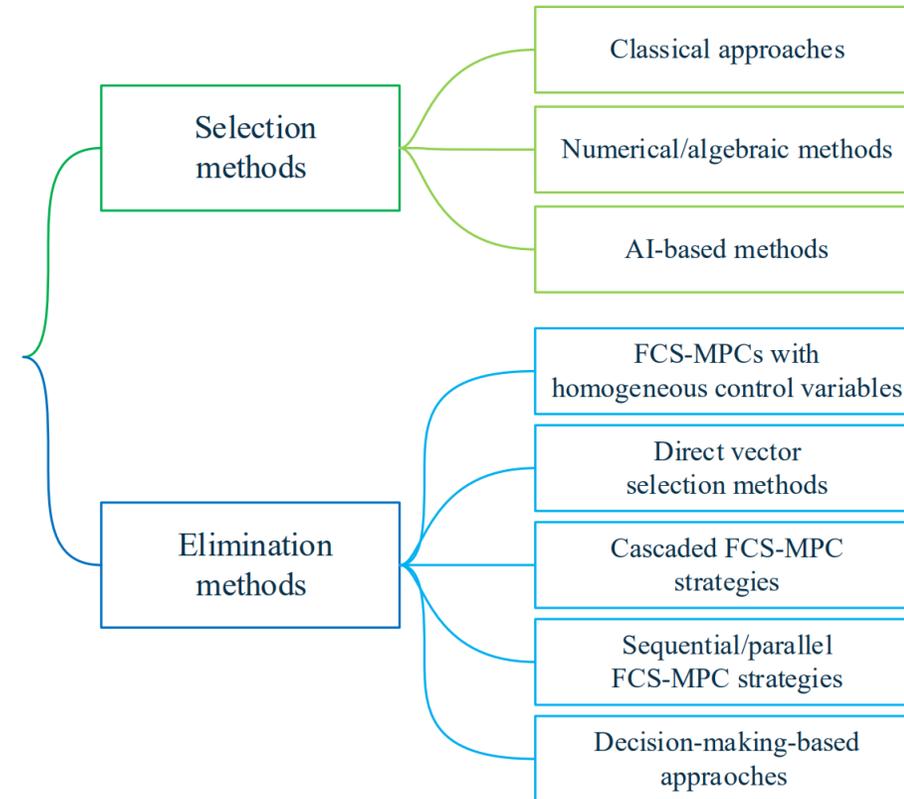
## - Comparison of Weighting Factor Design Methods

- Weighting factor design methods can be divided into two main groups: weighting factor selection methods and weighting factor elimination methods.

OVERVIEW OF WF DESIGN METHODS

|                                     | Control performance | Flexibility | Design complexity | Computational complexity |
|-------------------------------------|---------------------|-------------|-------------------|--------------------------|
| Classic approaches                  | XX                  | ✓✓          | XX                | ✓✓                       |
| Numerical/algebraic methods         | X                   | X           | X                 | ✓                        |
| Meta-heuristic optimization methods | X                   | ✓✓          | XX                | ✓✓                       |
| AI-based methods                    | ✓✓                  | X           | XX                | X                        |
| MPCs with unifying cost functions   | ✓                   | XX          | ✓✓                | ✓                        |
| Direct vector selection methods     | ✓                   | XX          | ✓✓                | ✓✓                       |
| Sequential/parallel MPC strategies  | ✓✓                  | ✓           | X                 | X                        |
| Decision-making-based methods       | ✓✓                  | ✓           | ✓                 | X                        |

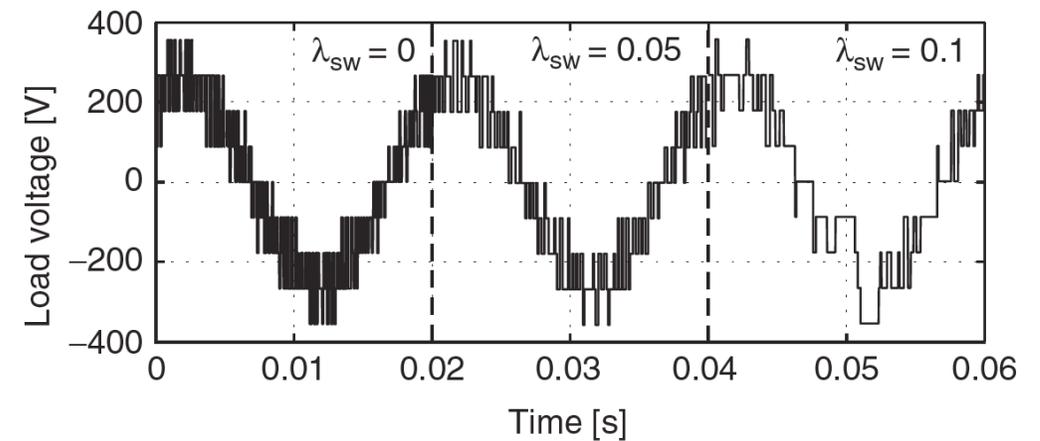
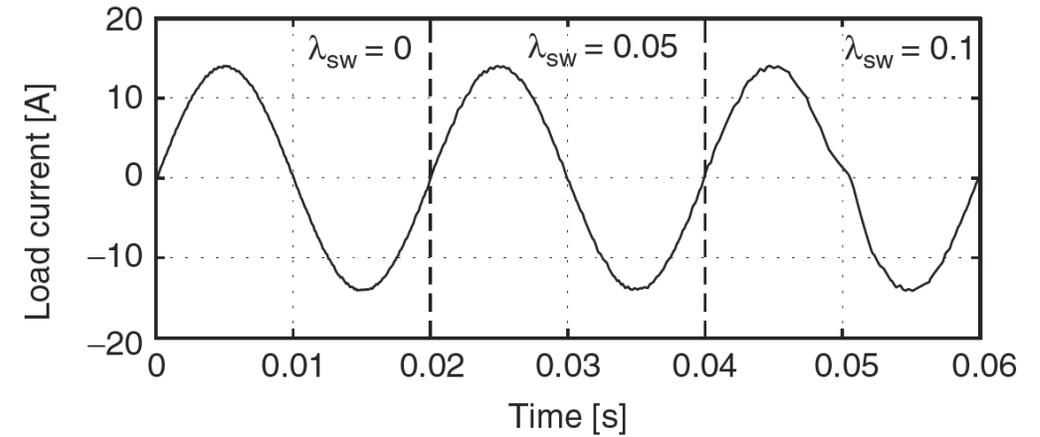
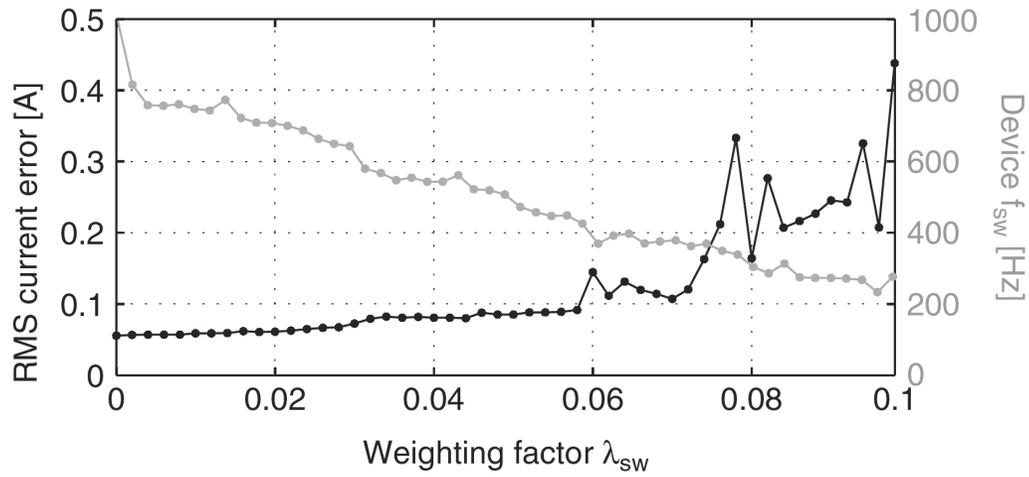
Weighting factor design methods



## - Selection of Weighting Factors: Examples

### Switching Frequency Reduction

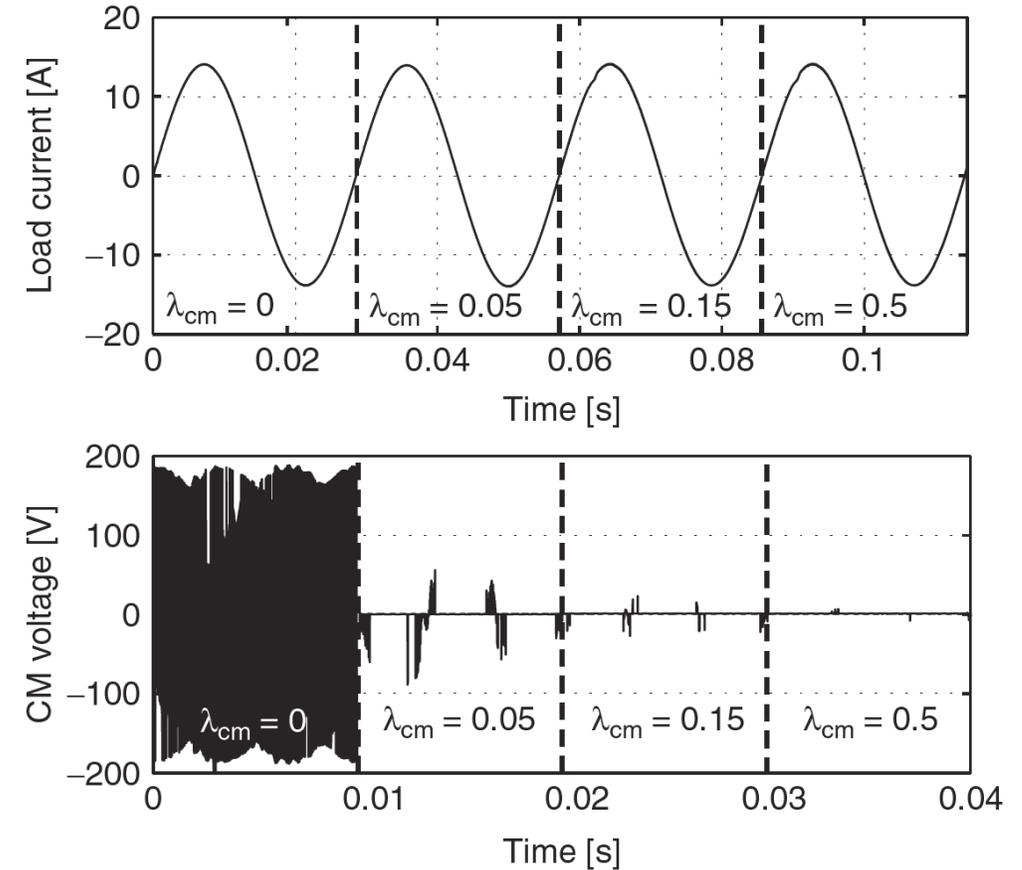
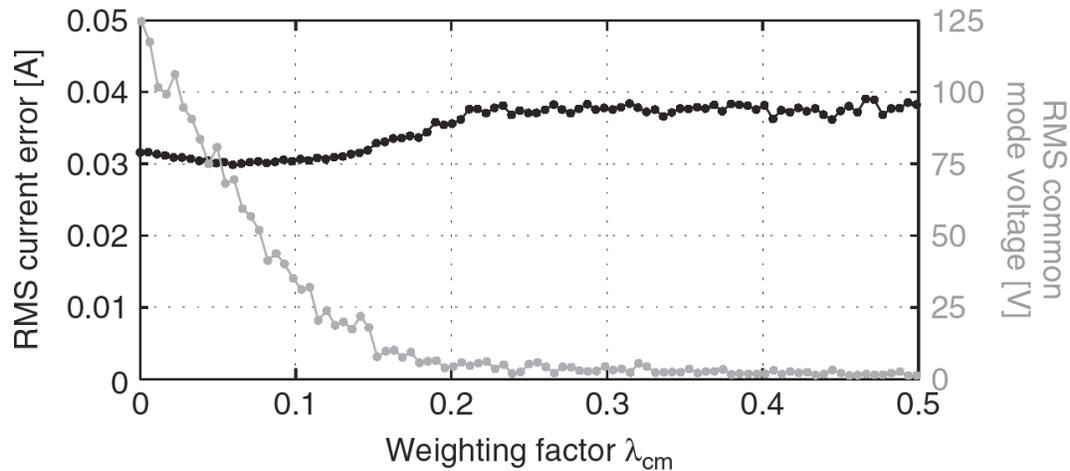
$$g = |i_{\alpha}^* - i_{\alpha}^p| + |i_{\beta}^* - i_{\beta}^p| + \lambda_{sw} n_{sw}^p$$



## - Selection of Weighting Factors: Examples

### Common-Mode Voltage Reduction

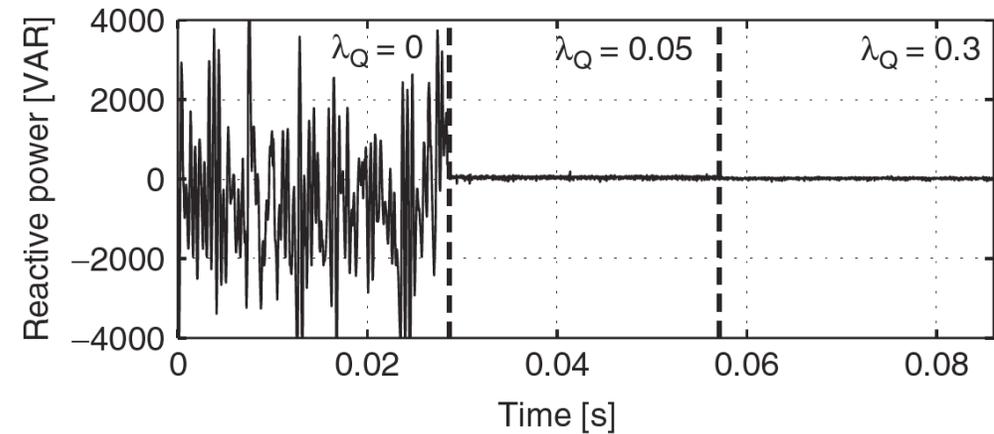
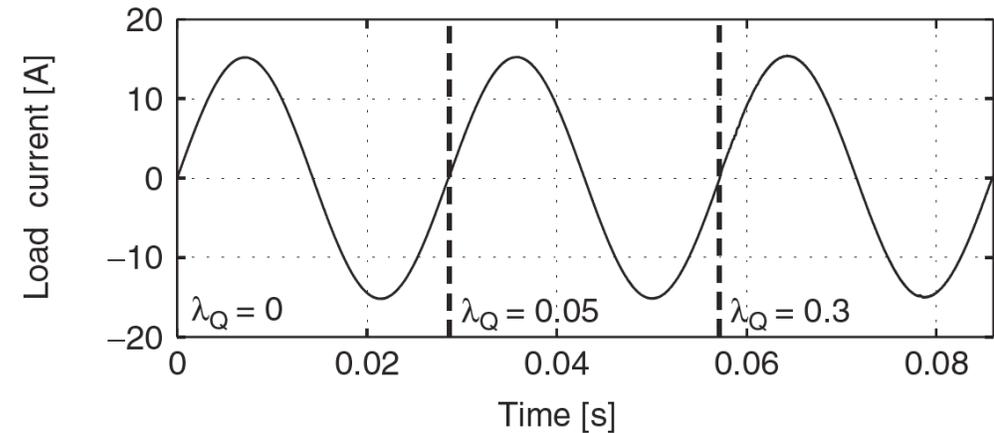
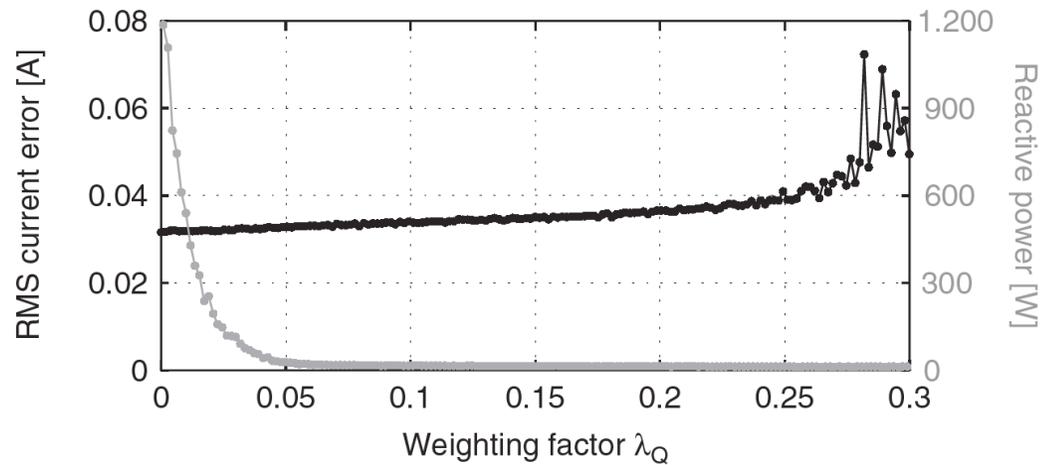
$$g = |i_{\alpha}^* - i_{\alpha}^p| + |i_{\beta}^* - i_{\beta}^p| + \lambda_{cm} |V_{cm}^p|$$



## - Selection of Weighting Factors: Examples

### Input Reactive Power Reduction

$$g = |i_{\alpha}^* - i_{\alpha}^p| + |i_{\beta}^* - i_{\beta}^p| + \lambda_Q |Q^p|$$





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## Predictive Control for Power Converters and Electrical Drives

# Trends and Challenges of Predictive Control



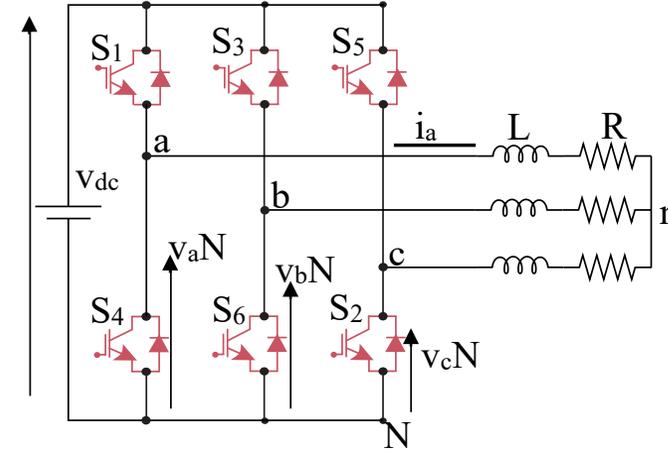
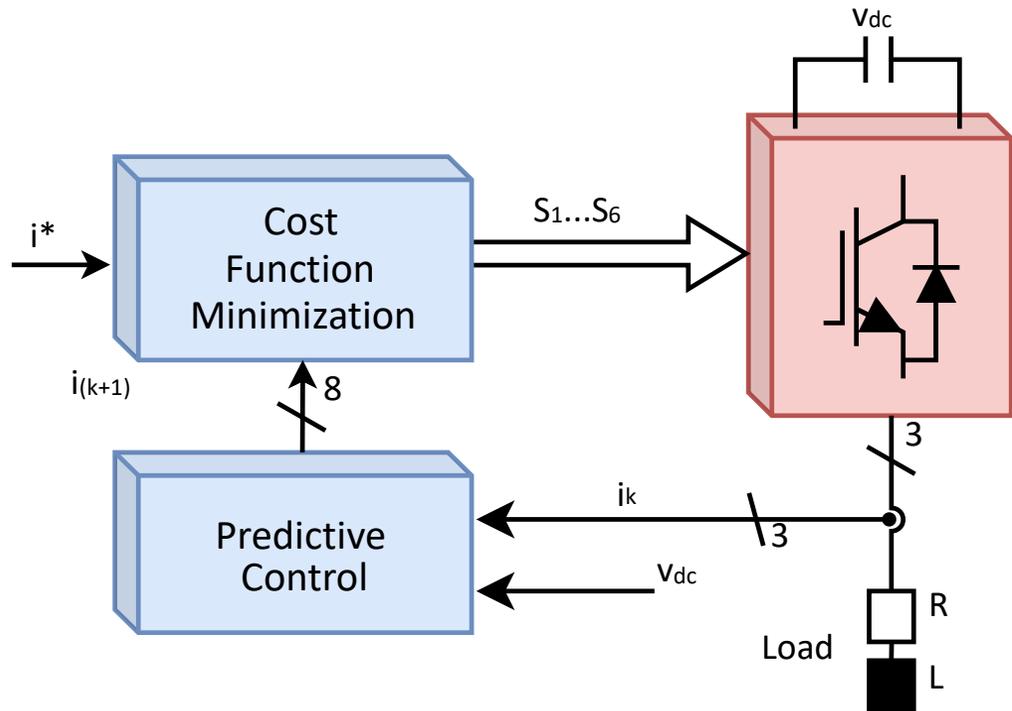
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## Predictive Control for Power Converters and Electrical Drives

# Modulated MPC for Power Converters

## - PCC of a Two-Level Voltage Source Inverter: Control Scheme

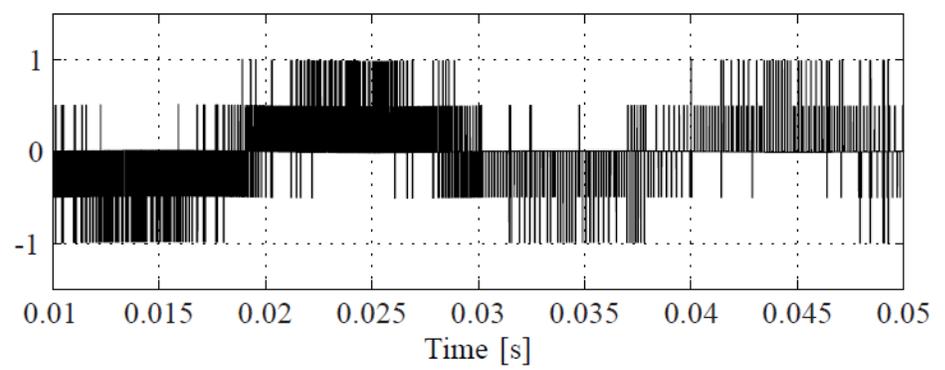
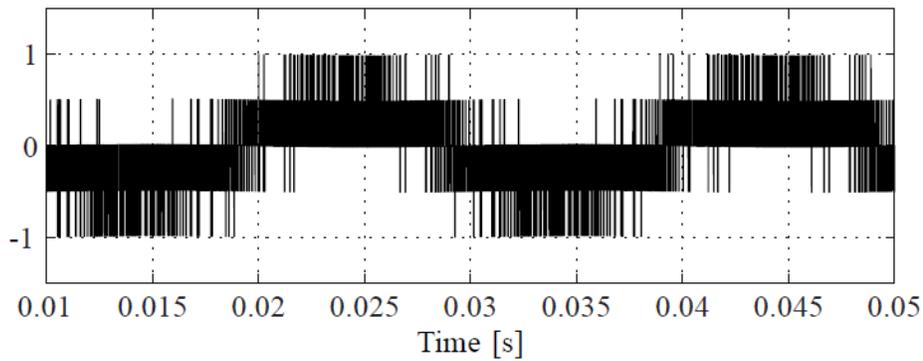
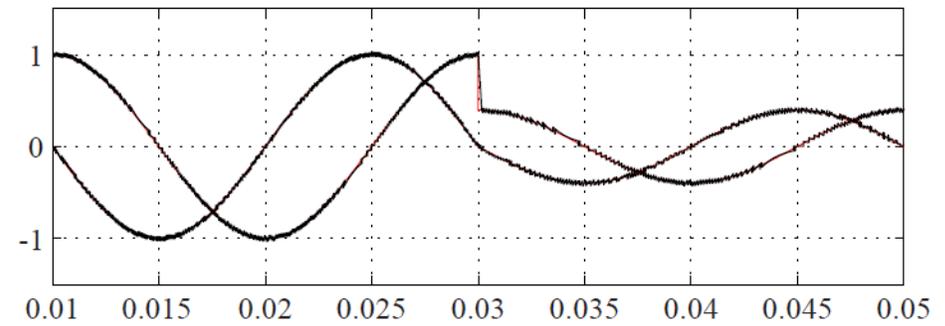
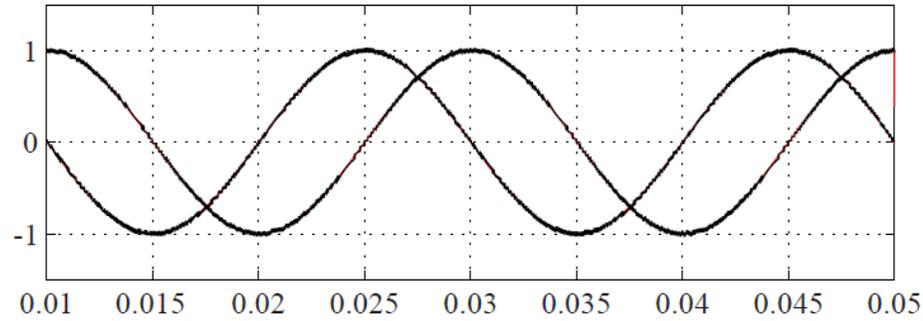


Valid Switching state of the VSI

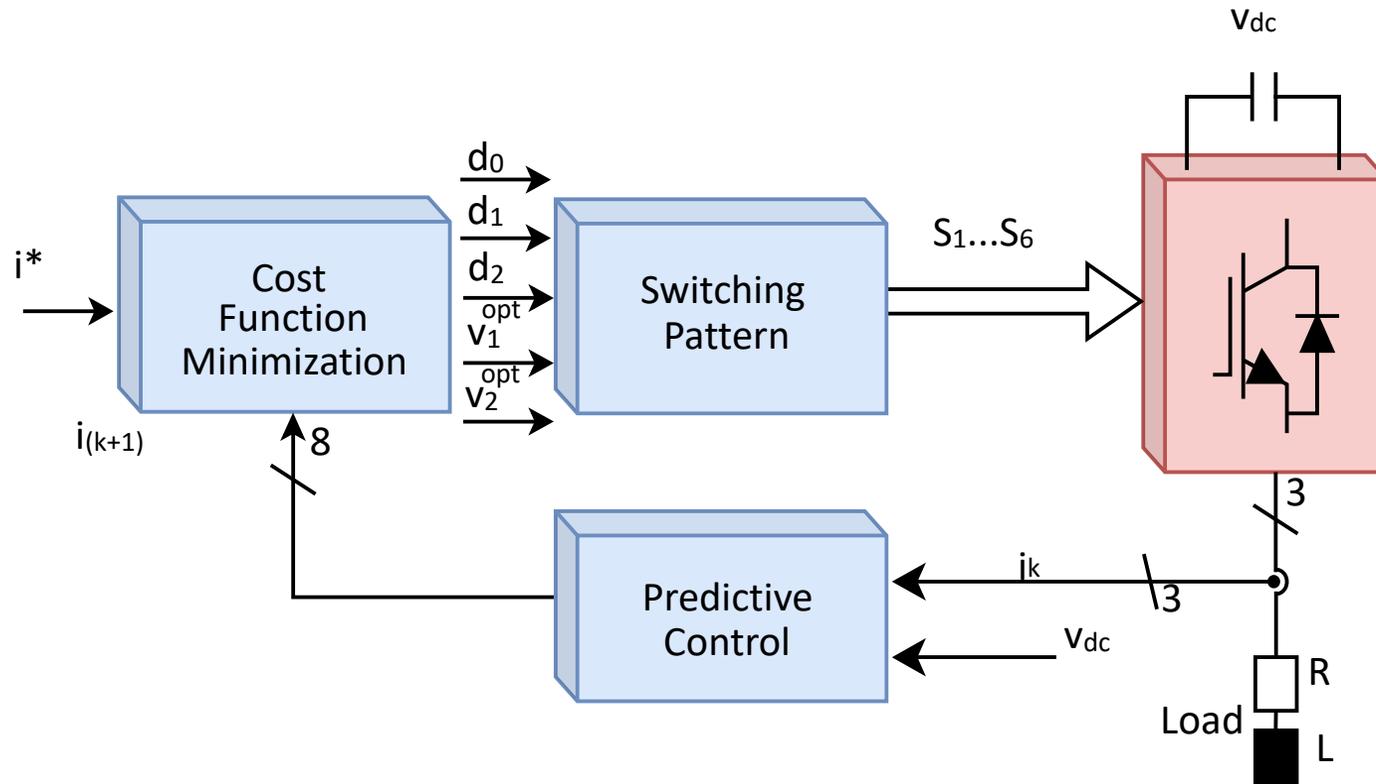
| # | $S_{r1}$ | $S_{r2}$ | $S_{r3}$ | $S_{r4}$ | $S_{r5}$ | $S_{r6}$ |
|---|----------|----------|----------|----------|----------|----------|
| 1 | 1        | 1        | 0        | 0        | 0        | 1        |
| 2 | 1        | 1        | 1        | 0        | 0        | 0        |
| 3 | 0        | 1        | 1        | 1        | 0        | 0        |
| 4 | 0        | 0        | 1        | 1        | 1        | 0        |
| 5 | 0        | 0        | 0        | 1        | 1        | 1        |
| 6 | 1        | 0        | 0        | 0        | 1        | 1        |
| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |



## - Modulated MPC for the Three-Phase Voltage Source Inverter: Results

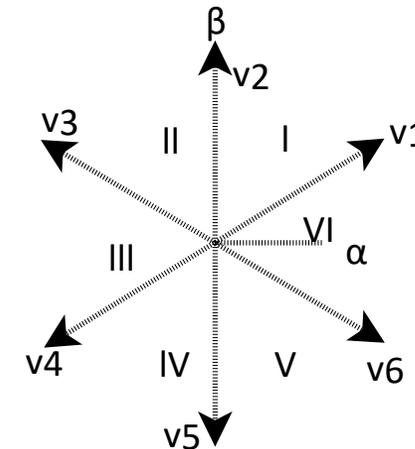


## - Modulated MPC for the Three-Phase VSI: Control Scheme



Valid Switching state of the VSI

| # | $S_{r1}$ | $S_{r2}$ | $S_{r3}$ | $S_{r4}$ | $S_{r5}$ | $S_{r6}$ |
|---|----------|----------|----------|----------|----------|----------|
| 1 | 1        | 1        | 0        | 0        | 0        | 1        |
| 2 | 1        | 1        | 1        | 0        | 0        | 0        |
| 3 | 0        | 1        | 1        | 1        | 0        | 0        |
| 4 | 0        | 0        | 1        | 1        | 1        | 0        |
| 5 | 0        | 0        | 0        | 1        | 1        | 1        |
| 6 | 1        | 0        | 0        | 0        | 1        | 1        |
| 7 | 1        | 0        | 1        | 0        | 1        | 0        |
| 8 | 0        | 1        | 0        | 1        | 0        | 1        |



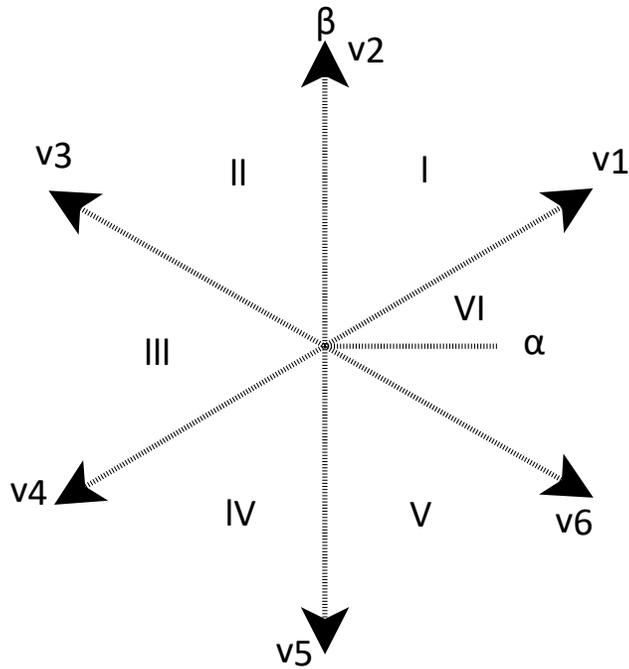
## - Modulated MPC for the Three-Phase Voltage Source Inverter

$$g(k + 1) = d_1 g_1 + d_2 g_2$$

$$d_0 = T_s g_1 g_2 / (g_0 g_1 + g_1 g_2 + g_0 g_2)$$

$$d_1 = T_s g_0 g_2 / (g_0 g_1 + g_1 g_2 + g_0 g_2)$$

$$d_2 = T_s g_0 g_1 / (g_0 g_1 + g_1 g_2 + g_0 g_2)$$

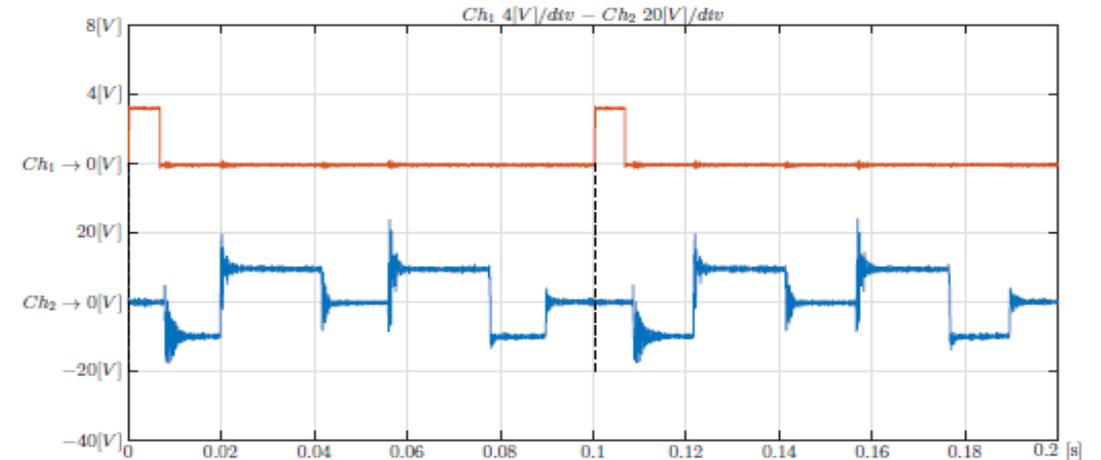


$$d_0 = K/g_0$$

$$d_1 = K/g_1$$

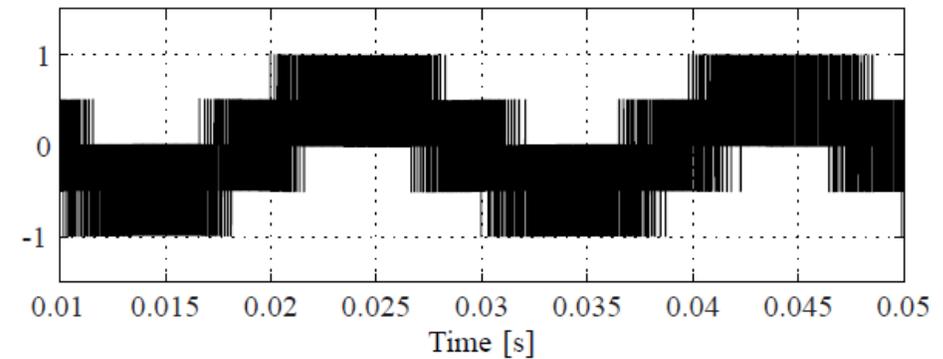
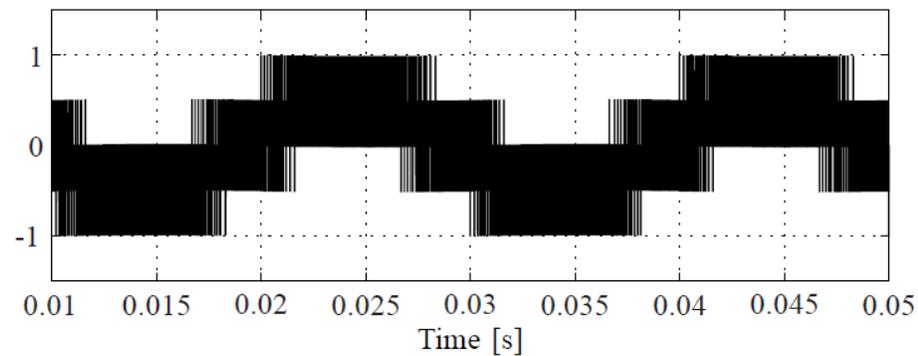
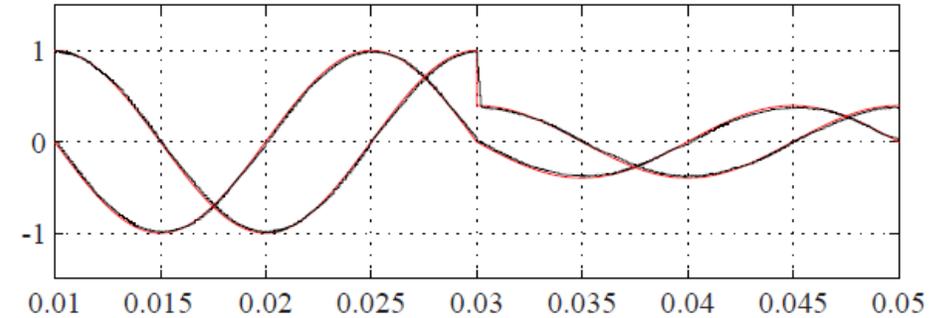
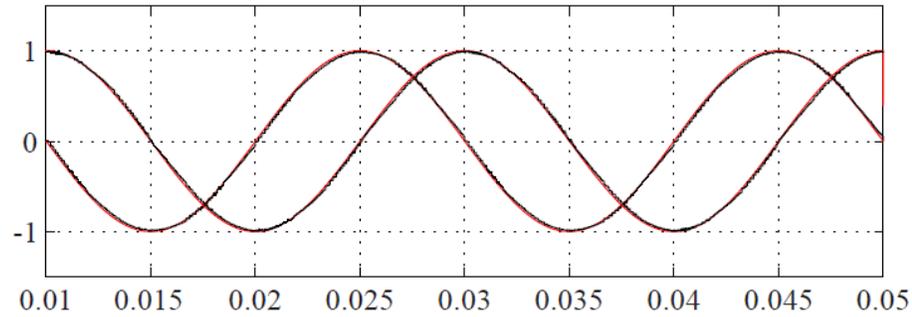
$$d_2 = K/g_2$$

$$d_0 + d_1 + d_2 = T_s$$



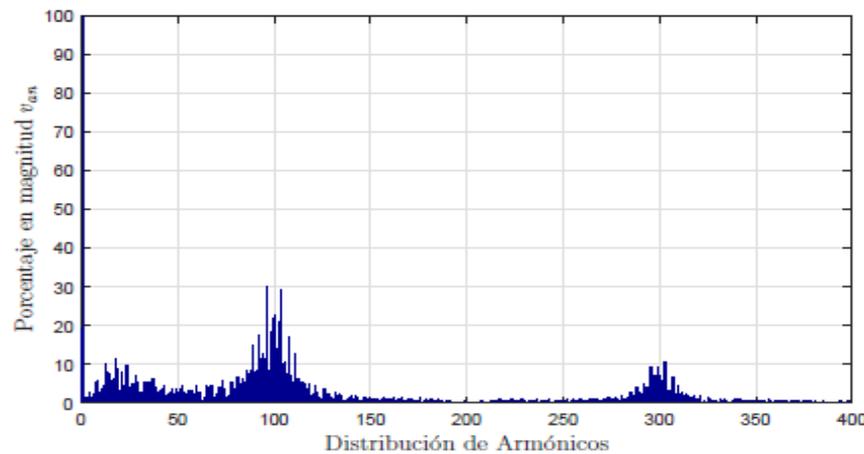
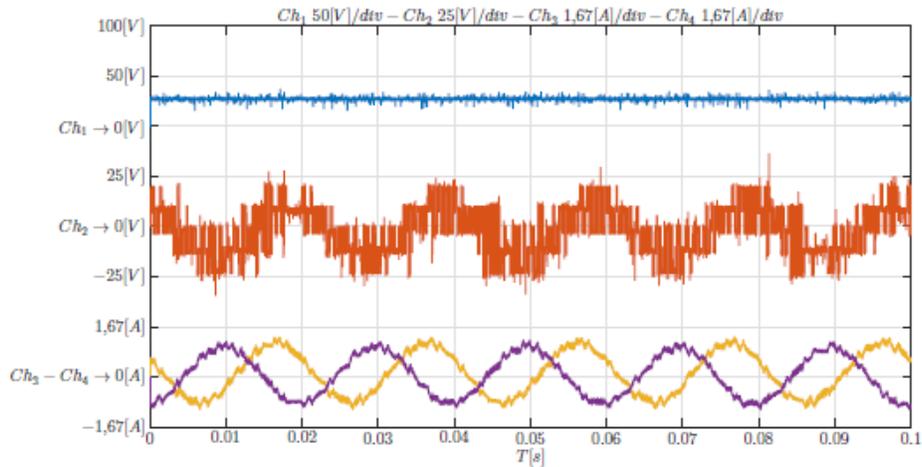


## - Modulated MPC for the Three-Phase Voltage Source Inverter: Results

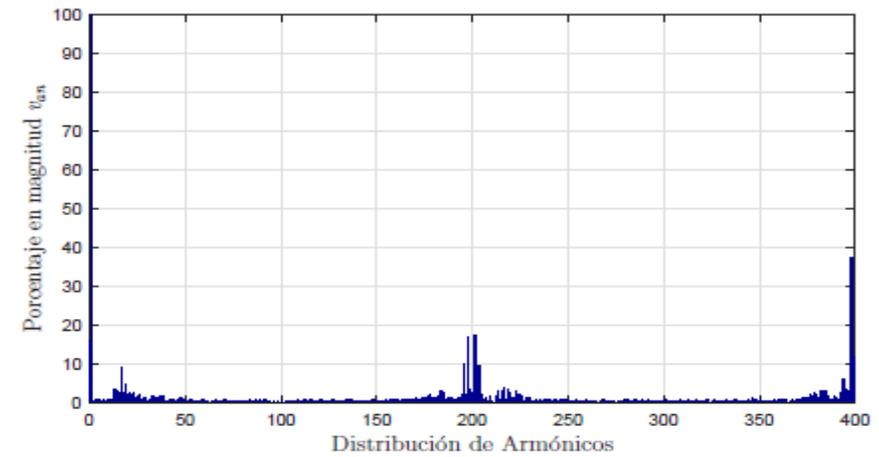
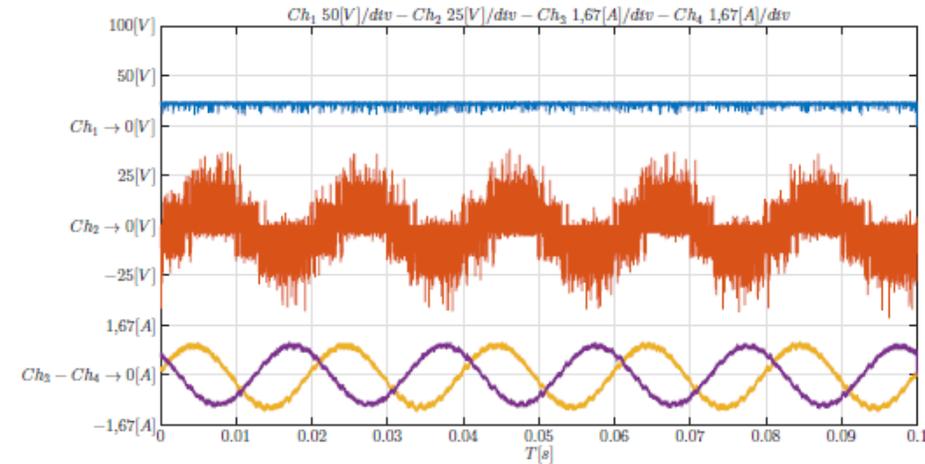




## - Modulated MPC for the Three-Phase VSI : Experimental Results



Classical MPC



Modulated MPC



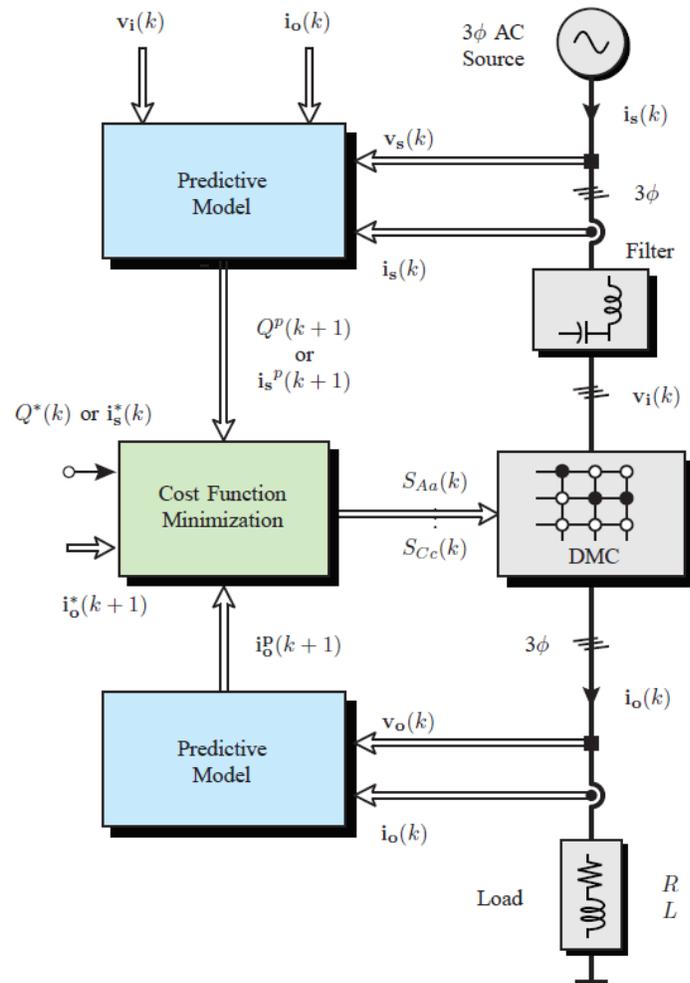
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## Predictive Control for Power Converters and Electrical Drives

# Sequential MPC for Power Converters

## - Predictive Control Strategies for the DMC



### - The main idea of Model Predictive Control

- Both input and output stages are controlled simultaneously using a predictive model of the instantaneous reactive power and a predictive model of the load.
- A **weighting factor is necessary** in order to provide more priority to the instantaneous reactive input power of the load currents.
- The cost function is evaluated for each of the twenty-seven available switching states of the DMC.
- The **optimal switching state which will be applied** to the converter in the next sampling instant, is selected by **minimizing the cost function**.



## - Predictive Control Strategies for the DMC: Introduction

### - Model Predictive Control: General Concept

#### - Despite the vast progress of MPC, there are still some issues that need to be solved:

- The control for the DMC and other power converters implies high computational costs
  - Every sampling instant **all the available switching states** of the converter **are evaluated** in the cost function.
  - The DMC has **27 available switching states**.
  - Some available solutions: **implementation in FPGAs or faster digital signal processors**.
- The correct selection of weighting factors:
  - Especially **when there are several control objectives**.
  - The correct selection has a **significant effect on the system performance**.
  - Despite there are some solutions, most of them are **tedious, complex and expensive**.



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## - Sequential MPC for a Direct Matrix Converter

Article

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# Sequential Model Predictive Control of Three-Phase Direct Matrix Converter

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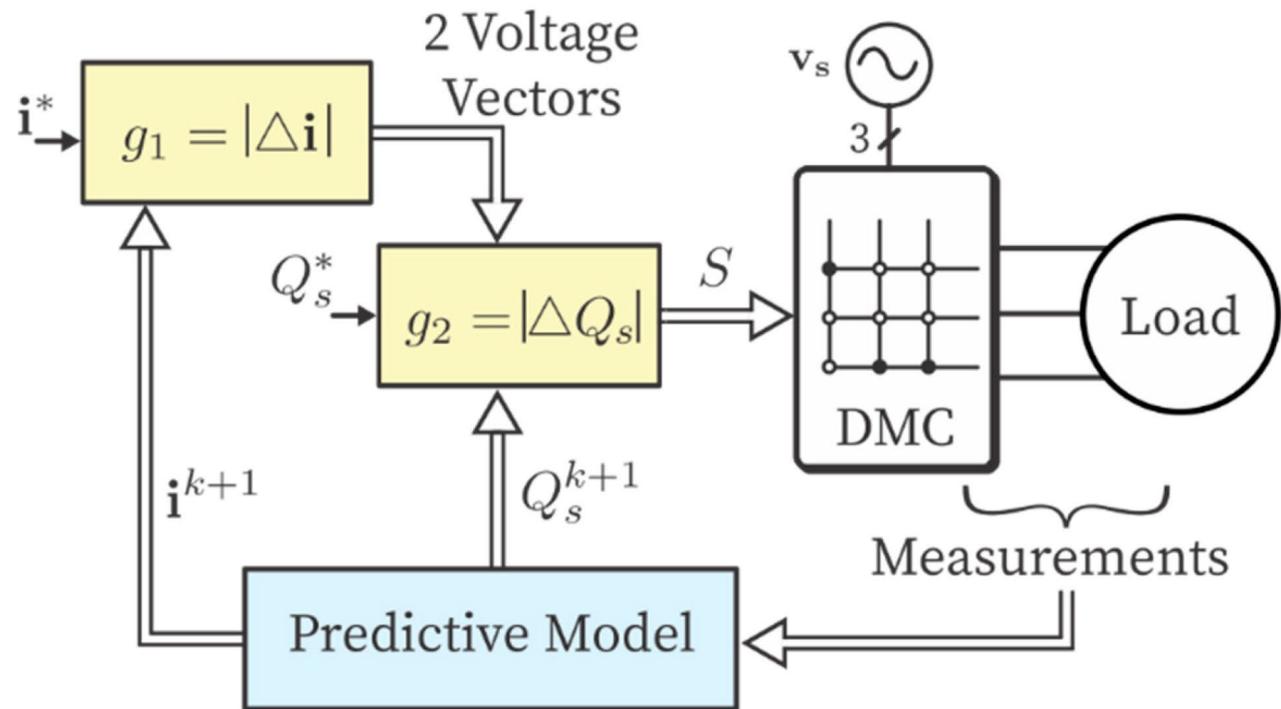
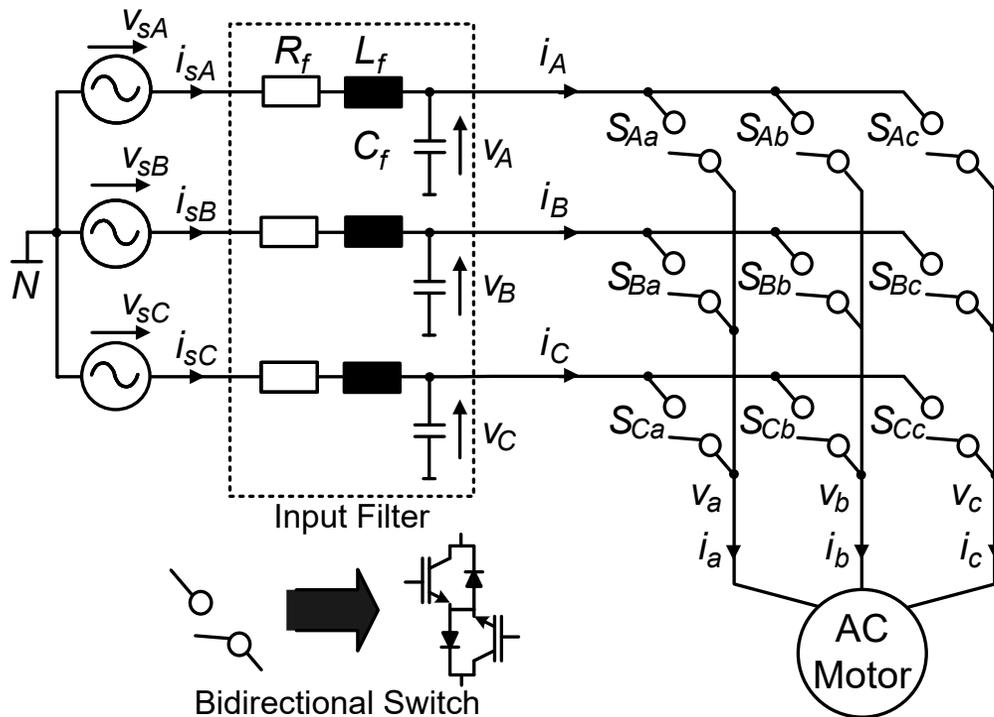
Jianwei Zhang, Margarita Norambuena, Li Li, David Dorrell and Jose Rodriguez

Special Issue

Control in Power Electronics

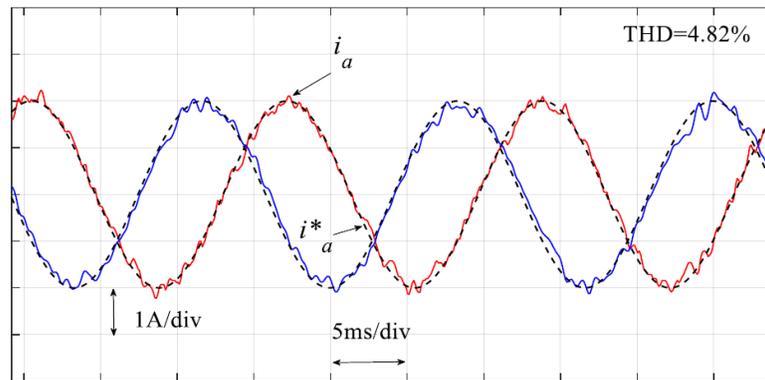
Edited by  
Prof. Dr. George Weiss and Prof. Dr. Yoash Levron

## - Sequential MPC for a Direct Matrix Converter

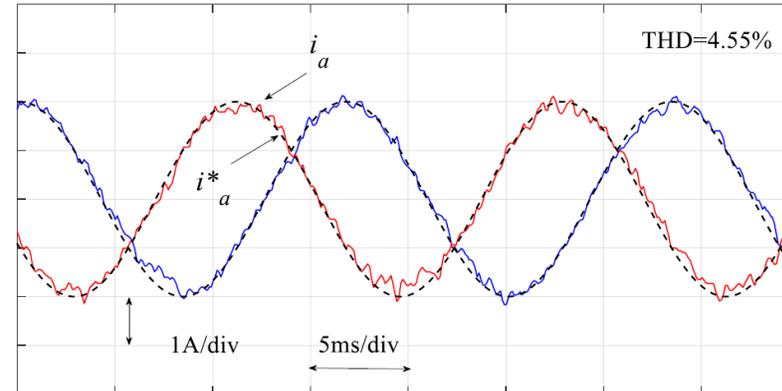


Block diagram of the Sequential Model Predictive Control for the Direct Matrix Converter

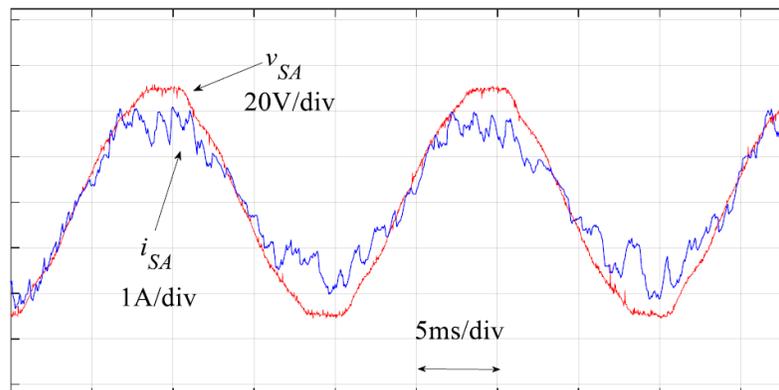
## - Sequential MPC for a Direct Matrix Converter



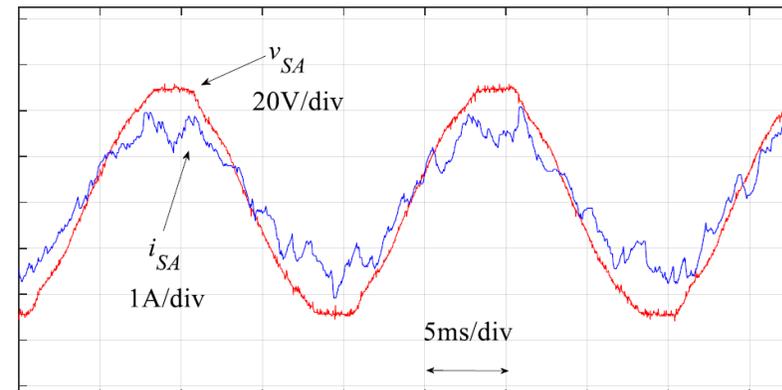
Load currents and references - classic MPC



Load currents and references - proposed SMPC

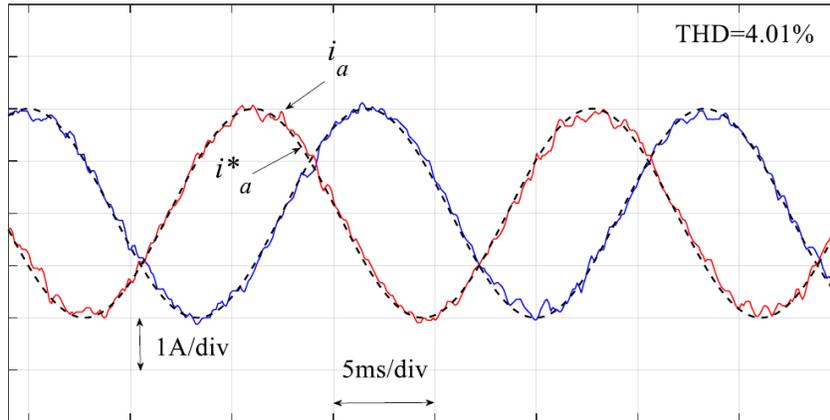


Input current and voltage - classic MPC

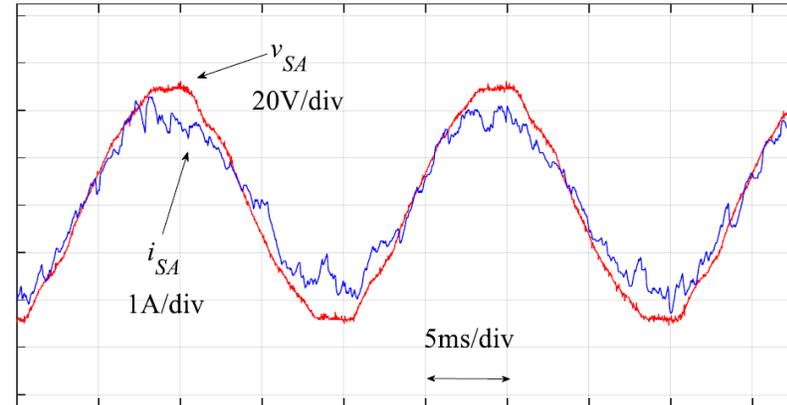


Input current and voltage - proposed SMPC

## - Sequential MPC for a Direct Matrix Converter



Load currents and references - proposed MPC



Input current and voltage - proposed SMPC

The execution time of the proposed SMPC (67  $\mu$ s) is reduced appreciably compared with the traditional MPC (81  $\mu$ s).

# - Alternating Sequential MPC for a Direct Matrix Converter

Conferences > 2023 IEEE International Confe... ?

## Alternating Sequential Model Predictive Control of Matrix Converter

Publisher: IEEE

Cite This

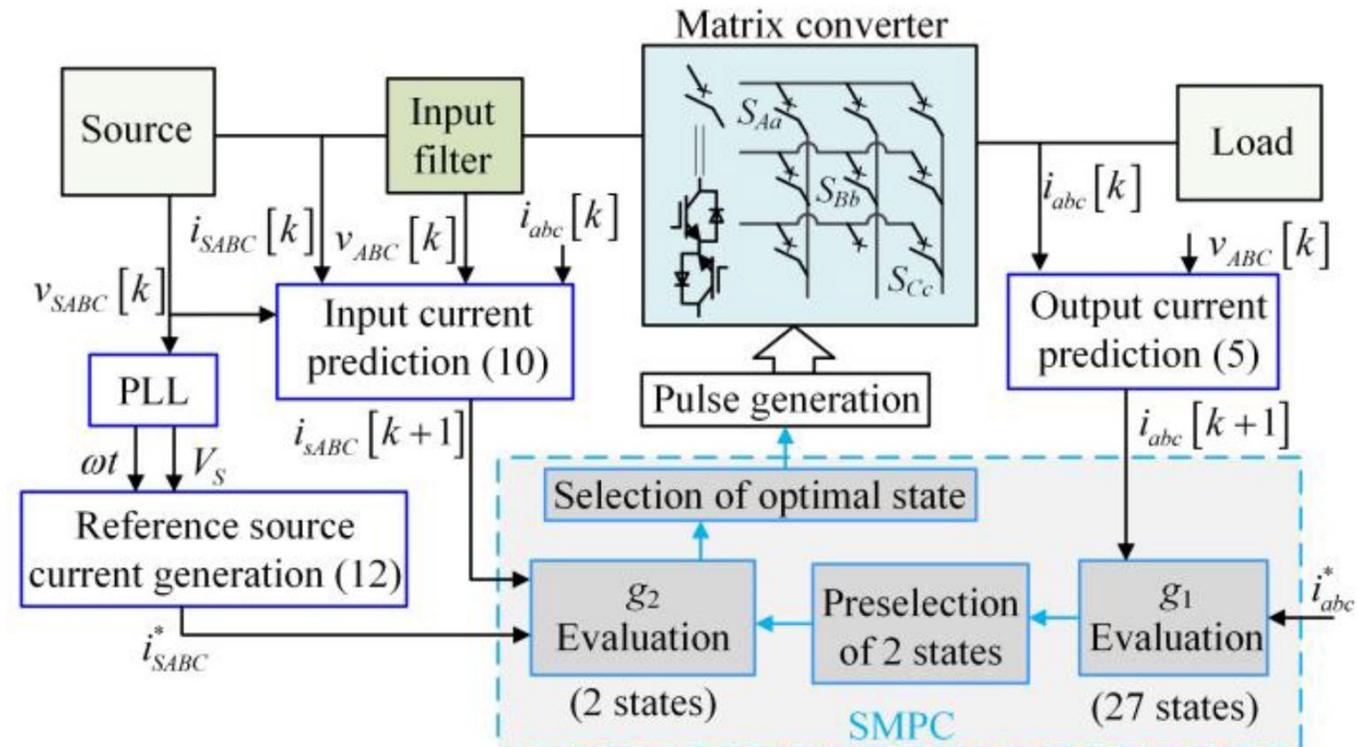
PDF

Jianwei Zhang ; Marco Rivera ; Patrick Wheeler All Authors

The **cost functions are evaluated in an alternating order**. For example,  $g_1$  is evaluated before  $g_2$  in the first sampling cycle and  $g_2$  is evaluated before  $g_1$  in the next sampling cycle, and so on.

The proposed ASMPC does **not need a weighting factor** and there is **no need to specify the priority for control objectives**.

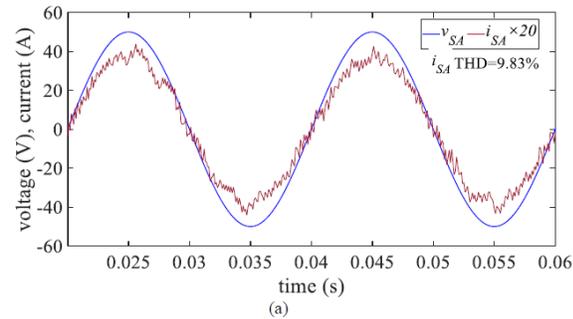
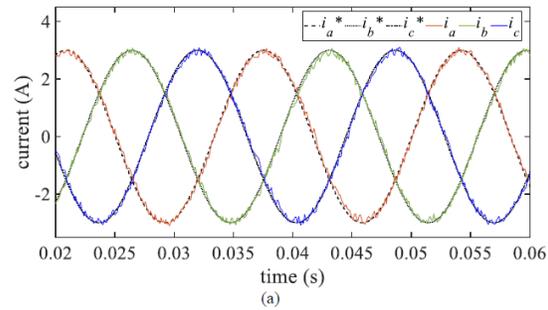
In addition, the **computational burden is reduced** because only two switch states are evaluated in the second cost function in each control interval.



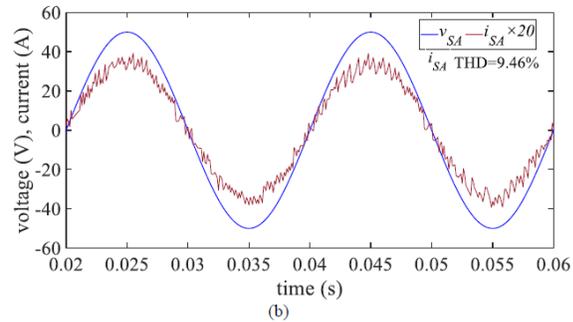
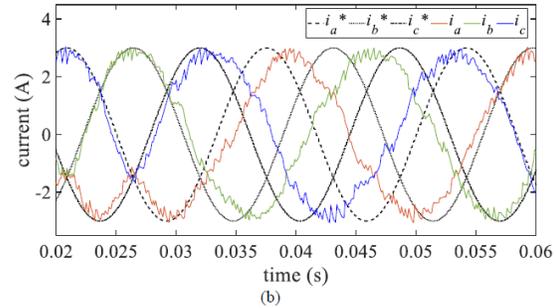


# - Alternating Sequential MPC for a Direct Matrix Converter

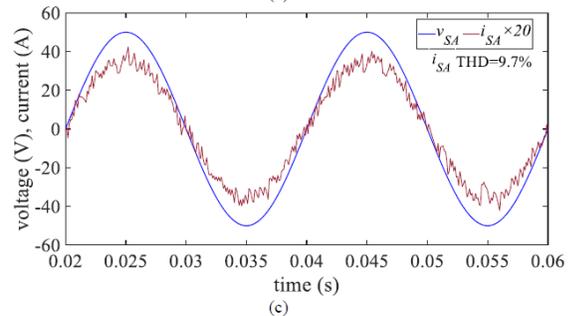
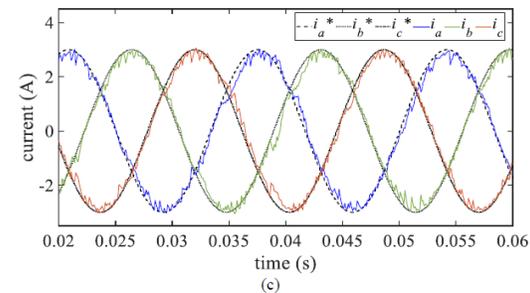
SMPC 1



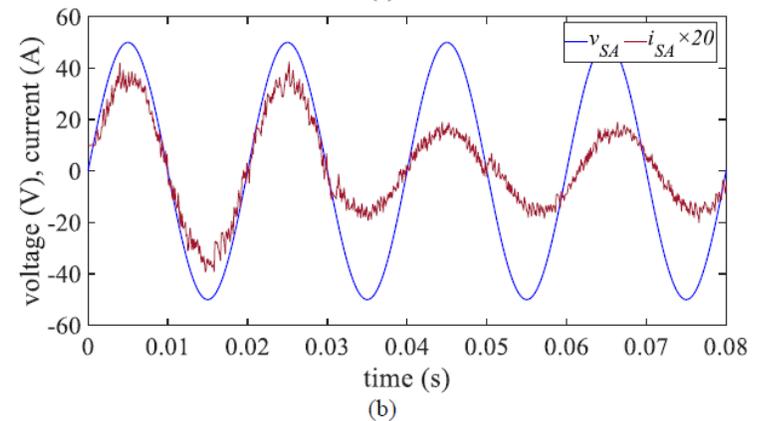
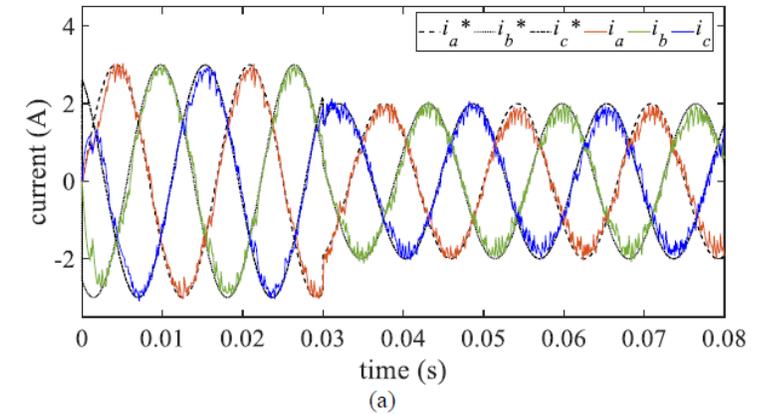
SMPC 2



ASMPC



ASMPC transient state





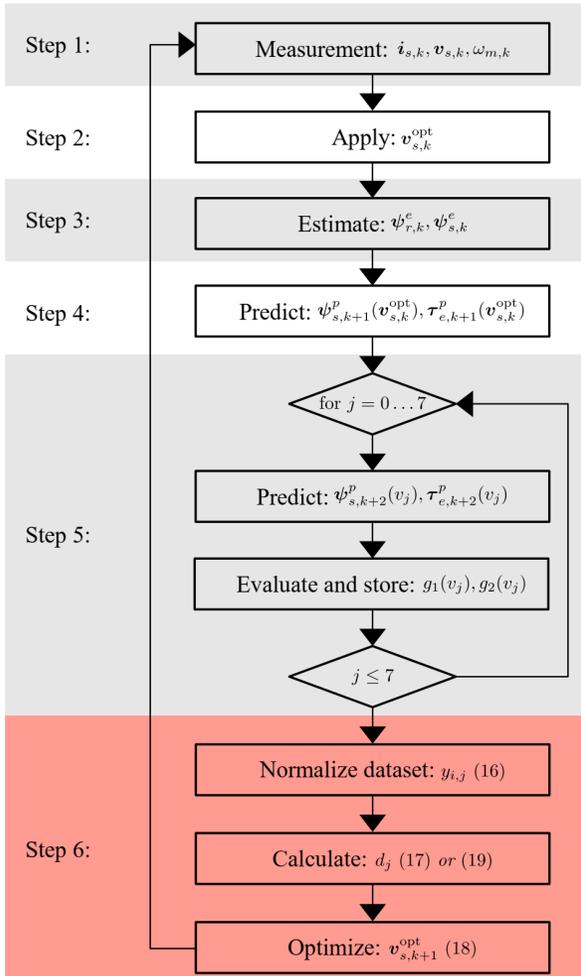
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## Predictive Control for Power Converters and Electrical Drives

# MPC based on Decision-Making Algorithms

## - A Decision-Making Algorithm for MPC Strategies



The decision-making algorithm with the flowchart on the left has the following steps:

1. Separation of multi-objective cost function:

$$g_1 = \left| \tau_e^* - \tau_{e,k+2}^p \right|$$

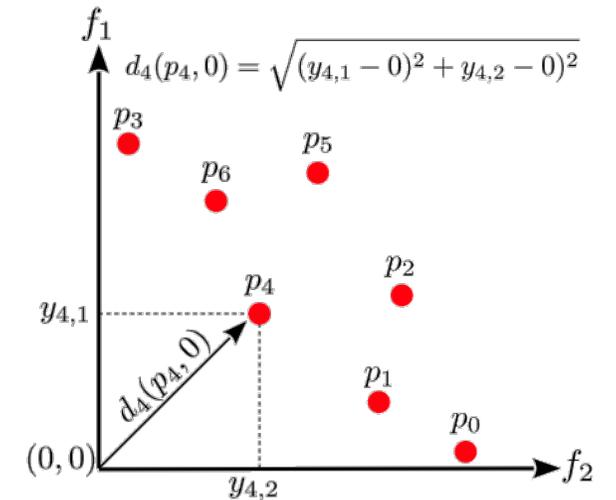
$$g_2 = \left| \|\psi_s^*\| - \|\psi_{s,k+2}^p\| \right|$$

2. Generation of dataset:

$$x_{ij} = \begin{pmatrix} g_1(v_0) & g_2(v_0) & \dots & g_n(v_0) \\ g_1(v_1) & g_2(v_1) & \dots & g_n(v_1) \\ \vdots & \vdots & \ddots & \vdots \\ g_1(v_m) & g_2(v_m) & \dots & g_n(v_m) \end{pmatrix}$$

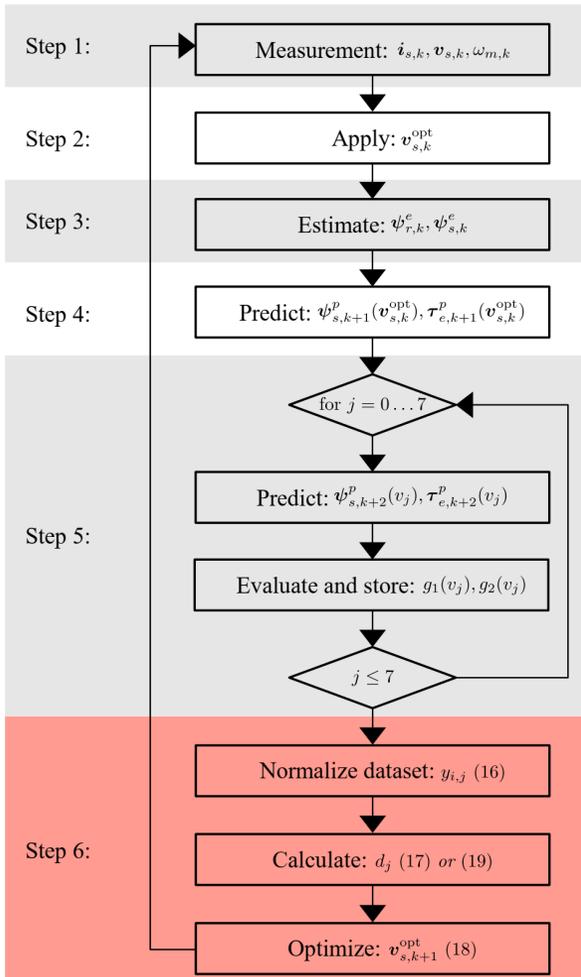
where  $i \in \{1, 2, \dots, n\}$  and  $j \in \{0, 1, \dots, m\}$  indicate the number of control objectives and voltage vectors, respectively.

For more information about this technique. Please click [here](#).



Decision-making methods separately evaluate each control objective in the cost function and then use a selection algorithm to choose an optimal voltage vector.

## - A Decision-Making Algorithm for MPC Strategies



3. Normalization of the dataset:

$$y_{ij} = \frac{x_i^{\min} - x_{ij}}{x_i^{\min} - x_i^{\max}}$$

4. Calculate the distances in the  $n$  –dimensional space using the normalized dataset

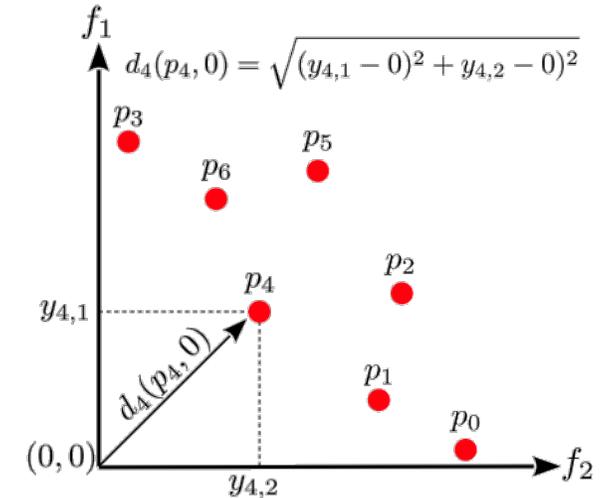
$$d_j(p_j, 0) = \sqrt{(y_{j,1})^2 + (y_{j,2})^2 + \dots + (y_{j,n})^2}$$

or

$$d_j(p_j, 0) = y_{j,1} + y_{j,2} + \dots + y_{j,n}$$

5. Select the  $j$ th voltage vector with minimum norm value:

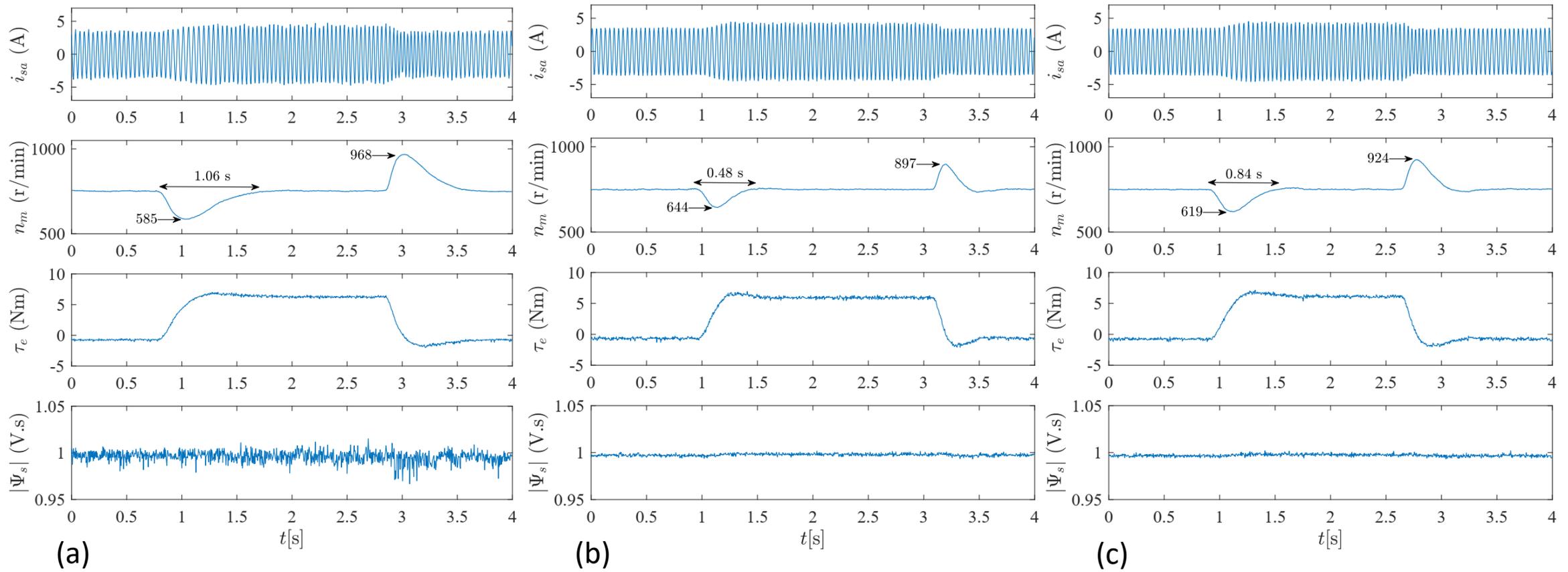
$$v_{opt} = \arg \min_j d_j$$



Euclidean norm

Absolute-value norm

## - A Decision-Making Algorithm for MPC Strategies



Experimental results: Control performance under load changes of 6 Nm at 750 r/min (a) conventional MPTC with  $\lambda_\psi = 20$  (b) DM-based MPTC with Euclidean norm (c) DM-based MPTC with absolute-value norm



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## Predictive Control for Power Converters and Electrical Drives

# Conclusions and Final Remarks



## Conclusions

- MPC presents a **different approach** for the control of power converters.
- MPC takes advantages of the **discrete nature** of the power converters.
- By using the same scheme, it is possible to control **different variables** such as: current, voltage, power, torque, flux, and others.
- **Constrains** and **non-linearities** can be easily included in the model.
- The control is **simple** and can be easily applied to any converter topology.



## Conclusions

- Challenges such as the **performance improvement**, **reduction of computational cost** and the **avoidance of weighting factors** have been considered **new trends in model predictive control** and several proposals have been recently presented.
- **Modulated model predictive control** allows for improving the performance of the system with **a significant reduction of the ripple** in the controller variables.
- **Sequential model predictive control** does not require the use of **weighting factors** in the cost function. It allows for effective control of several variables at the same time.



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## Predictive Control for Power Converters and Electrical Drives

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## Predictive Control for Power Converters and Electrical Drives

# Discussions and Questions



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# Model Predictive Control for Power Electronics Applications

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